

Higher-order Networks for Anomaly Detection

2nd KDD Workshop on Anomaly Detection in Finance



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Research by

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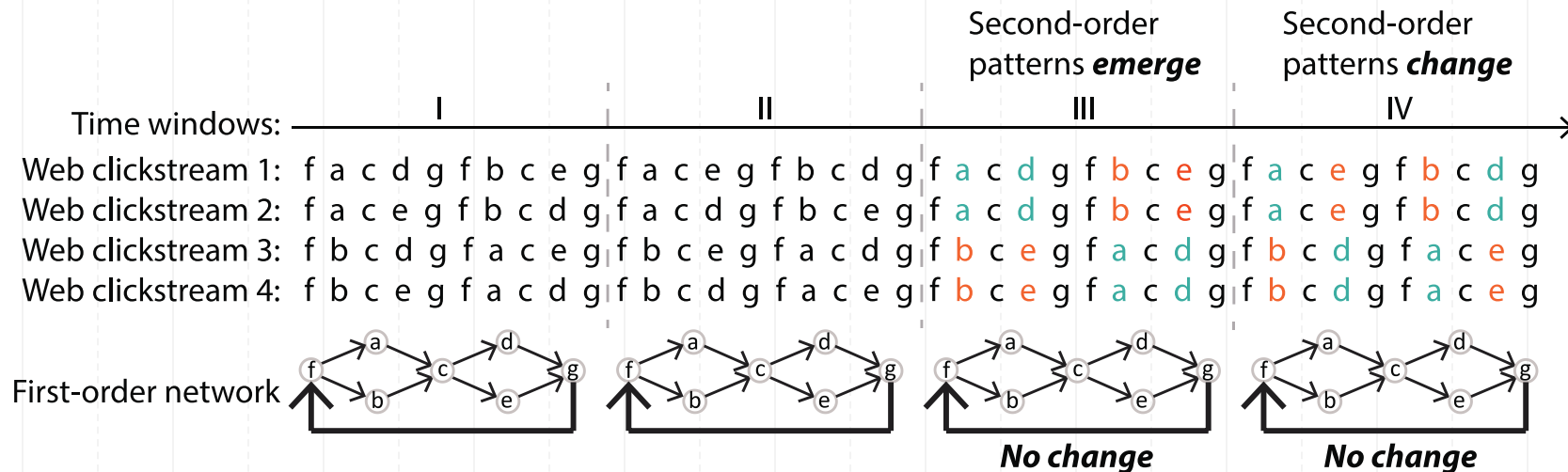
Anomaly detection and higher-order patterns

- Anomalies are deviations from the expected behavior of a complex system
- It is important that the data representation does not lose important information
- Current network-based anomaly detection methods use the First-Order Network (FON) to represent the underlying raw data
- What if we miss anomalies that are only discoverable through **higher-order patterns**?



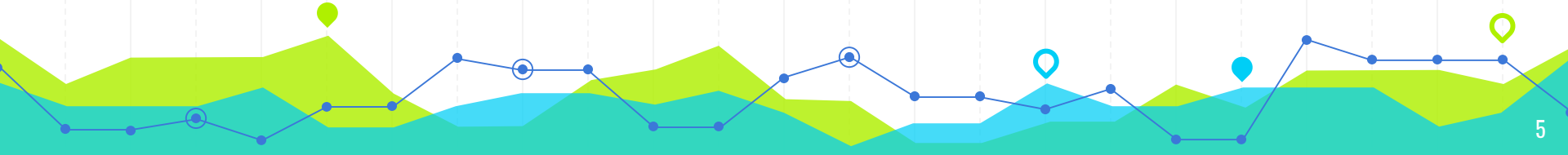
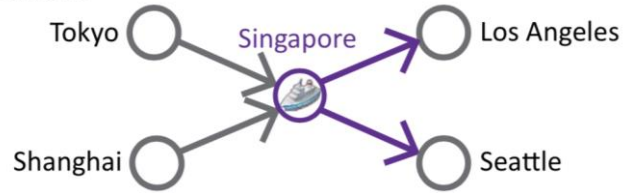
Example: Clickstream data

Anomalies completely hidden in FON



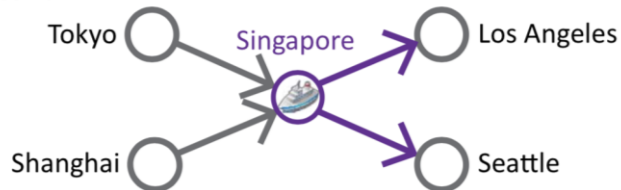
Higher-Order Network

First-order network



Higher-Order Network

First-order network

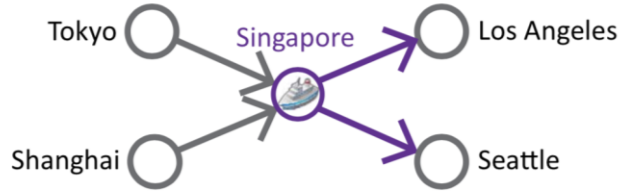


Higher-order network (HON)



Higher-Order Network

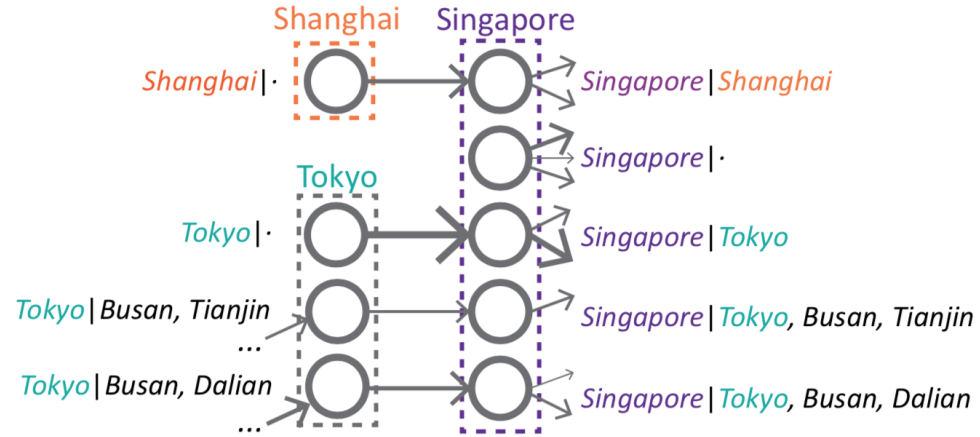
First-order network



Higher-order network (HON)

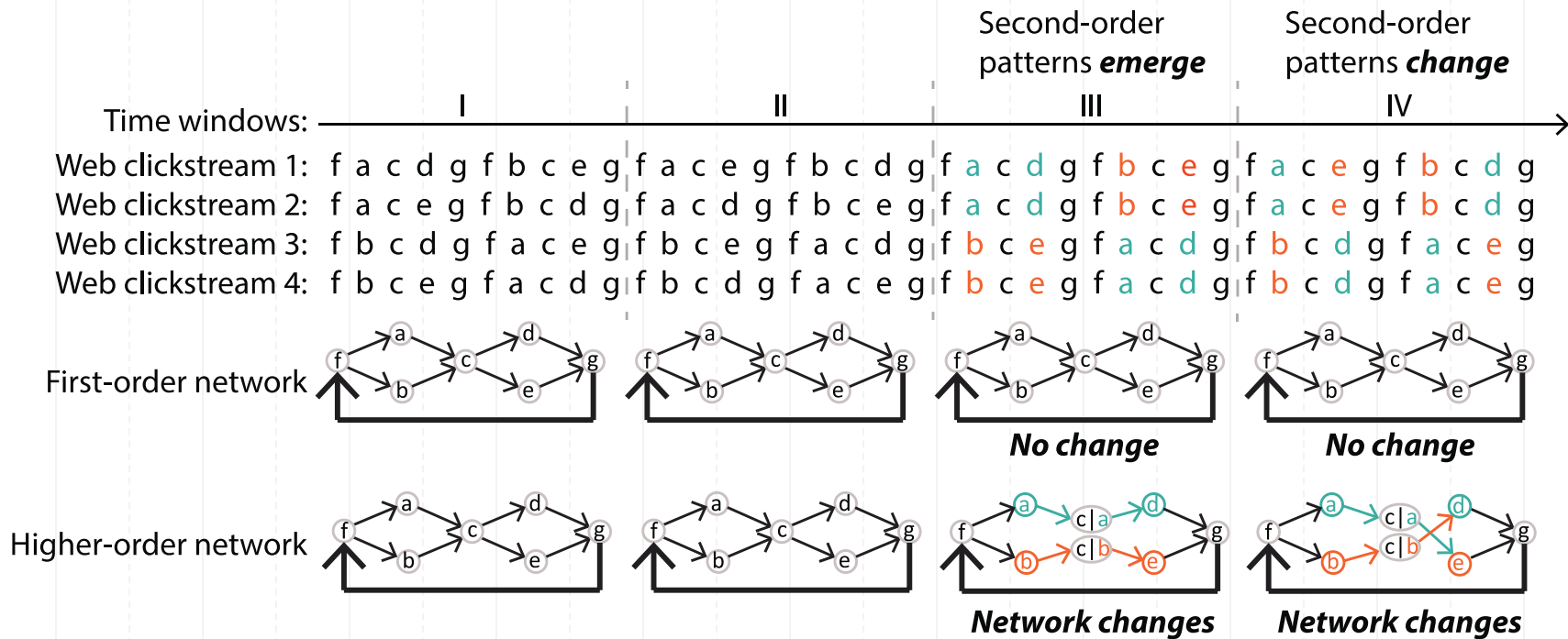


Variable orders of dependencies in HON



Example: Clickstream data

Anomalies revealed by representing data as HON



Anomaly detection in dynamic networks

**Network
construction
(w/ BuildHON+)**

**Calculating
network
distances**

**Detecting
Anomalies**

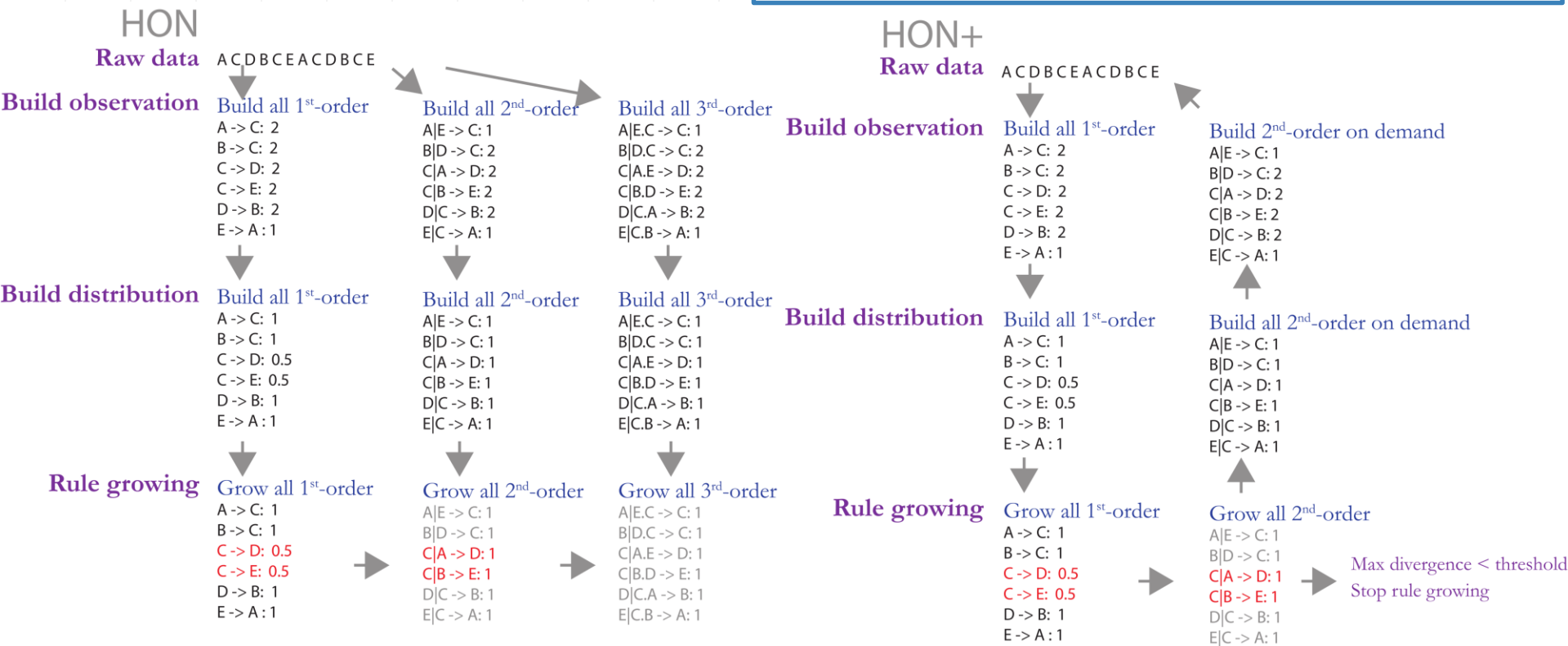
BuildHON+

Compared to the original HON construction algorithm*, BuildHON+ is

- Parameter-free
- More effective finding higher-order patterns (order 10 or higher)
- A magnitude faster with early stopping heuristics
- Python package available**

* Xu, Jian, Thanuka L. Wickramaratne, and Nitesh V. Chawla. "Representing higher-order dependencies in networks." *Science advances* 2, no. 5 (2016): e1600028.

** <https://github.com/xyjprc/hon>



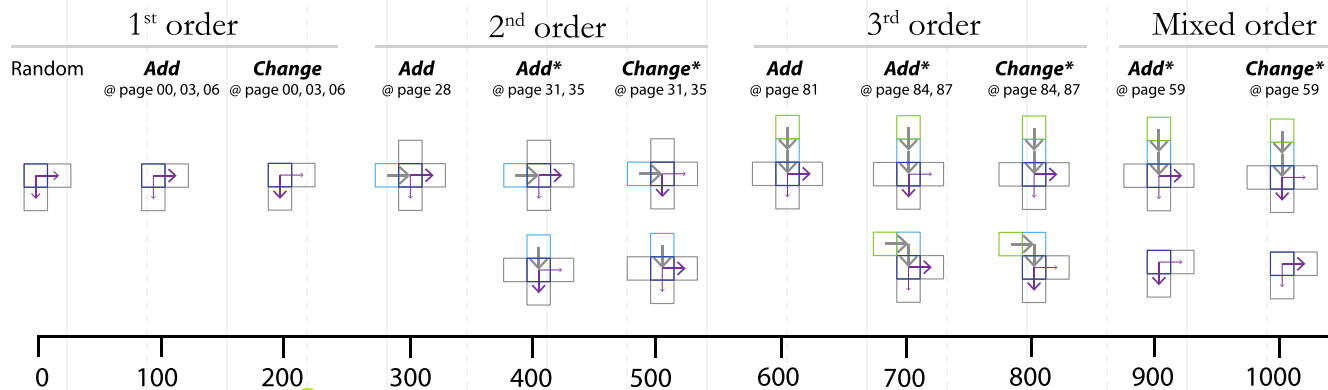
Results



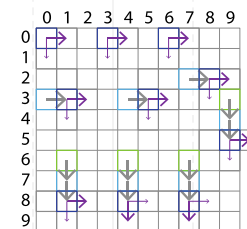
Synthetic data creation

- Web clickstream of 100,000 users navigating through 100 webpages, organized as a 10x10 grid
- Users change navigation behavior every 100 time windows
- Ground truth: 11 known anomalies of different natures (change of patterns of various orders)
- 11,000,000,000 clicks for anomaly detection task

Legend  Current page  Next page  Previous page  Previous of previous page  Next click  Previous click(s)



Locations of injected anomalous clicking behaviors



Synthetic data results

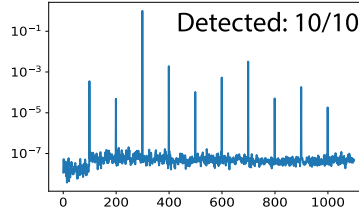
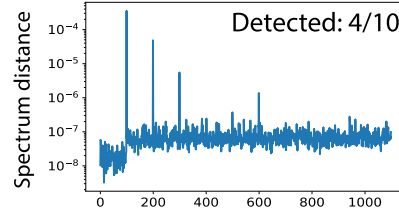
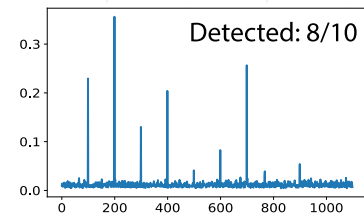
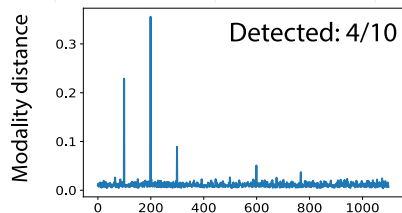
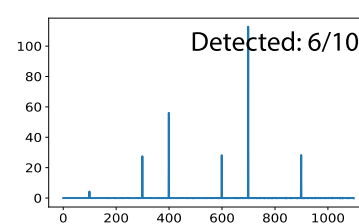
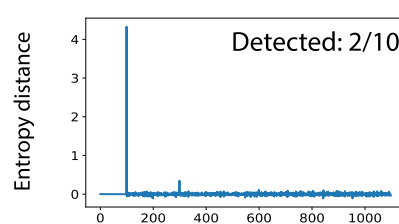
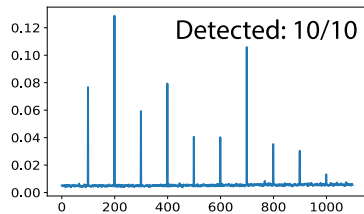
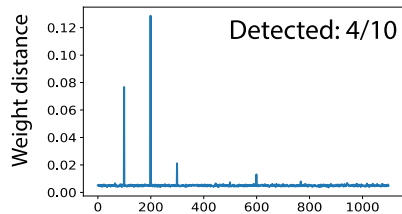
HON identifying more types of anomalies than FON

First-order network

Higher-order network

First-order network

Higher-order network



Random
Add 1st order
Change 1st order
Add 2nd order
Add complementary 2nd order
Change complementary 2nd order
Add 3rd order
Add complementary 3rd order
Change complementary 3rd order
Add complementary mixed orders
Change complementary mixed orders

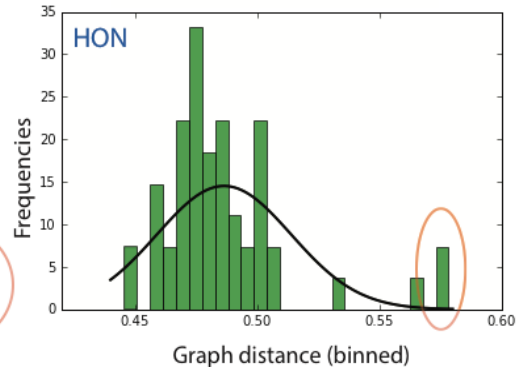
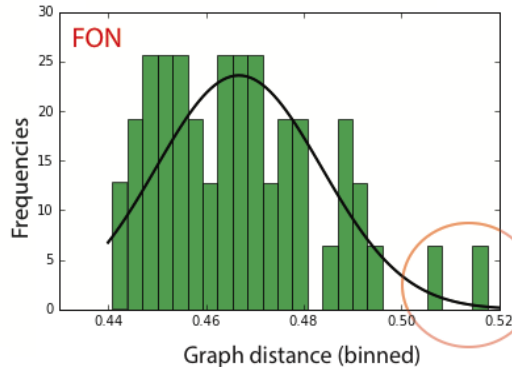
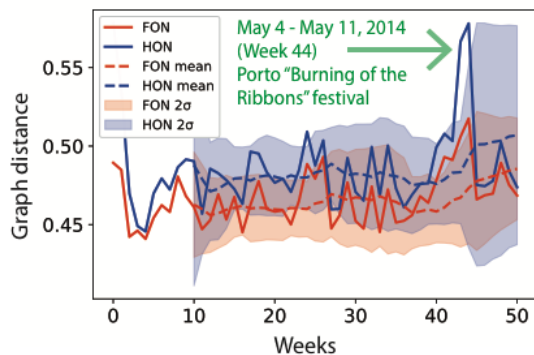
Random
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Change complementary 2nd order
Add 3rd order
Add complementary 3rd order
Change complementary 3rd order
Add complementary mixed orders
Change complementary mixed orders

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Add 1st order
Change 1st order
Add 2nd order
Add complementary 2nd order
Change complementary 2nd order
Add 3rd order
Add complementary 3rd order
Change complementary 3rd order
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Change complementary 3rd order
Add complementary mixed orders
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Real-world taxi data of Porto

- One year of all the 442 GPS trajectories from taxis in Porto, Portugal.
- Construct the FON and HON traffic networks for each week
- Compute the graph distances for neighboring time windows

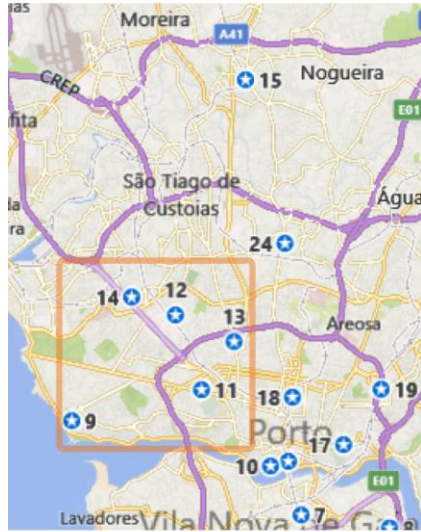


Anomalous traffic pattern more pronounced on HON

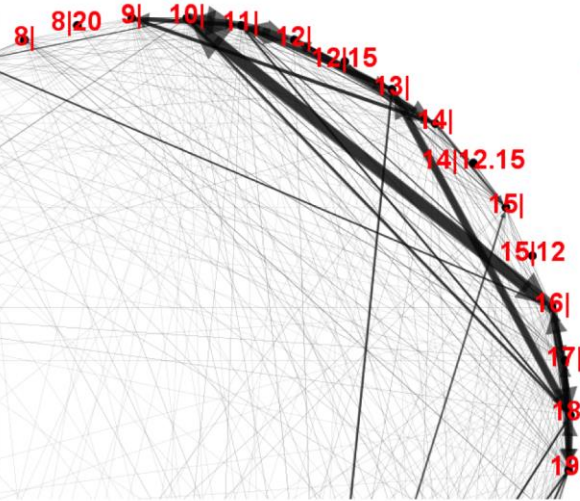
Network differences

HON highlighting differences in Location 9-14
Which are the main venues for the event

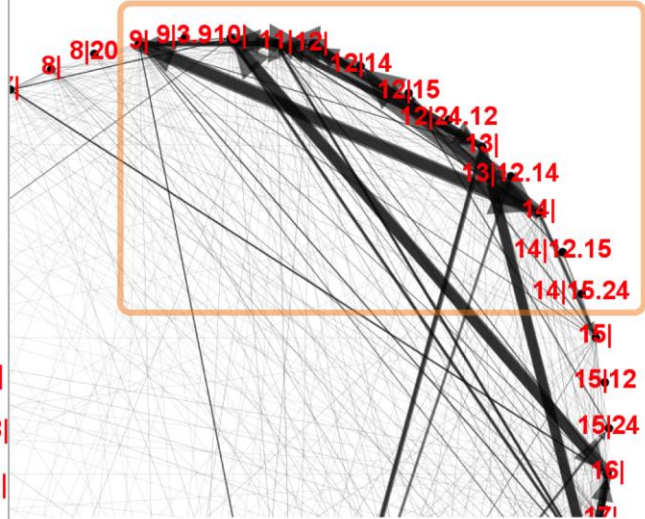
Police stations at Porto



Week 43

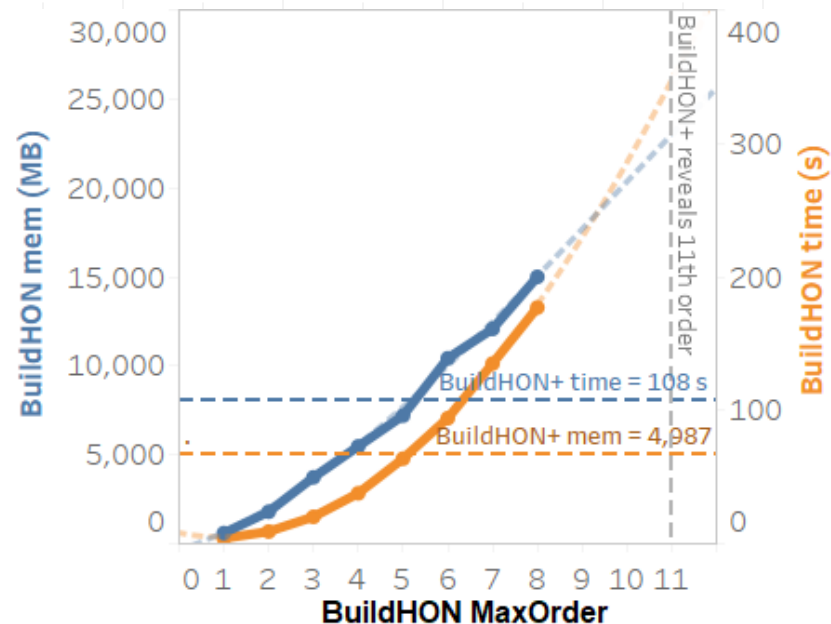


Week 44



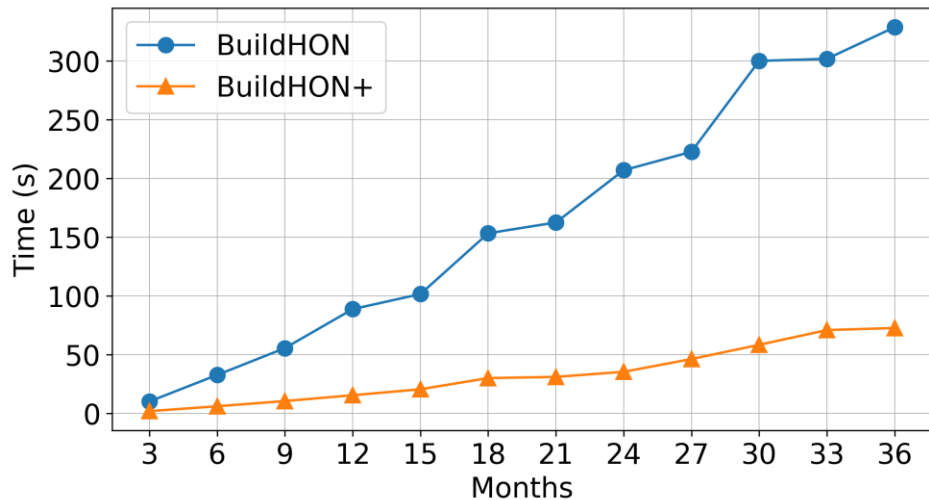
Performance improvement:

- **Data:** The shipping trajectories data with 3,415,577 voyages made by 65,591 ships, shown to have more than fifth order of dependencies.
- **BuildHON** would need 3x time and 5x memory than **BuildHON+** to achieve the same results

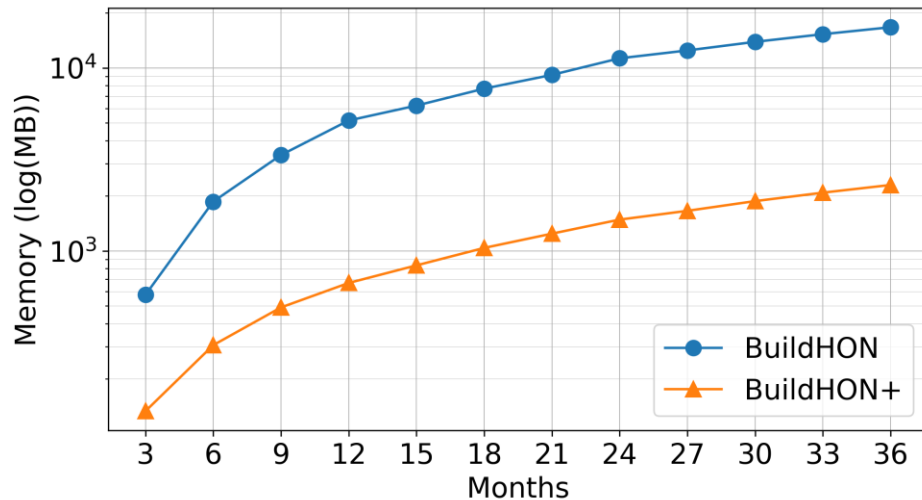


Performance improvement:

BuildHON+ showing consistent advantage with various sized data



(a)



(b)



Summary

- There are anomalies that are only discoverable through **higher-order patterns**
- The higher-order network (HON) representation can help reveal such anomalies from sequential data
- BuildHON+ is a scalable HON construction algorithm
- HON-based dynamic network anomaly detection method applies to a wide variety of contexts
- More info: www.HigherOrderNetwork.com



Thanks!

