

A DISSERTATION

REPRESENTING BIG DATA AS NETWORKS: NEW METHODS AND INSIGHTS

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Tijana Milenkovic

Zoltan Toroczkai

Examination committee

Prof. Nitesh Chawla, *chair*



Prof. David Lodge



Prof. Tijana Milenkovic



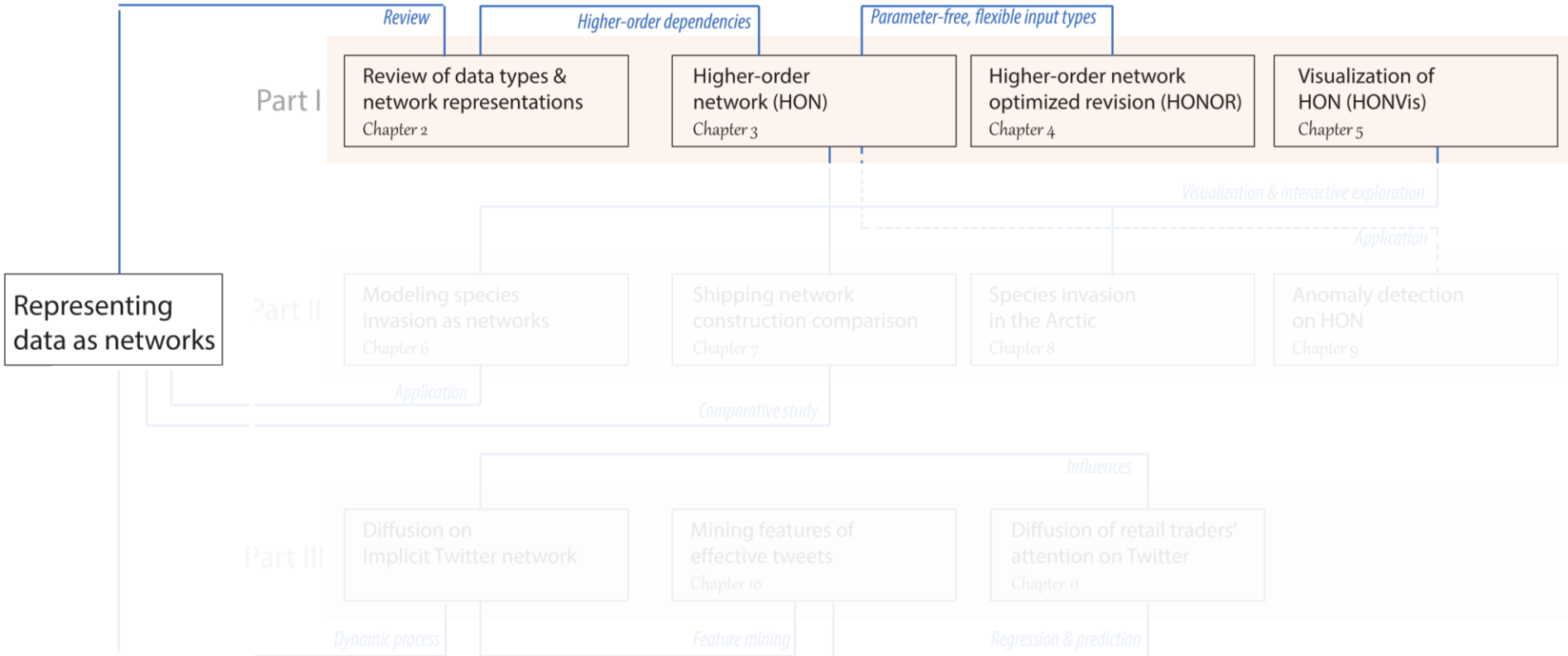
Prof. Zoltan Torotzkai



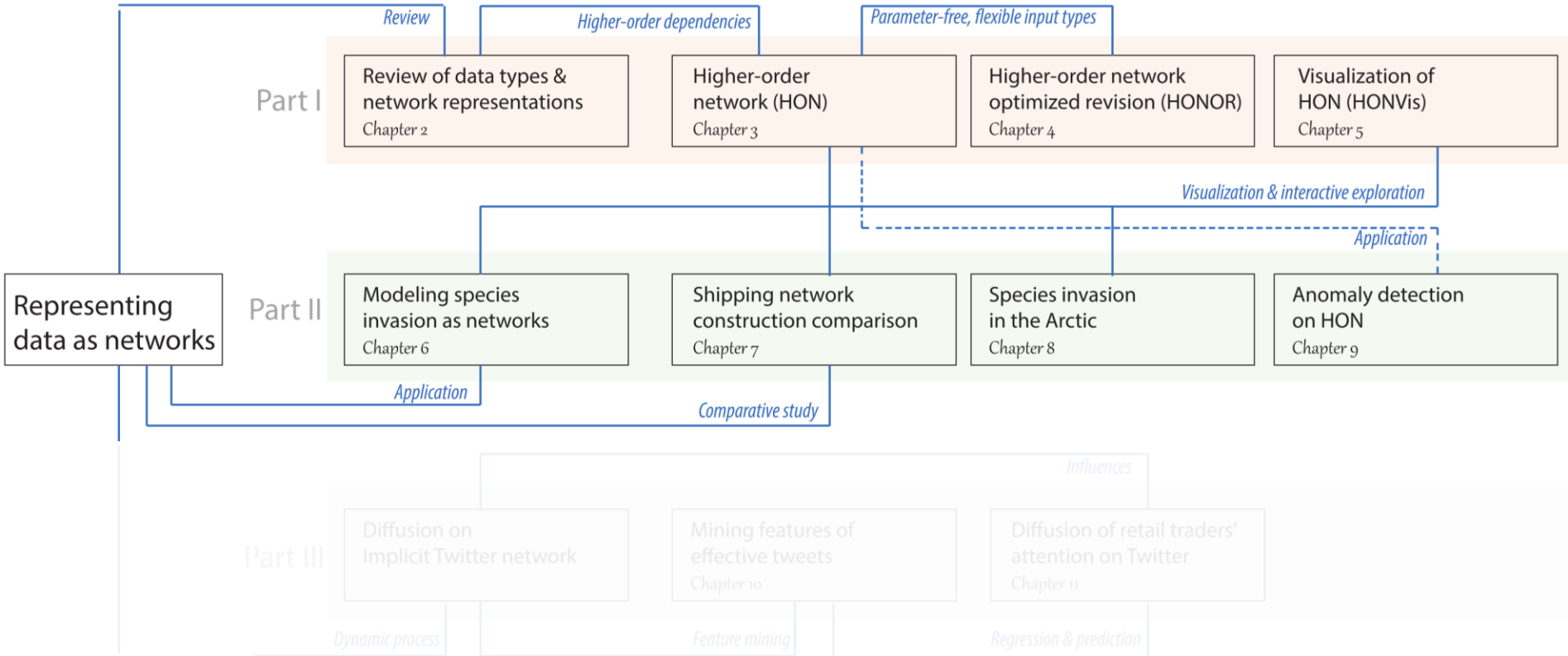
Overview

Representing
data as networks

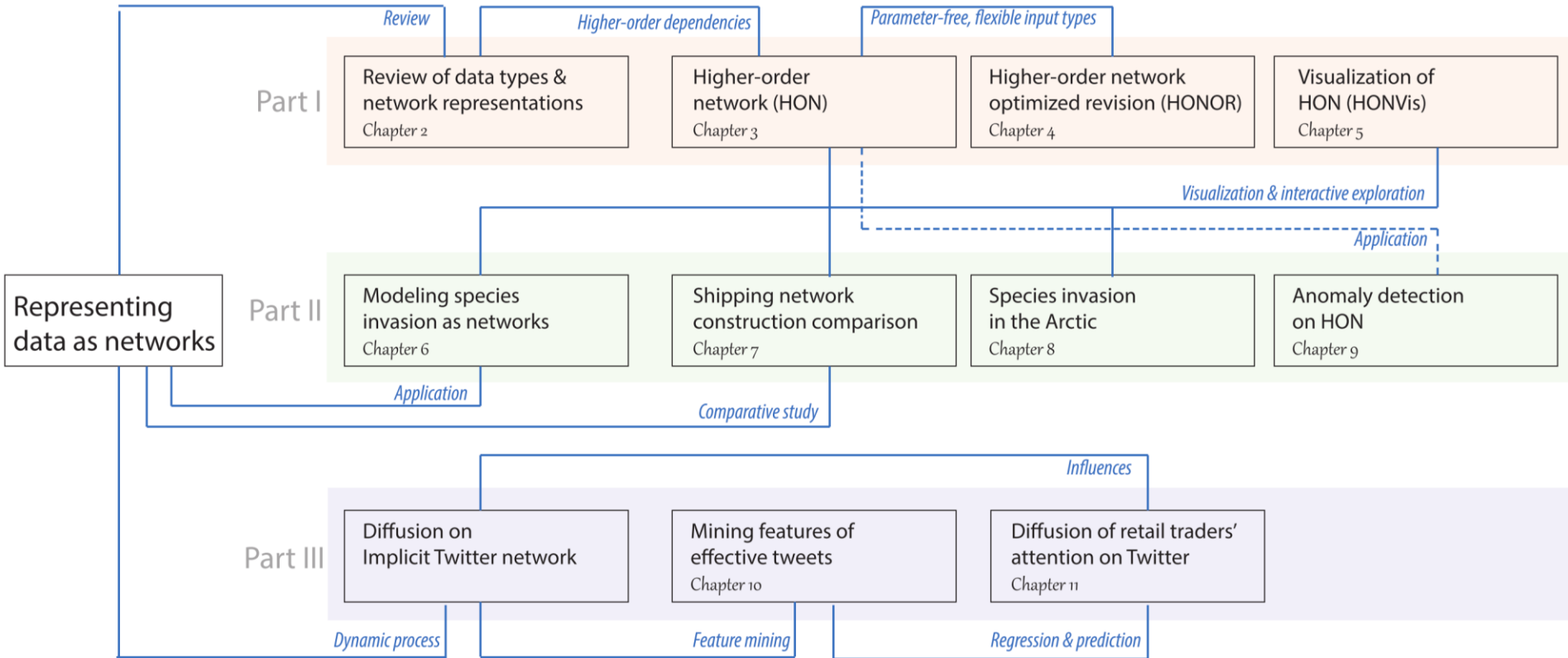
Overview



Overview

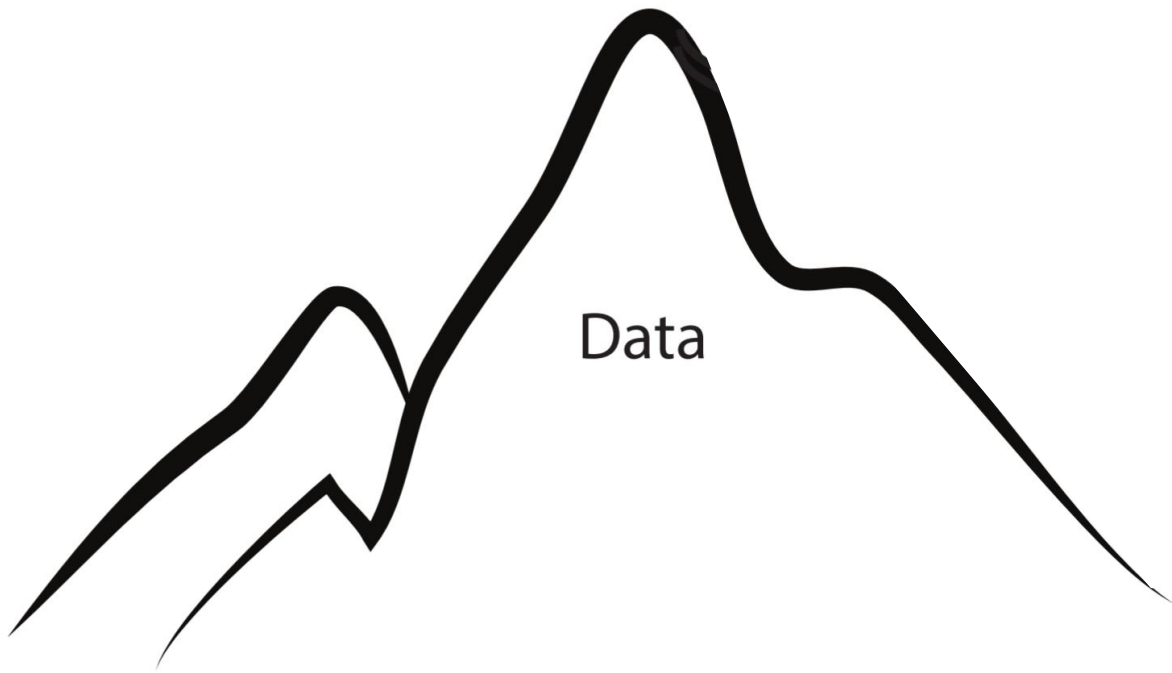


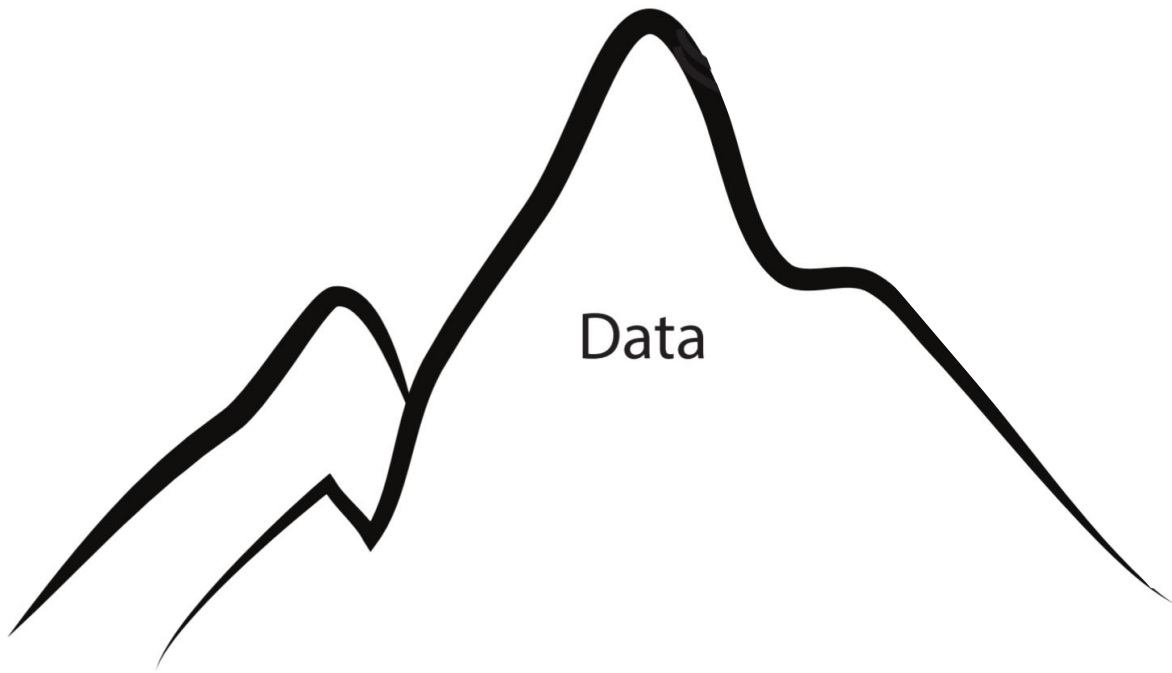
Overview



Part I

Methods to represent data as networks





Pairwise

- a - b
- a - c
- a - d
- b - c

Weighted pairwise

- a - b : 5
- a - c : 3
- a - d : 1
- b - c : 2

Directed pairwise

- a -> b
- a -> c
- a -> d
- b -> c

Temporal pairwise

- a - b : 1, 3
- a - c : 2
- a - d : 2, 3
- b - c : 1, 4

Matrix

a	b	c
0	3	5
b	3	0
c	5	1

Tensor

	T=1:	T=2:
0	3	5
3	0	1
5	1	0

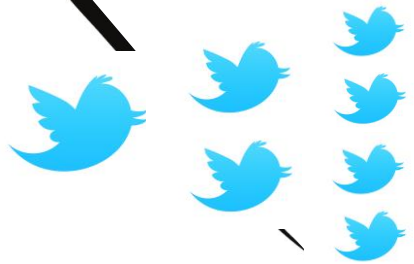
Transaction 3	 
Transaction 4	 
Transaction 5	   

Group
 abc
 ac
 bcd



Sequential
 abab
 acac
 dacdac

Data



Diffusion
 a → b → c
 a → d
 b → c
 b → d



Time series
 1 2 1 2
 1 3 1 3
 4 1 3 4 1 3

Data

Pairwise
a-b
a-c
a-d
b-c

Weighted pairwise
a-b:5
a-c:3
a-d:1
b-c:2

Directed pairwise
a->b
a->c
a->d
b->c

Temporal pairwise
a-b:1,3
a-c:2
a-d:2,3
b-c:1,4

Matrix
abc
a 0 3 5
b 3 0 1
c 5 1 0

Tensor
T=1: T=2:
0 3 5 0 1 5
3 0 1 3 0 4
5 1 0 5 4 0

Group
abc
ac
bcd

Sequential
abab
acac
dacdac

Diffusion
a->b-c
a->d
b->c
b->d

Time series
1 2 1 2
1 3 1 3
4 1 3 4 1 3



Data

Network

Pairwise
a-b
a-c
a-d
b-c

Weighted pairwise
a-b:5
a-c:3
a-d:1
b-c:2

Directed pairwise
a->b
a->c
a->d
b->c


Temporal pairwise
a-b:1,3
a-c:2
a-d:2,3
b-c:1,4

Matrix
a b c
a 0 3 5
b 3 0 1
c 5 1 0

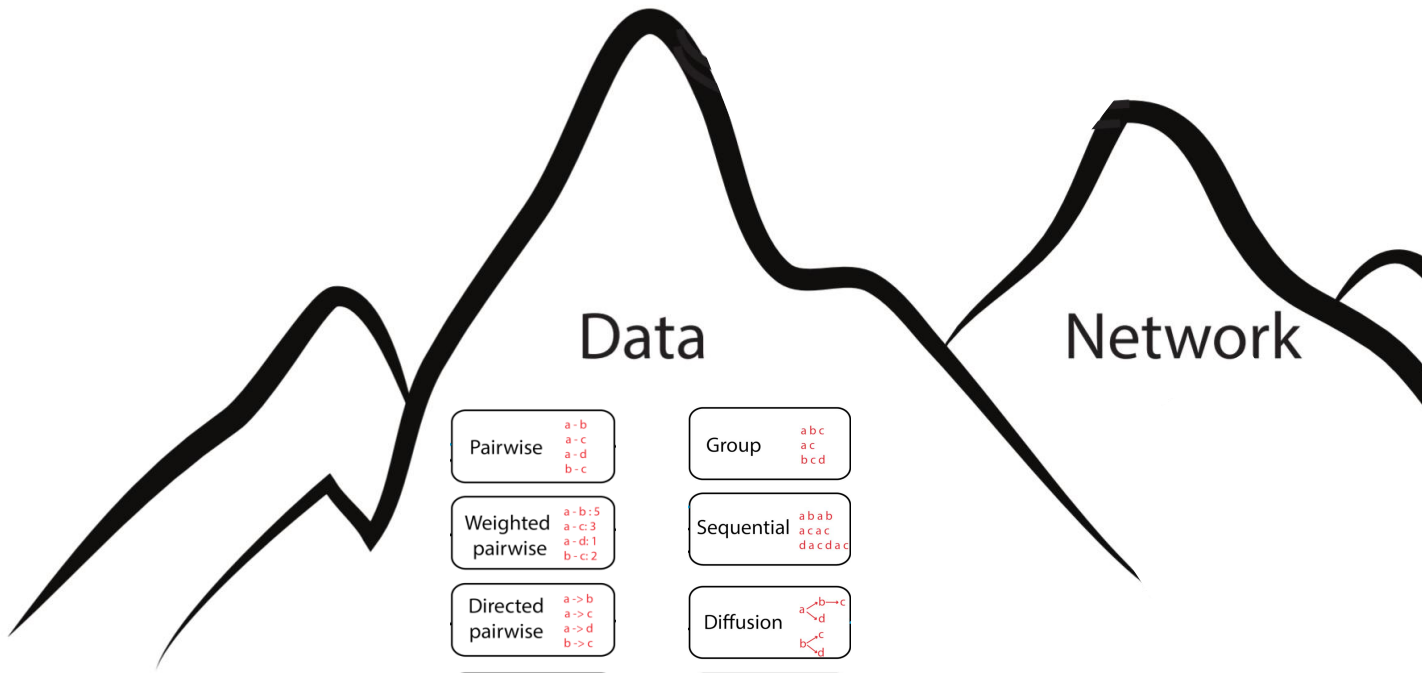
Tensor
T=1: T=2:
0 3 5 0 1 5
3 0 1 1 0 4
5 1 0 5 4 0

Group
a b c
a c
b c d

Sequential
a b a b
a c a c
d a c d a c

Diffusion


Time series
1 2 1 2
1 3 1 3
4 1 3 4 1 3



Data

Network

Pairwise

- a-b
- a-c
- a-d
- b-c

Weighted pairwise

- a-b:5
- a-c:3
- a-d:1
- b-c:2

Directed pairwise

- a->b
- a->c
- a->d
- b->c

Temporal pairwise

- a-b:1,3
- a-c:2
- a-d:2,3
- b-c:1,4

Matrix

a	b	c
0	3	5
b	3	0
c	5	1

Tensor

T=1:	T=2:
0	3
5	1
3	0
1	4
5	1
1	0
4	3

Group

- abc
- ac
- bcd

Sequential

- abab
- acac
- dacdac

Diffusion

Time series

1	2	1	2
1	3	1	3
4	1	3	4
1	3	4	1

Simple

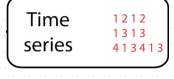
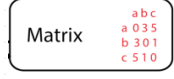
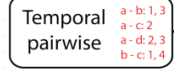
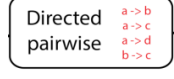
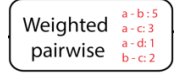
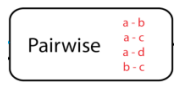
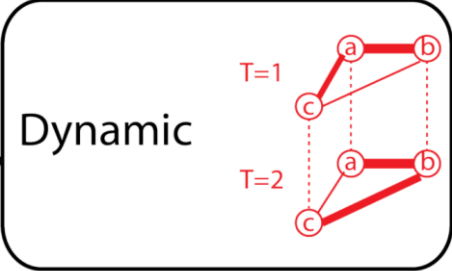
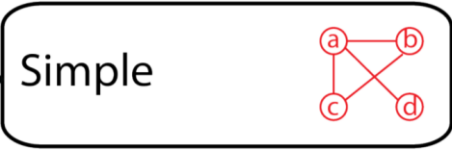
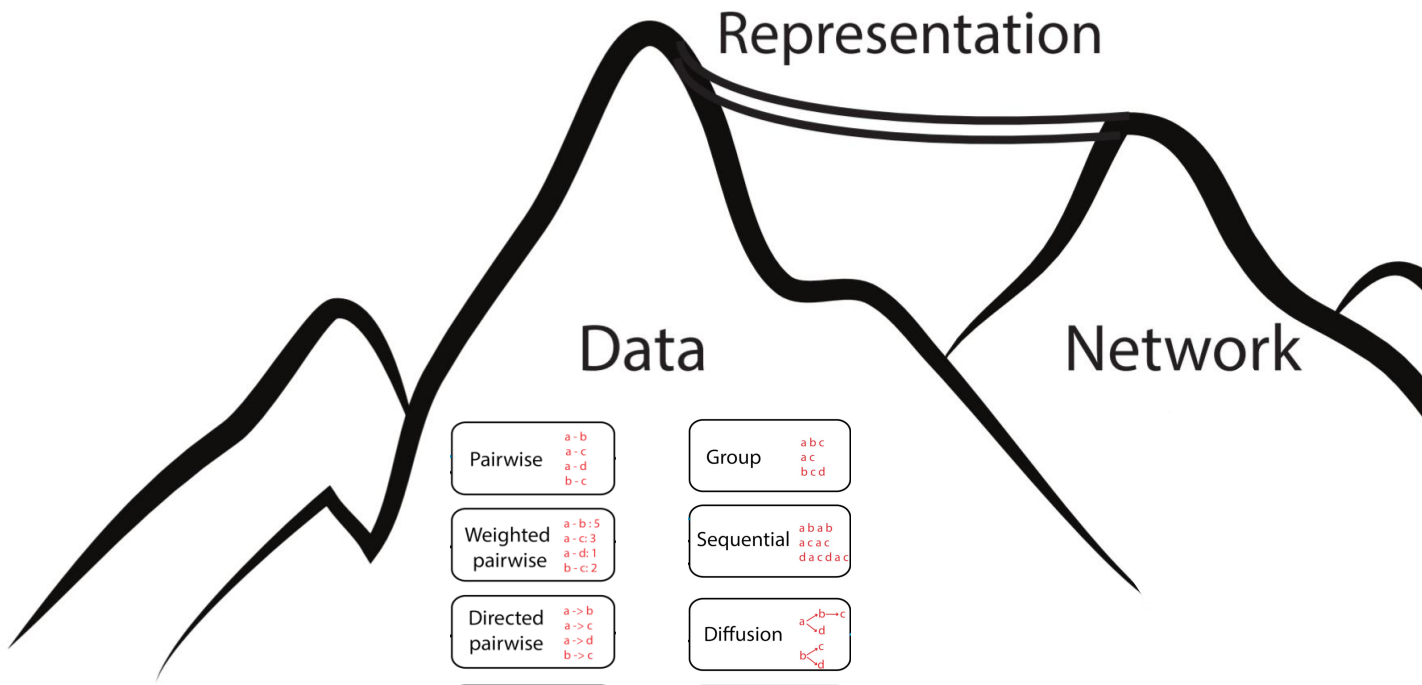
Weighted

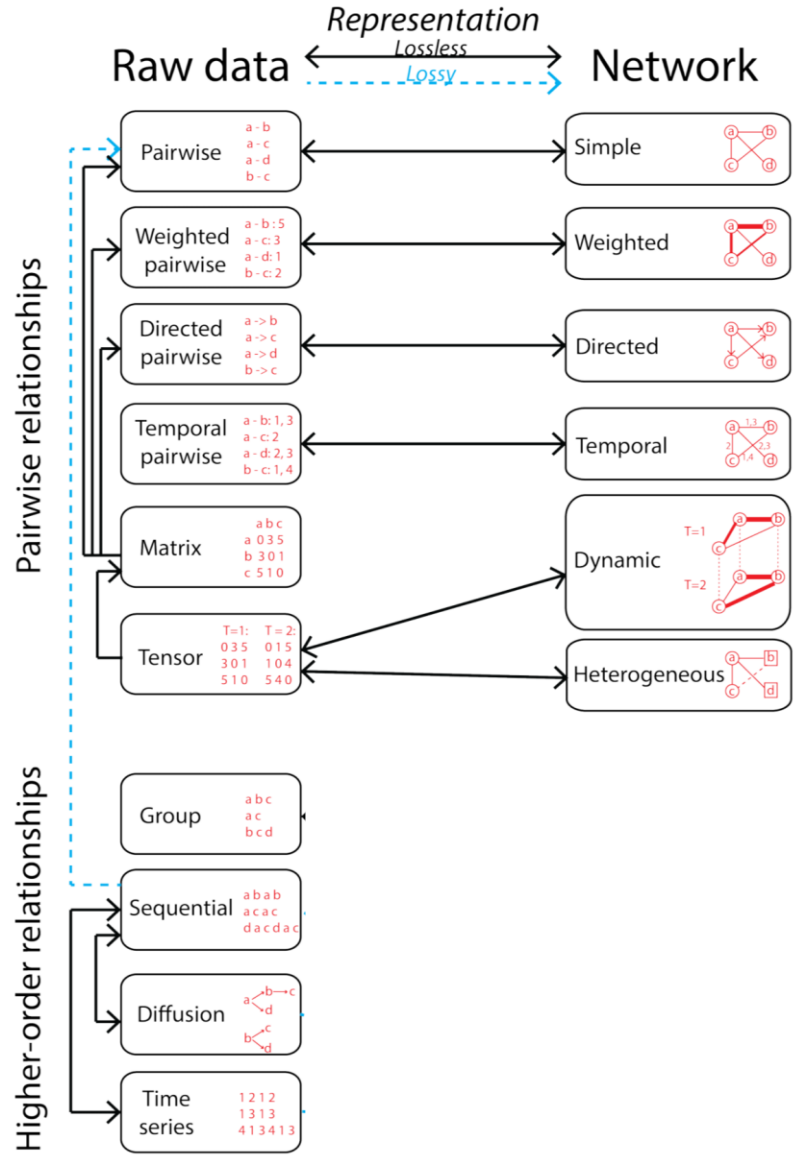
Directed

Temporal

Dynamic

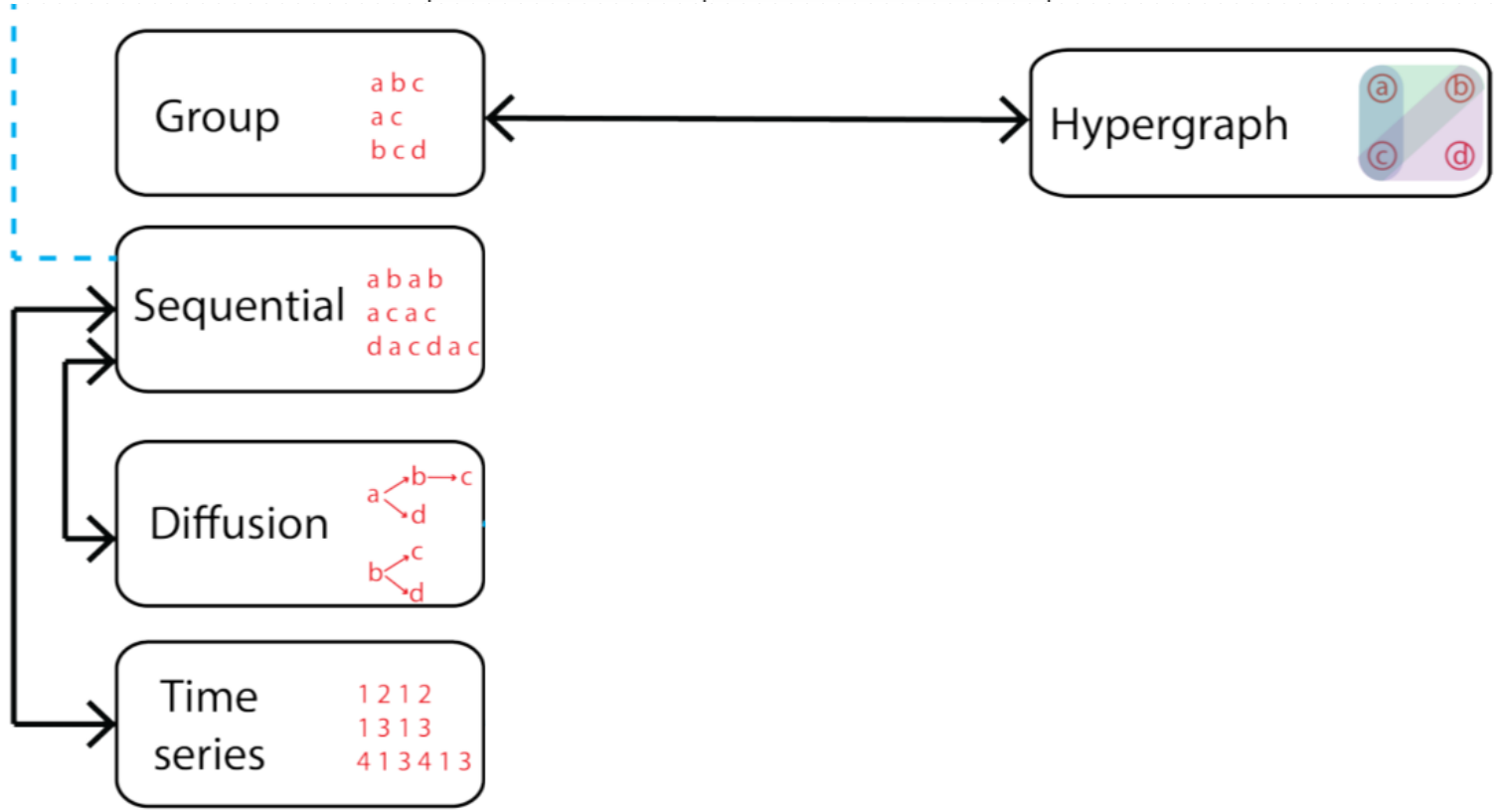
Heterogeneous



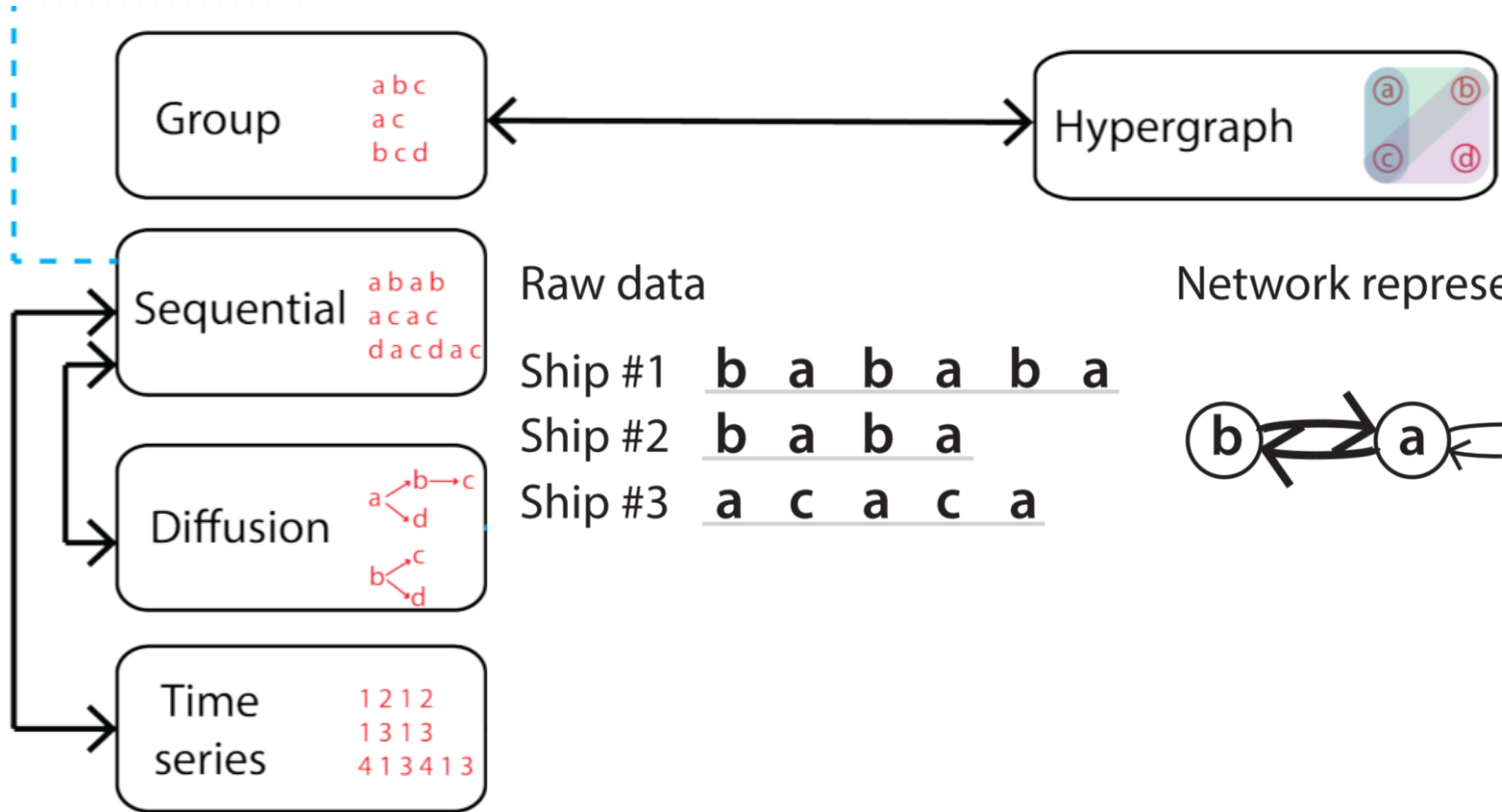


Transaction 3	 
Transaction 4	 
Transaction 5	   

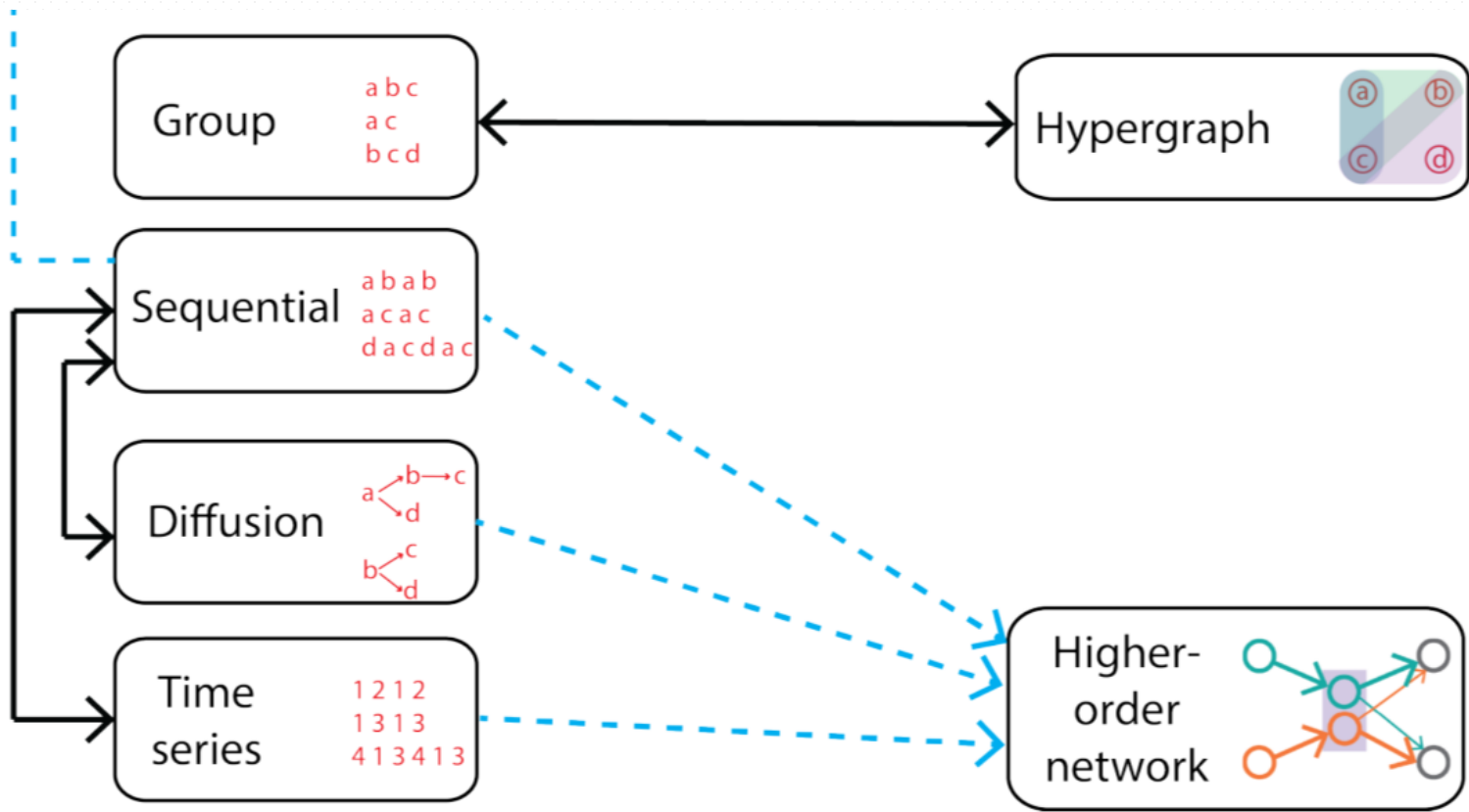
Higher-order relationships



Higher-order relationships



Higher-order relationships



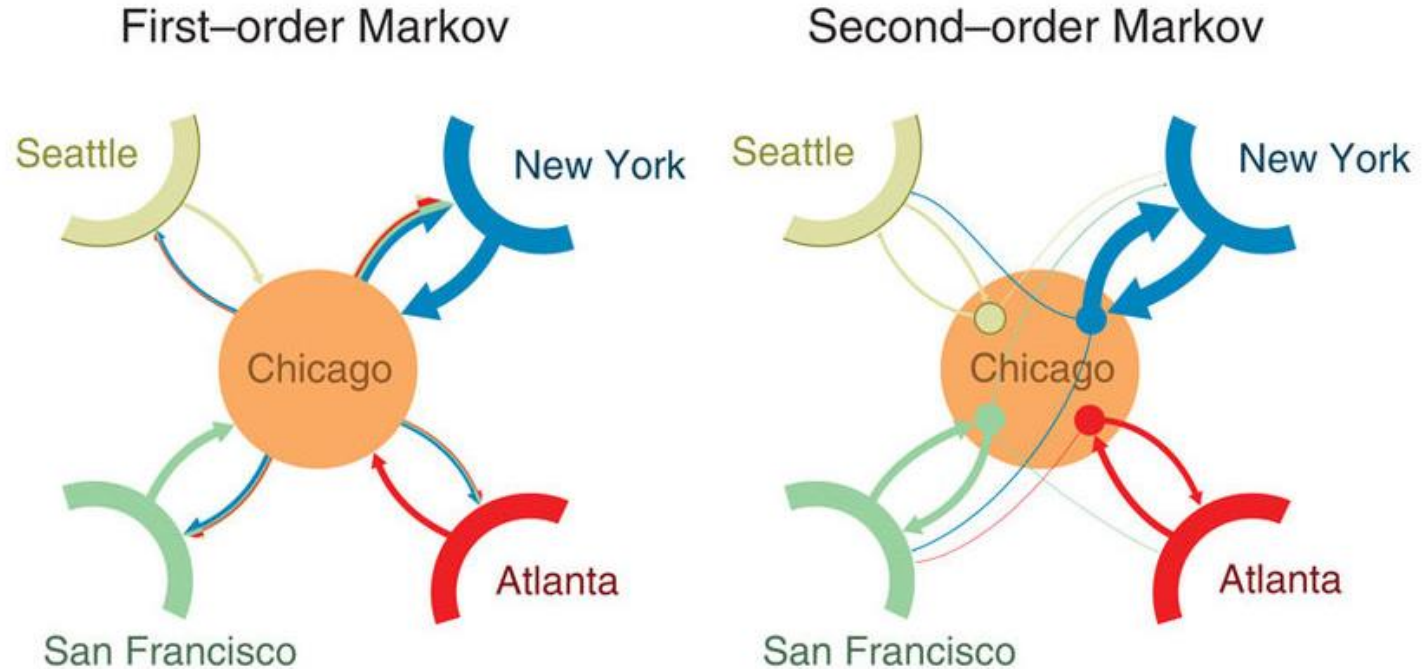
Higher-order network

Representing higher-order dependencies in networks

Higher-order network



Fixed-order network



Variable orders in HON

Fixed-order

Variable-order

Assuming a fixed order beyond the second order becomes impractical because *“higher-order Markov models are more complex”* due to combinatorial explosion

--- Rosvall et al. (Nature Comm. 2014)

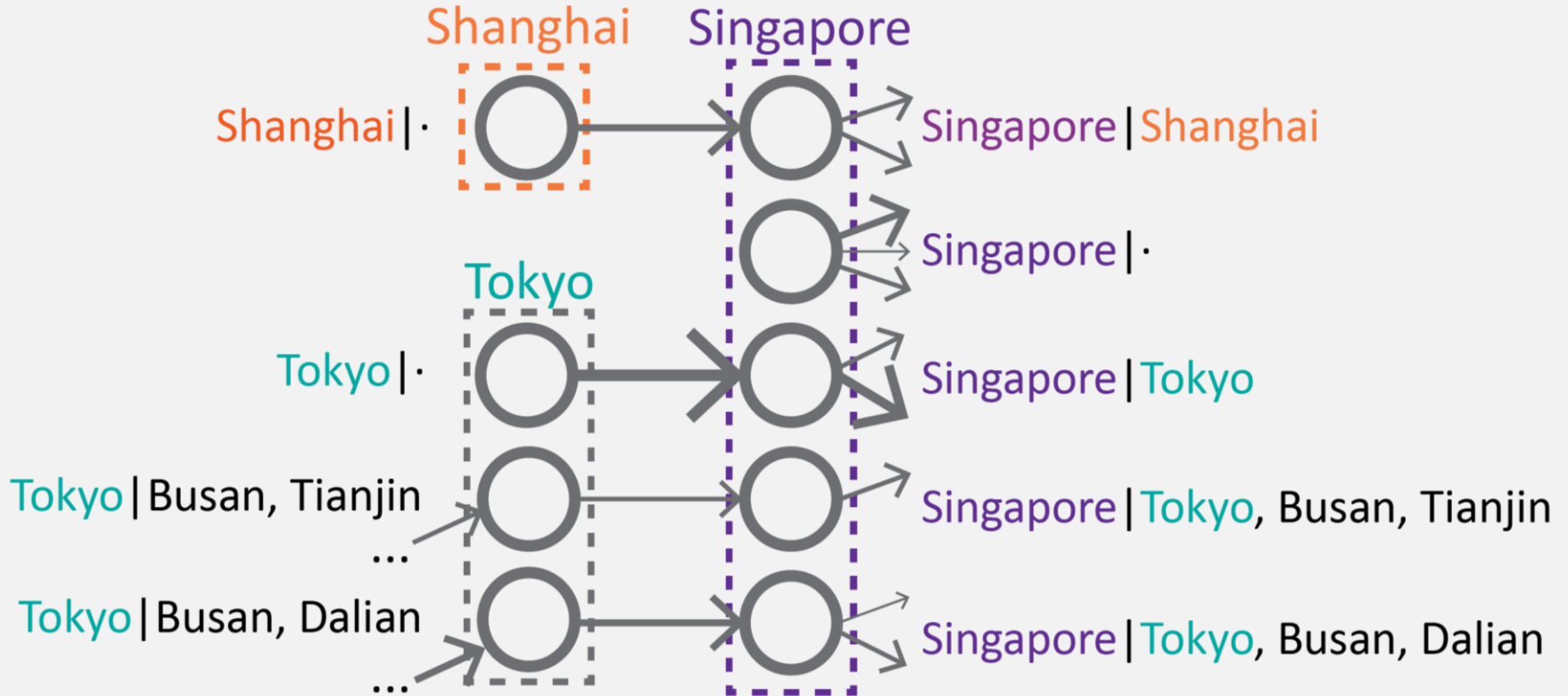
Relatively easier to build

Accurate: use higher-order when necessary

Scalable: use lower-order when sufficient

Variable orders in HON

Variable orders of dependencies in HON

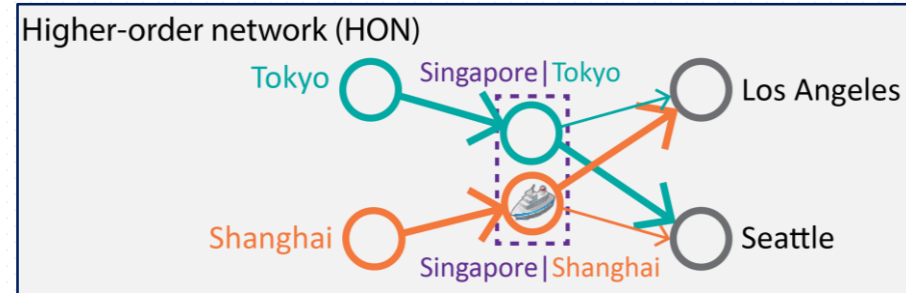
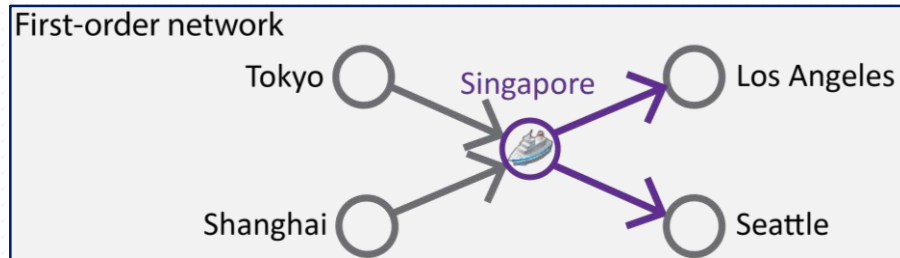


Scalable for big data

Compatible with existing tools

Conventionally: every node represents a single entity (location, state, etc.)

Now: break down nodes into higher-order nodes that carry different dependency relationships



$$P(X_{t+1} = i_{t+1} | X_t = i_t) = \frac{W(i_t \rightarrow i_{t+1})}{\sum_j W(i_t \rightarrow j)}$$

$$P(X_{t+1} = j | X_t = (i | h)) = \frac{W(i | h \rightarrow j)}{\sum_k W(i | h \rightarrow k)}$$

Only change the node labeling

Takeaways

Higher-order network is:

More **accurate** in capturing dynamics in raw data.

More **scalable** than fixed-order networks.

Compatible with existing network algorithms.

Limitations:

Multiple parameters: maximum order & minimum support.

Costly to build for very high orders.

Higher-order network optimized revision

Parameter-free, scalable for arbitrarily high order

HON construction workflow

Raw data

Rule
extraction

Network
wiring

HON

- Sequential data

- Which nodes to split into higher-order nodes, and how high the orders are

- Connect nodes representing different orders

- Use HON like the conventional network for analyses

HON

Raw data

A B C A B C A C B

HON

Raw data

A B C A B C A C B



Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1

Build all 2nd-order

A|C -> B: 1

A|C -> C: 1

B|A -> C: 2

C|B -> A: 2

C|A -> B: 1

Build all 3rd-order

A|C.B -> B: 1

A|C.B -> C: 1

B|A.C -> C: 1

C|B.A -> A: 2

C|A.C -> B: 1

HON

Raw data

A B C A B C A C B



Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1

Build all 2nd-order

A|C -> B: 1

A|C -> C: 1

B|A -> C: 2

C|B -> A: 2

C|A -> B: 1

Build all 3rd-order

A|C.B -> B: 1

A|C.B -> C: 1

B|A.C -> C: 1

C|B.A -> A: 2

C|A.C -> B: 1



Build distribution

Build all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33



Build all 2nd-order

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33



Build all 3rd-order

A|C.B -> B: 0.5

A|C.B -> C: 0.5

B|A.C -> C: 1

C|B.A -> A: 0.67

C|A.C -> B: 0.33

HON

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2
A -> C: 1
B -> C: 2
C -> A: 2
C -> B: 1

Build all 2nd-order

A|C -> B: 1
A|C -> C: 1
B|A -> C: 2
C|B -> A: 2
C|A -> B: 1

Build all 3rd-order

A|C.B -> B: 1
A|C.B -> C: 1
B|A.C -> C: 1
C|B.A -> A: 2
C|A.C -> B: 1

Build distribution

Build all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

Build all 2nd-order

A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

Build all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

Grow all 2nd-order

A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

Grow all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33



HON

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

Build all 2nd-order

A|C -> B: 1

A|C -> C: 1

B|A -> C: 2

C|B -> A: 2

Build all 3rd-order

A|C.B -> B: 1

A|C.B -> C: 1

B|A.C -> C: 1

C|B.A -> A: 2

$$D_{KL}(ExtDistr || Distr) \leq \frac{NewOrder}{\log_2(1 + \sum C[ExtSource][*])}$$

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

A|C.B -> C: 0.5

B|A.C -> C: 1

C|B.A -> A: 0.67

C|A.C -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

Grow all 2nd-order

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

Grow all 3rd-order

A|C.B -> B: 0.5

A|C.B -> C: 0.5

B|A.C -> C: 1

C|B.A -> A: 0.67

C|A.C -> B: 0.33

HON

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2
A -> C: 1
B -> C: 2
C -> A: 2
C -> B: 1

Build all 2nd-order

A|C -> B: 1
A|C -> C: 1
B|A -> C: 2
C|B -> A: 2
C|A -> B: 1

Build all 3rd-order

A|C.B -> B: 1
A|C.B -> C: 1
B|A.C -> C: 1
C|B.A -> A: 2
C|A.C -> B: 1

Build distribution

Build all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

5th order

Build all 2nd-order

A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

4th order

3rd order

2nd order

1st order

Build all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

Grow all 2nd-order

A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

Grow all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

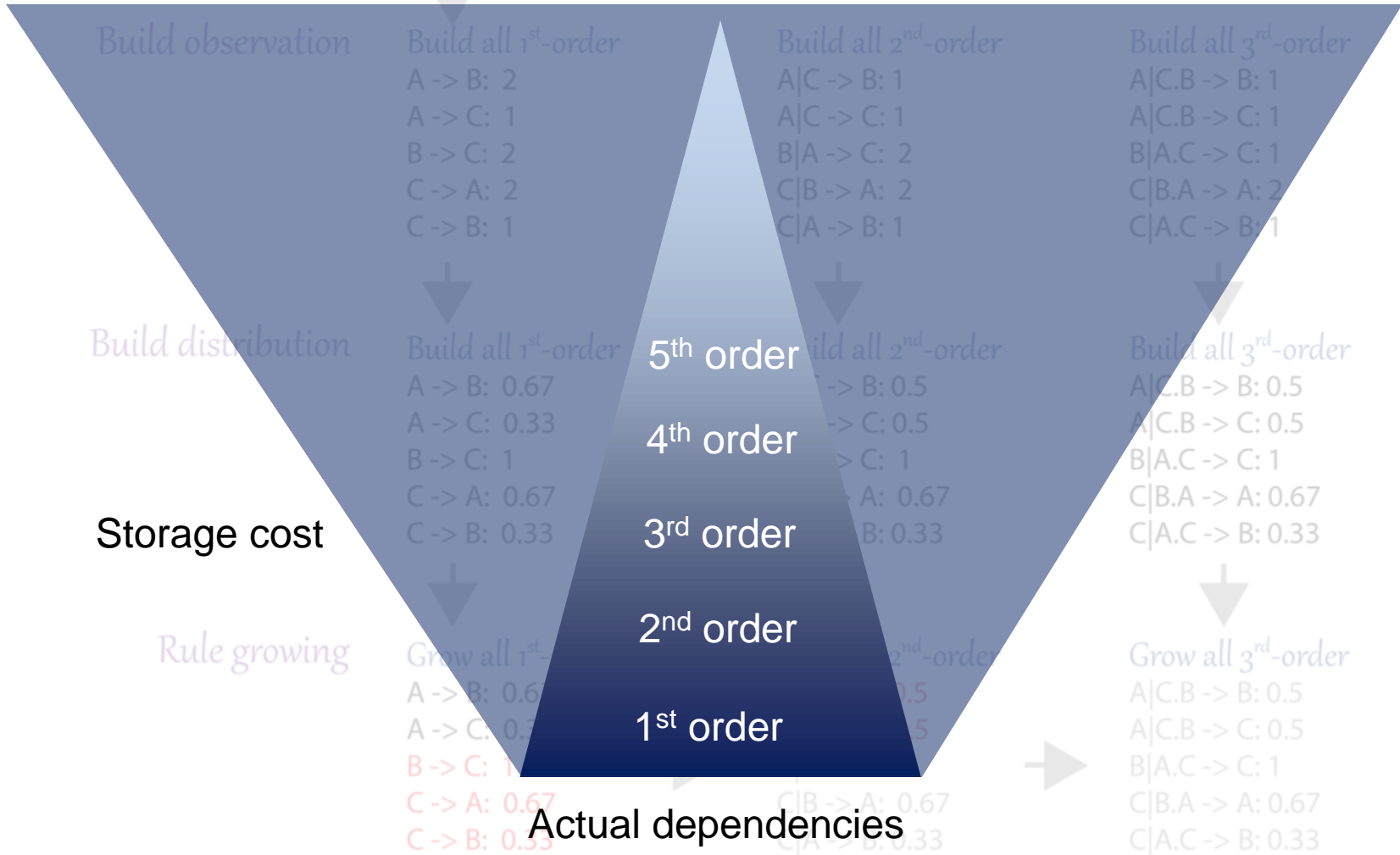
Actual dependencies

HON

Raw data

A B C A B C A C B

$\Theta(\text{Order}^2 \times \text{RawDataSize})$



HON

Raw data

A B C A B C A C B

$\Theta(\text{Order} \times \text{RawDataSize})$

Build observation

Build all 1st-order

A -> B: 2
A -> C: 1
B -> C: 2
C -> A: 2
C -> B: 1

Build all 2nd-order

A|C -> B: 1
A|C -> C: 1
B|A -> C: 2
C|B -> A: 2
C|A -> B: 1

Build all 3rd-order

A|C.B -> B: 1
A|C.B -> C: 1
B|A.C -> C: 1
C|B.A -> A: 2
C|A.C -> B: 1

Build distribution

Build all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

5th order

Build all 2nd-order

A -> B: 0.5
A -> C: 0.5
B -> C: 1
C -> A: 0.67
C -> B: 0.33

4th order

Build all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

Storage cost

3rd order

Rule growing

Grow all 1st-order

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

2nd order

Build all 2nd-order

A -> B: 0.5
A -> C: 0.5
B -> C: 1
C -> A: 0.67
C -> B: 0.33

1st order

Grow all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

Actual dependencies

HON

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2
A -> C: 1
B -> C: 2
C -> A: 2

Build all 2nd-order

A|C -> B: 1
A|C -> C: 1
B|A -> C: 2
C|B -> A: 2

Build all 3rd-order

A|C.B -> B: 1
A|C.B -> C: 1
B|A.C -> C: 1
C|B.A -> A: 2

$$\begin{aligned} \max(D_{KL}(ExtDistr||Distr)) &= \max\left(\sum_{i \in Distr} P_{ExtDistr}(i) \times \log_2 \frac{P_{ExtDistr}(i)}{P_{Distr}(i)}\right) \\ &= 1 \times \log_2 \frac{1}{\min(P_{Distr}(i))} + 0 + 0 + \dots \\ &= -\log_2(\min(P_{Distr}(i))) \end{aligned}$$

A -> B: 0.67
A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33



A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33



A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

HON

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2
A -> C: 1
B -> C: 2
C -> A: 2

Build all 2nd-order

A|C -> B: 1
A|C -> C: 1
B|A -> C: 2
C|B -> A: 2

Build all 3rd-order

A|C.B -> B: 1
A|C.B -> C: 1
B|A.C -> C: 1
C|B.A -> A: 2

$$-\log_2(\min(P_{Distr}(i))) \cong \frac{NewOrder}{\log_2(1 + \sum C[ExtSource][*])}$$

A -> C: 0.33
B -> C: 1
C -> A: 0.67
C -> B: 0.33

A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67
A -> C: 0.33
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C -> A: 0.67
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Grow all 2nd-order

A|C -> B: 0.5
A|C -> C: 0.5
B|A -> C: 1
C|B -> A: 0.67
C|A -> B: 0.33

Grow all 3rd-order

A|C.B -> B: 0.5
A|C.B -> C: 0.5
B|A.C -> C: 1
C|B.A -> A: 0.67
C|A.C -> B: 0.33

HONOR

Raw data

A B C A B C A C B

HONOR

Raw data

A B C A B C A C B



Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1

HONOR

Raw data

A B C A B C A C B



Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1



Build distribution

Build all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

HONOR

Raw data

A B C A B C A C B



Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1



Build distribution

Build all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33



Rule growing

Grow all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33



HONOR

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1

Build 2nd-order on demand

A|C -> B: 1

A|C -> C: 1

B|A -> C: 2

C|B -> A: 2

C|A -> B: 1

Build distribution

Build all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

Build 2nd-order on demand

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

Grow 2nd-order on demand

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

HONOR

Raw data

A B C A B C A C B

Build observation

Build all 1st-order

A -> B: 2

A -> C: 1

B -> C: 2

C -> A: 2

C -> B: 1

Build 2nd-order on demand

A|C -> B: 1

A|C -> C: 1

B|A -> C: 2

C|B -> A: 2

C|A -> B: 1

Build distribution

Build all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

Build 2nd-order on demand

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

Rule growing

Grow all 1st-order

A -> B: 0.67

A -> C: 0.33

B -> C: 1

C -> A: 0.67

C -> B: 0.33

Grow 2nd-order on demand

A|C -> B: 0.5

A|C -> C: 0.5

B|A -> C: 1

C|B -> A: 0.67

C|A -> B: 0.33

Max divergence < threshold

Stop rule growing

Takeaways

HONOR is:

Parameter-free version of HON.

More **scalable** for big data

Supports arbitrarily high order.

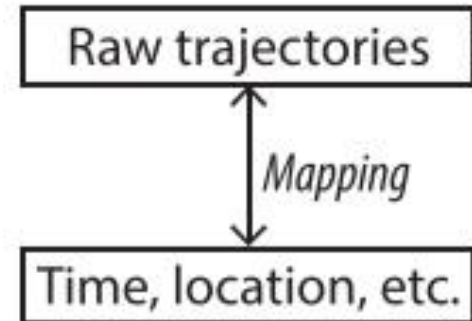
Lazy evaluation reduces actual search space.

HONVis

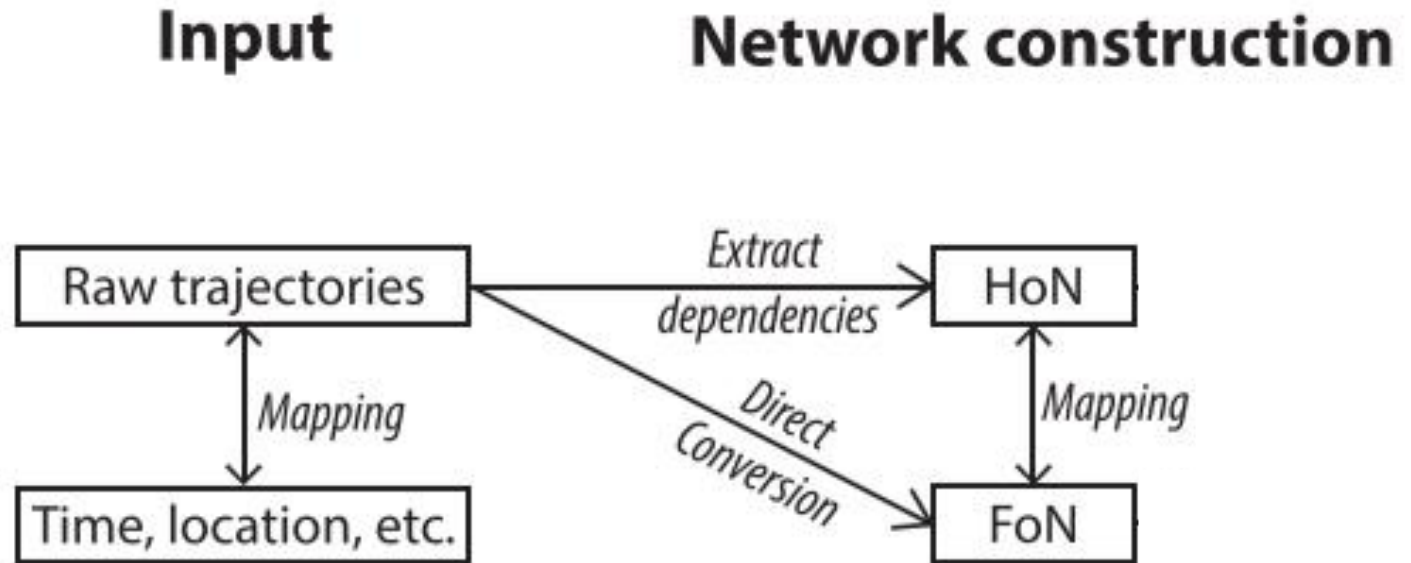
Visualization & interactive exploration software

HoNVis framework

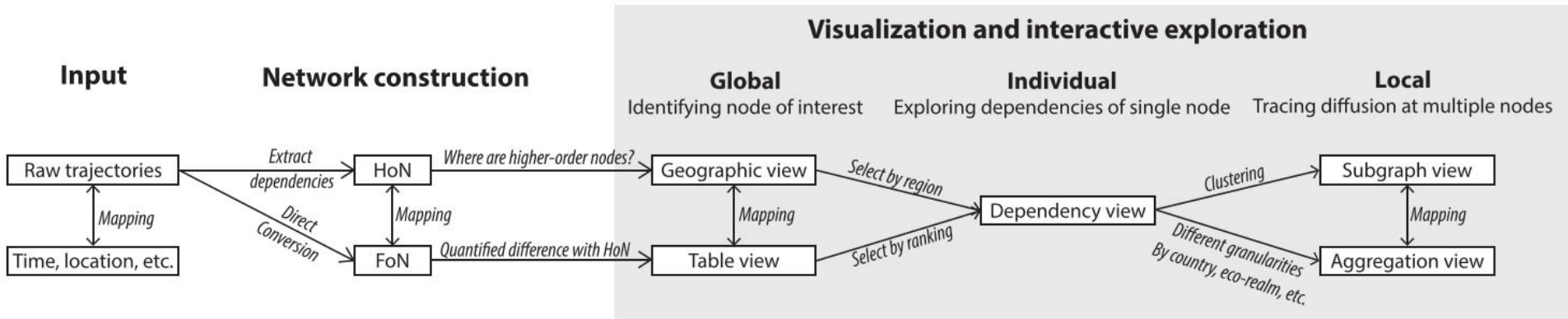
Input



HoNVis framework



HoNVis framework



HoNVis interface

Geographic View
Node Weight
 Prefer High Weight
Edge Straightening

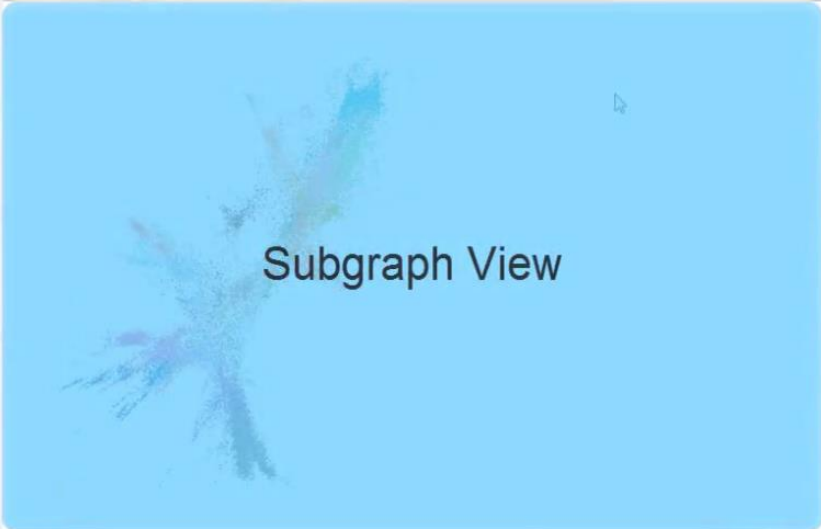
Dependency View
Destination Order
Minimum Probability
Minimum Weight
Font Size
Label Margin



Parameter Control Panel

Subgraph View
 Trace Forward

Aggregation View
 Hide View
 Exact Group
 Use Subgraph
Node Group
Node Weight
 Display In-Group Edges
 Display Between-Group Edges
Edge Opacity
Edge Straightening



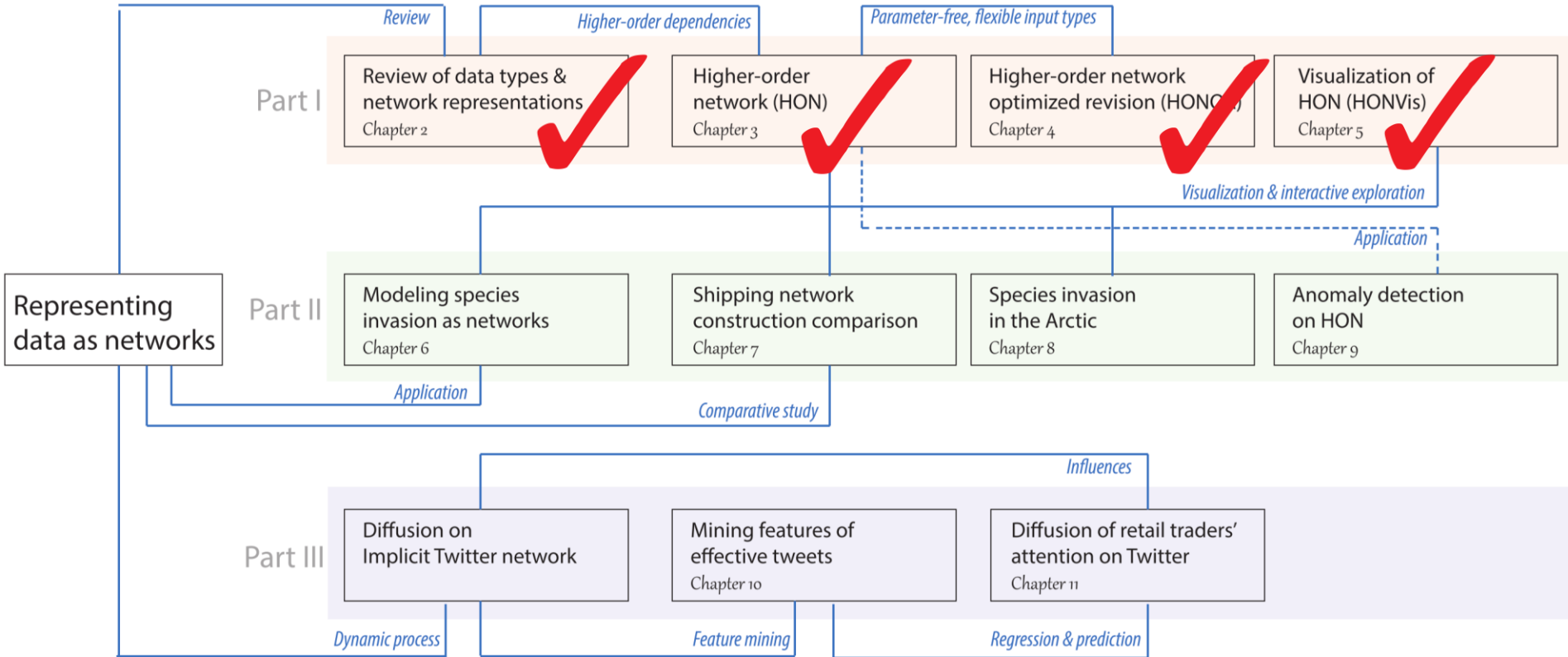
Takeaways

HONVis is:

The **first** visualization software for HON.

Facilitates interactive explorations.

Overview



Part II

Insights in real-world applications

Species invasion network

Non-indigenous species risk assessment &
prediction framework (NIS-RAPS)

Invasive species



**\$120 billion / year
damage & control costs**

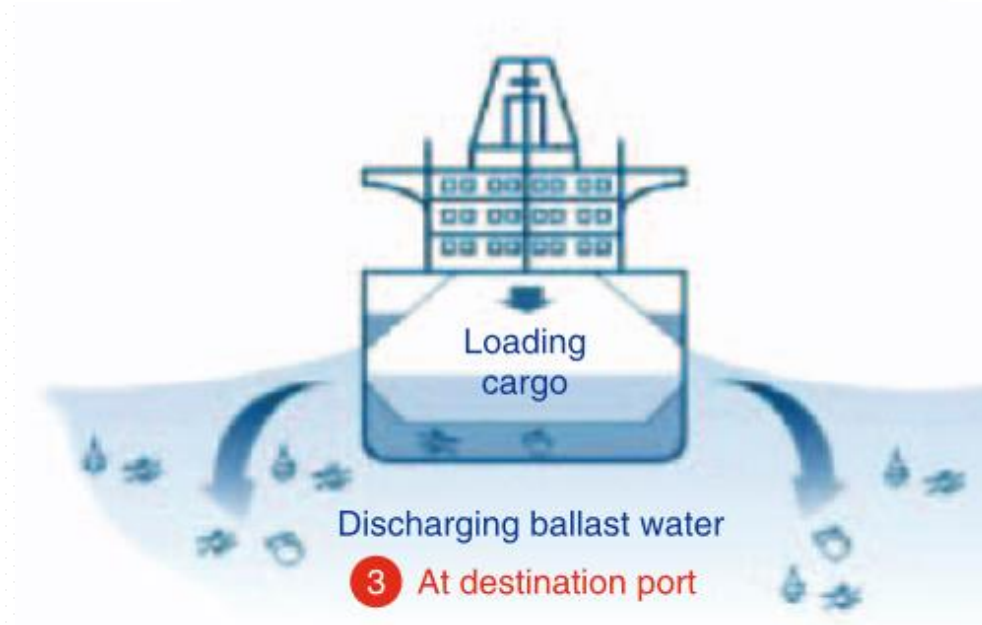
Zebra mussels @ Great Lakes
Clogging water pipes, attach to boats







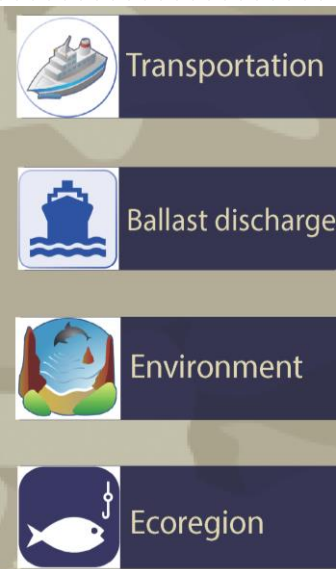
Ship-borne species invasion



Ship-borne species invasion

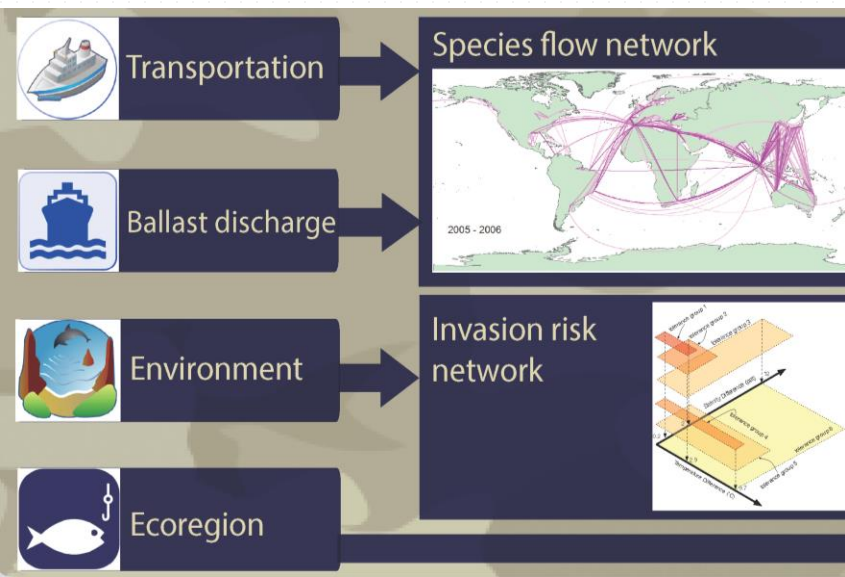


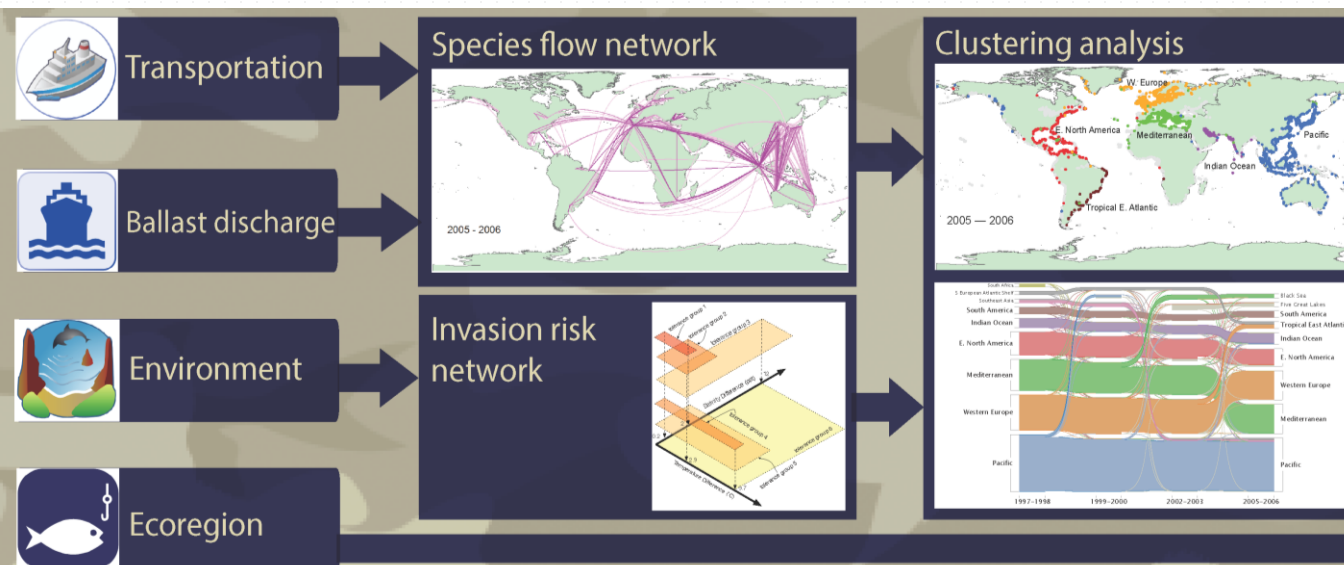
-  Transportation
-  Ballast discharge
-  Environment
-  Ecoregion



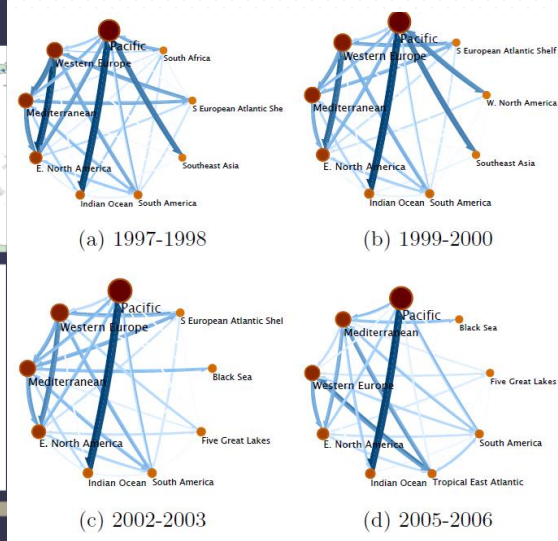
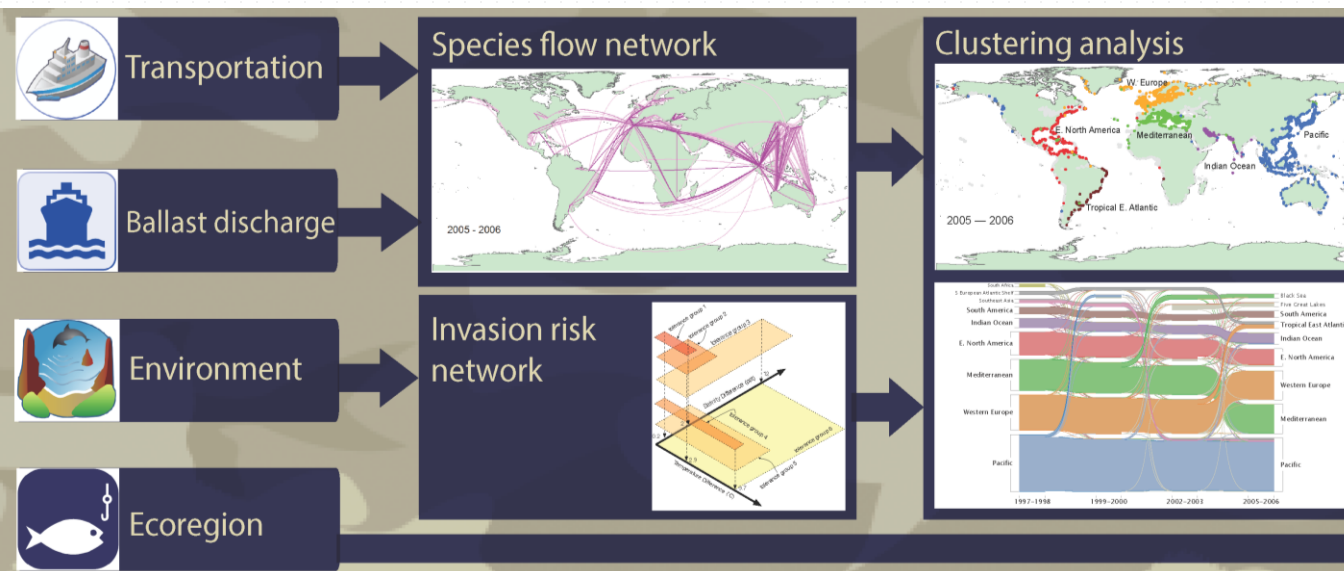
Probability of vessel v introducing species from port i to port j

$$p_{ij}^{(v)} = \underbrace{\rho_{ij}^{(v)}}_{\text{Mgmt efficacy}} \underbrace{\left(1 - e^{-\lambda D_{ij}^{(v)}}\right)}_{\text{Ballast discharge}} \underbrace{e^{-\mu \Delta t_{ij}^{(v)}}}_{\text{Mortality}}$$





* Clustering uses MapEquation by Rosvall et al. (2008)



* Clustering uses MapEquation by Rosvall et al. (2008)



Transportation



Ballast discharge

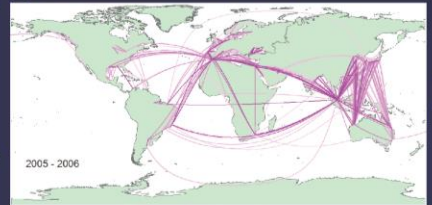


Environment

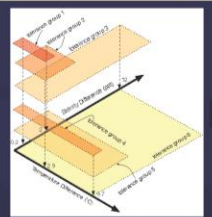


Ecoregion

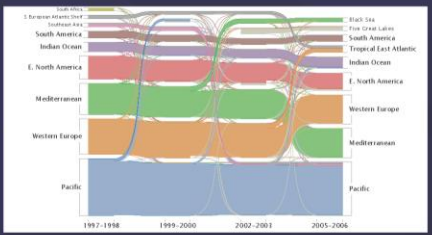
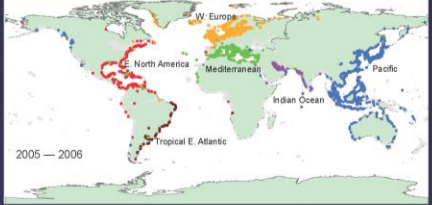
Species flow network



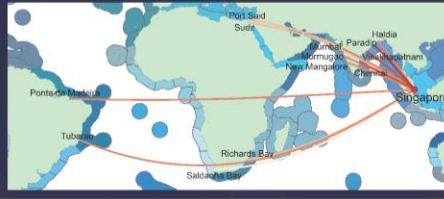
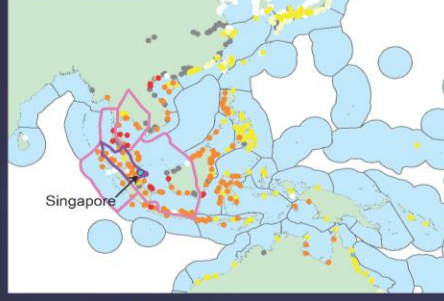
Invasion risk network



Clustering analysis



Risk assessment



Takeaways

NIS-RAPS:

Integrates multiple sources of data.

A network approach for invasive species modeling.

Provides insights to inform policy makers.

Shipping network construction

How does network construction choices influence network properties and analysis results?



Lloyds ship movement data

Work

Ducruet
2013

Ducruet
2012

Ducruet
2010

Ducruet
2010b

Gonzalez
Laxe 2012

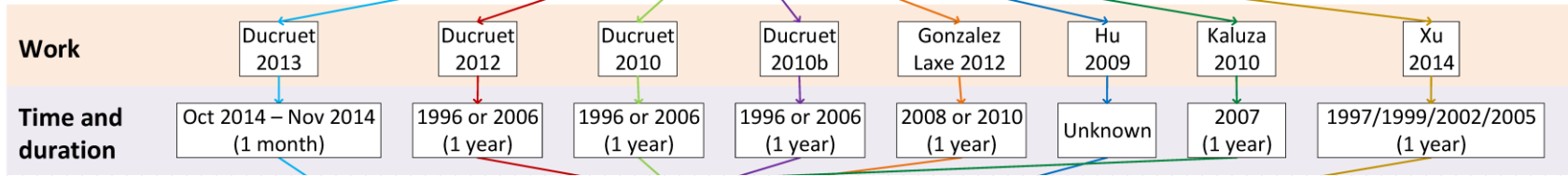
Hu
2009

Kaluza
2010

Xu
2014

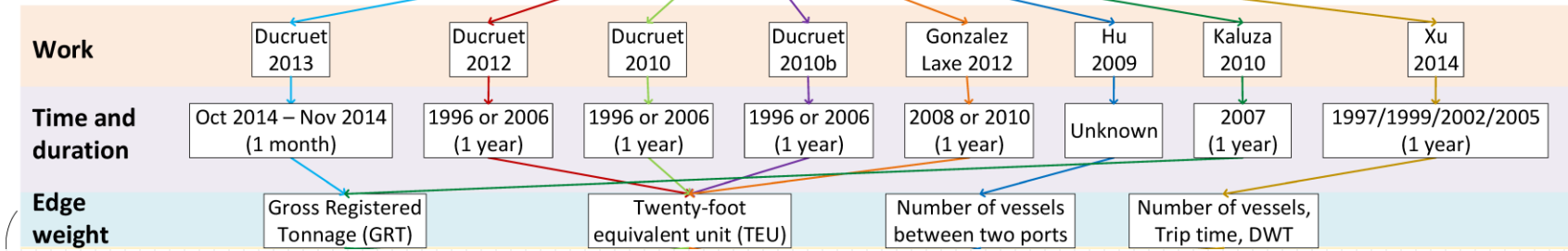


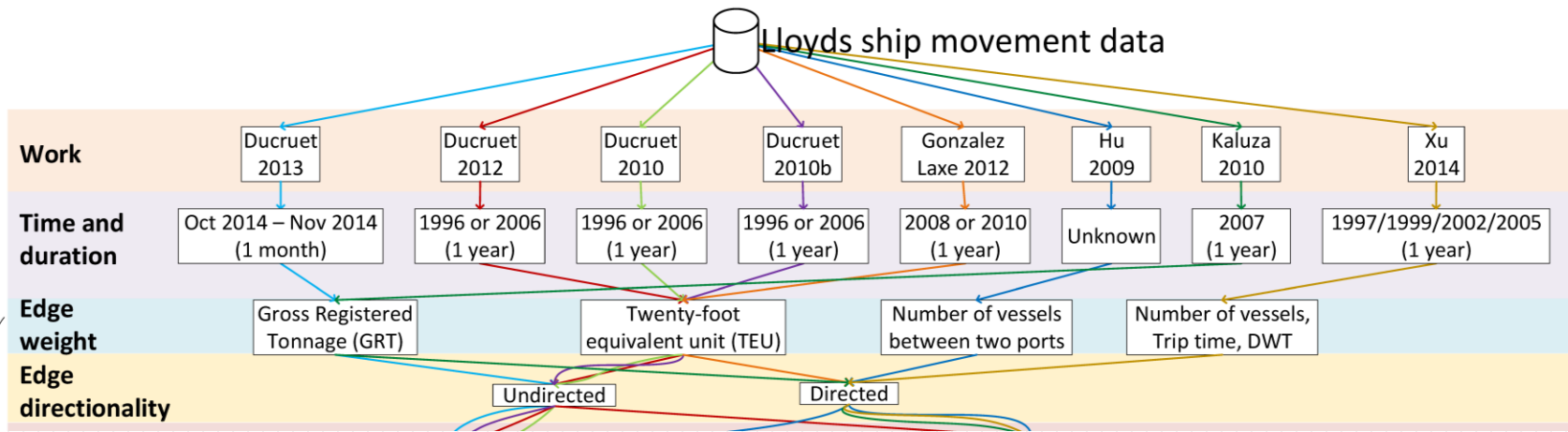
Lloyds ship movement data





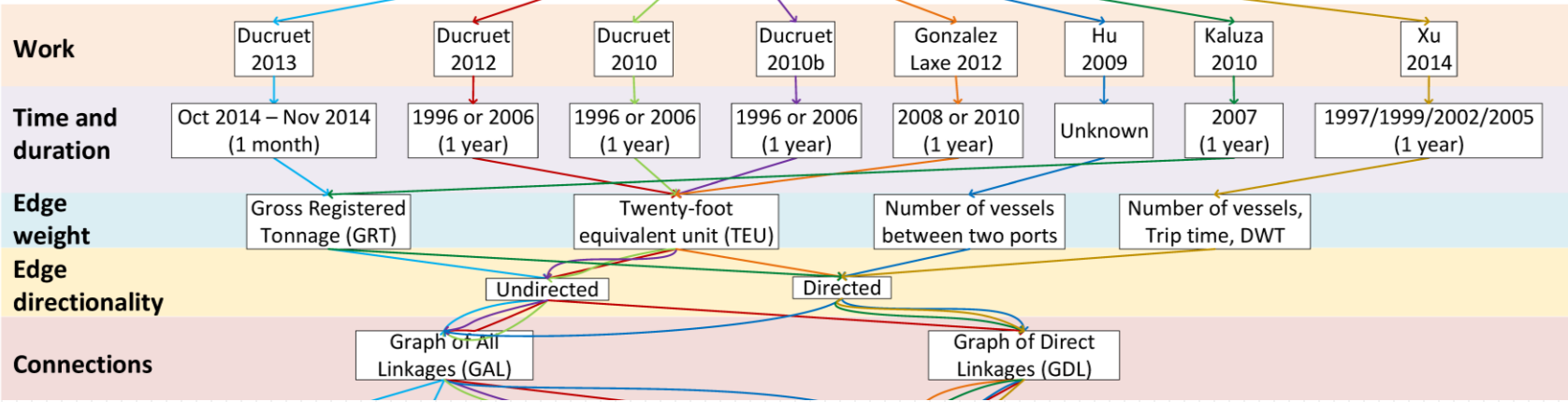
Lloyds ship movement data

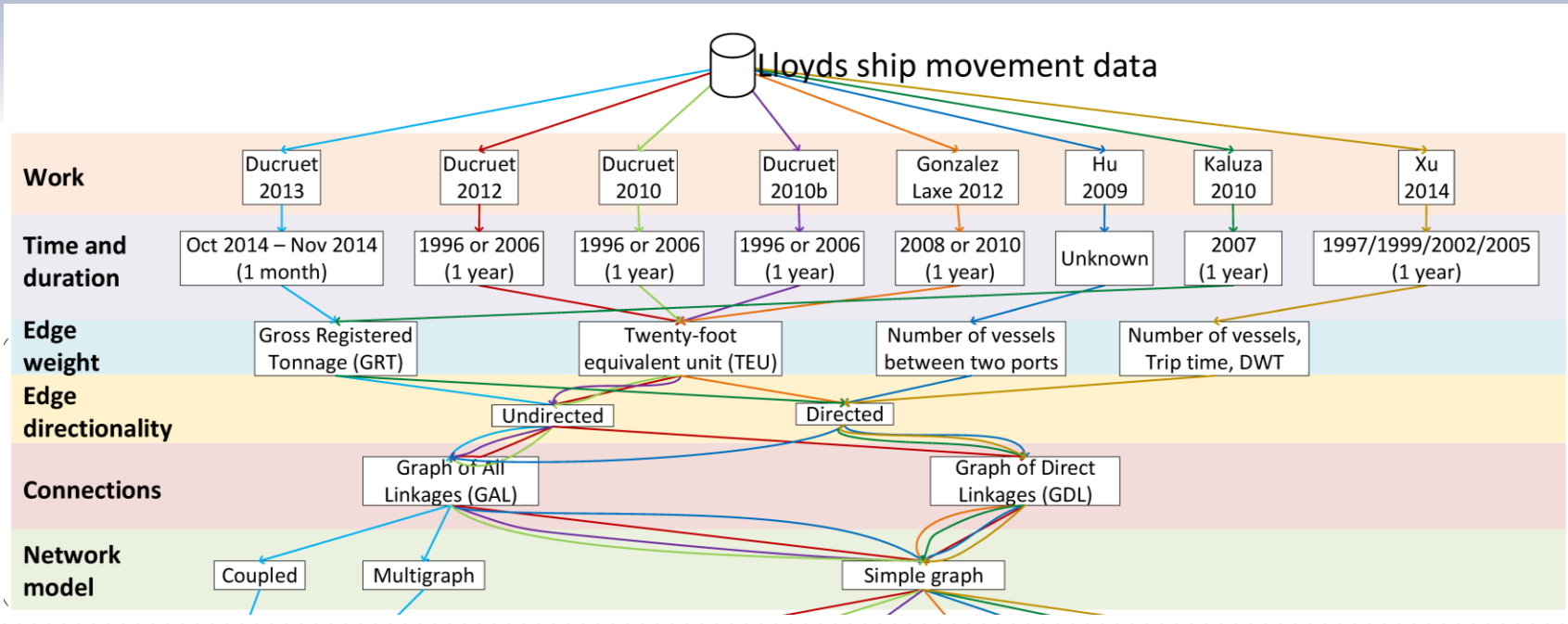




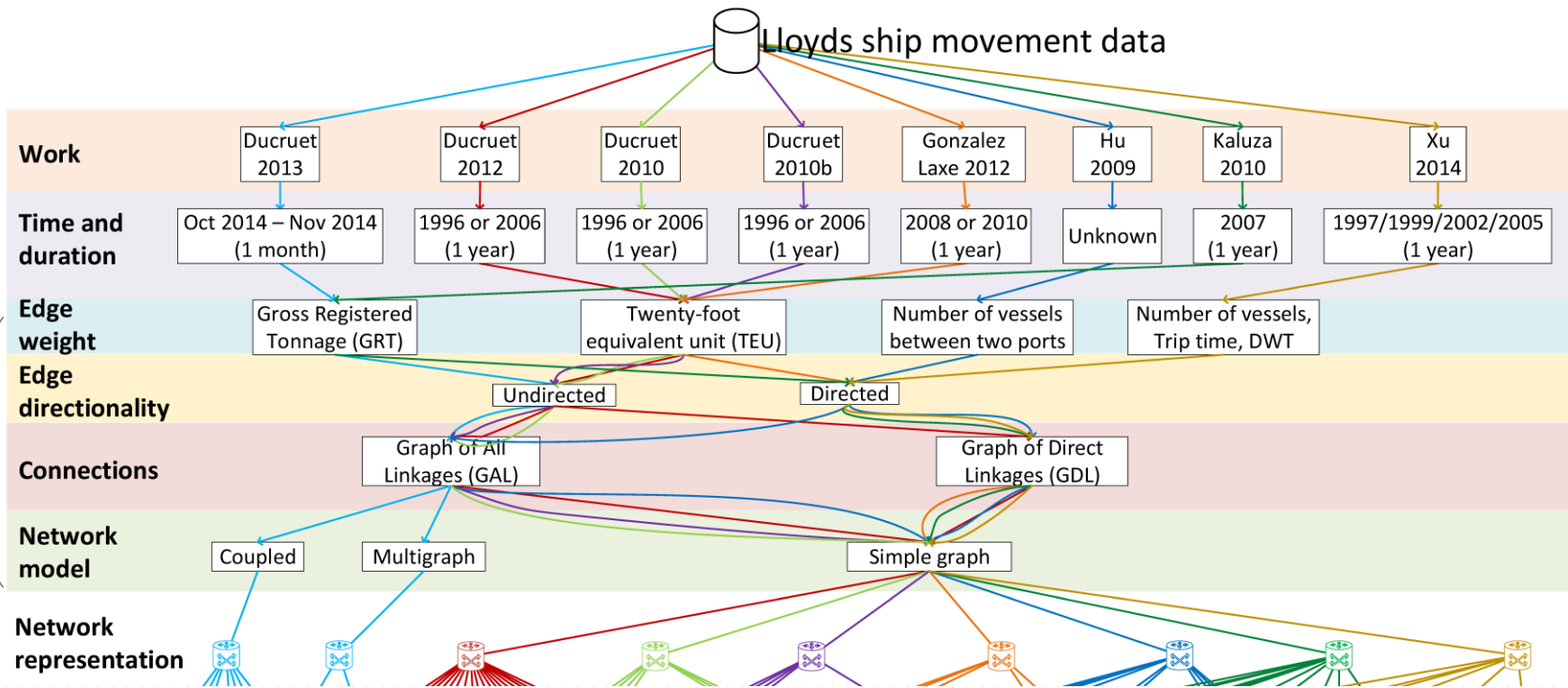


Lloyds ship movement data

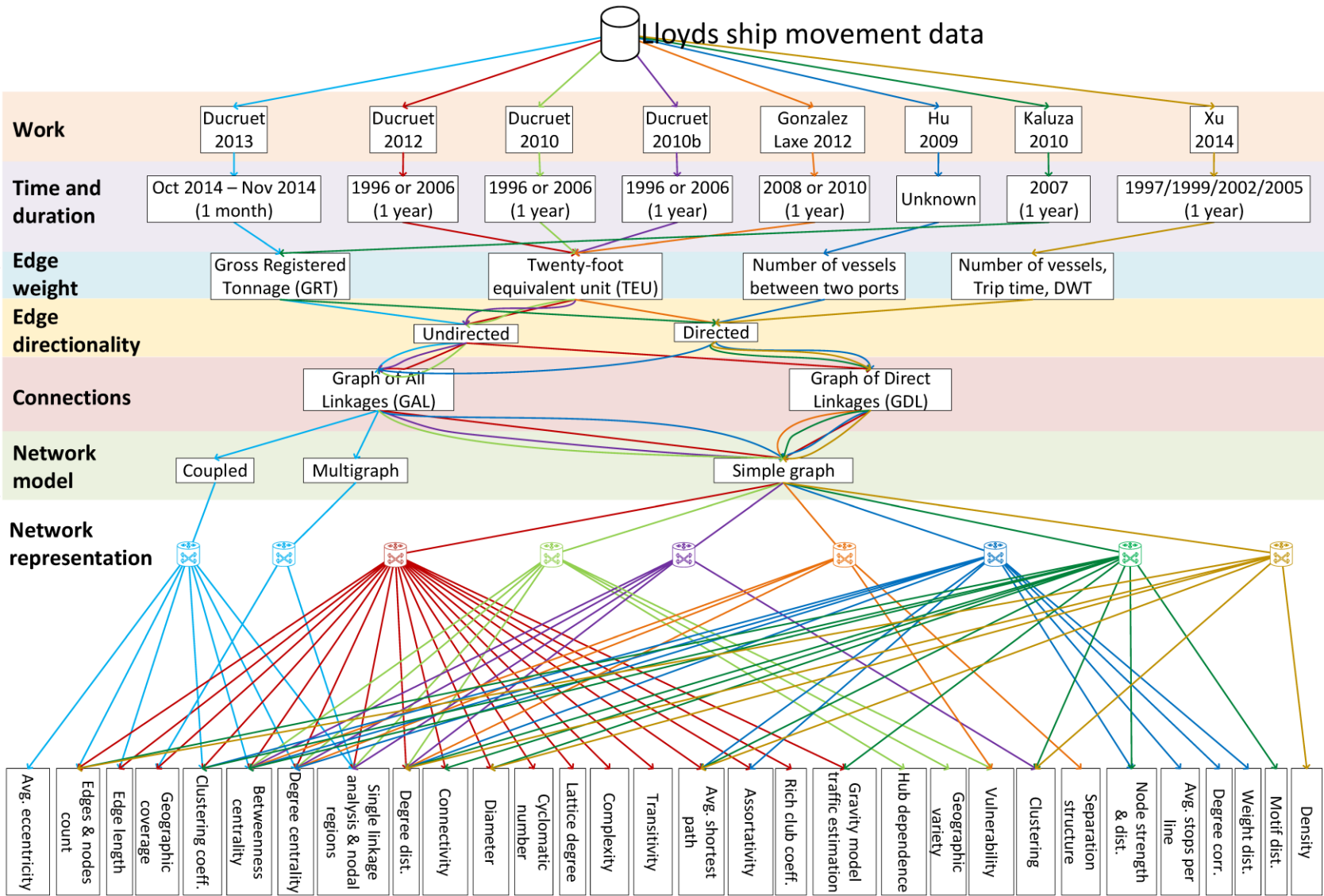




Network construction



Network construction

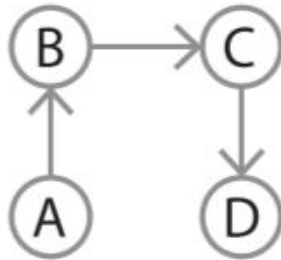


Network linkage mechanisms

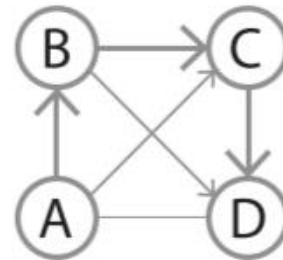
Raw trajectory

A B C D

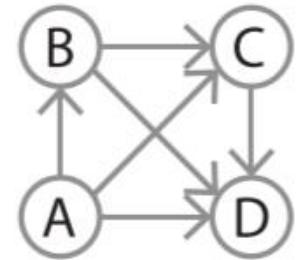
Direct linkage



Weighted indirect linkage



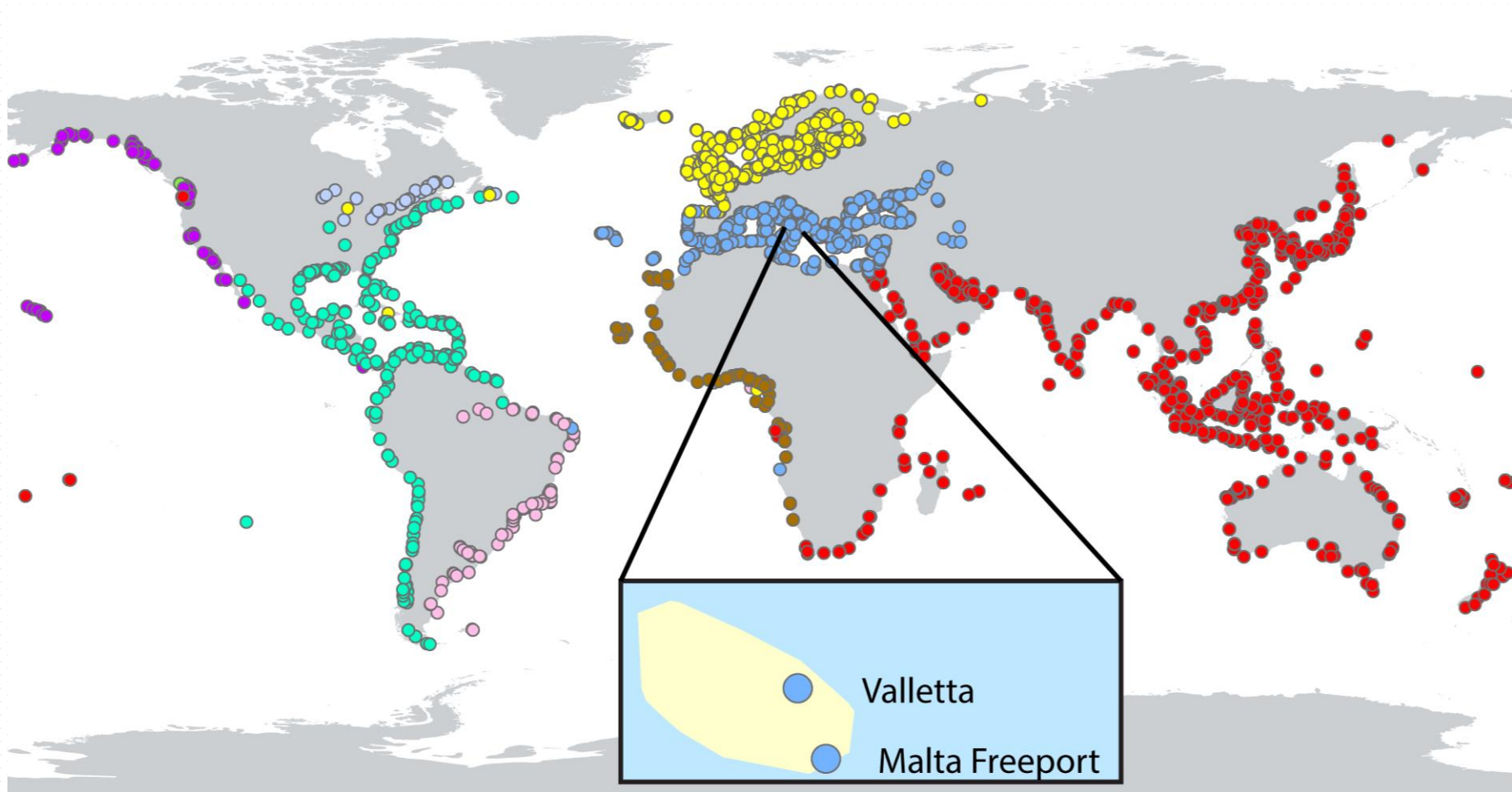
Indirect linkage



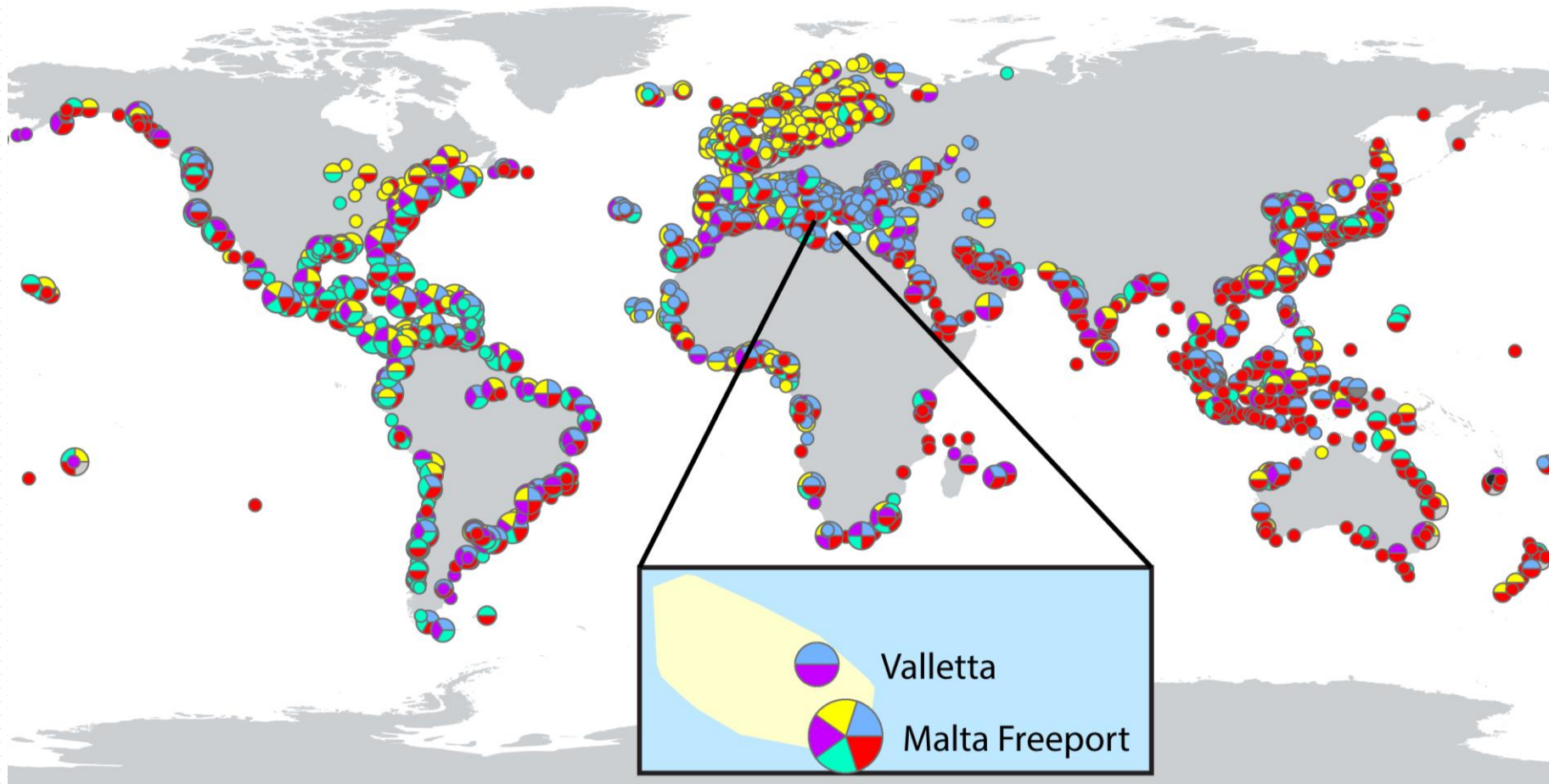
Network linkage mechanisms

	Direct Linkage		Indirect Linkage
num_of_nodes	3.60E+3	=	3.60E+3
num_of_edges	1.32E+5	<	7.37E+5
density	2.05E-2	<	1.14E-1
average_degree	7.35E+1	<	4.10E+2
highest_degree	1.28E+3	<	2.42E+3
generalized_clustering_coefficient	5.48E-1	<	7.23E-1
transitivity	2.96E-1	<	4.96E-1
avg_shortest_path	2.65	>	2.04
diameter	8	>	5
radius	4	>	3

Clustering: first-order network



Clustering: higher-order network



Takeaways

Global shipping traffic is:

Imbalanced in directionality – directed network

Unevenly distributed shipping frequency & traffic – weighted network

Higher-order movement patterns – higher-order network

Other important factors include

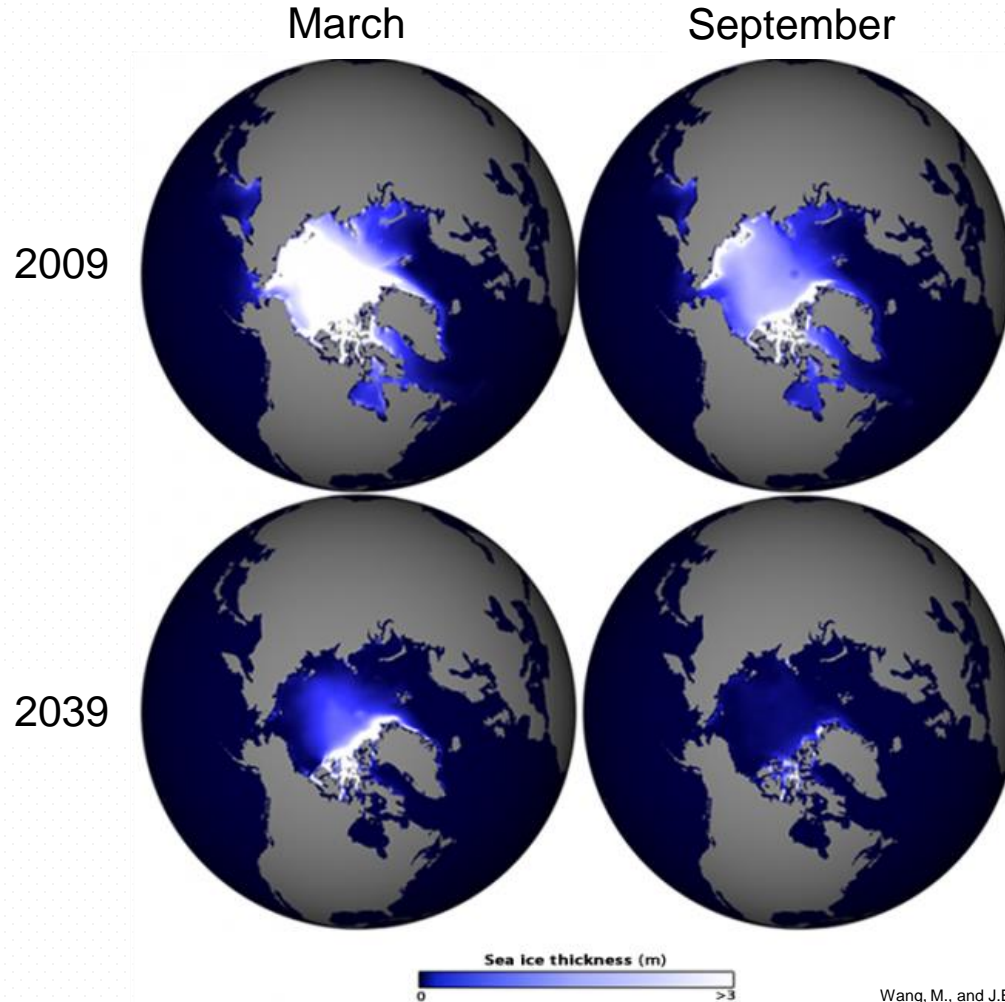
Linkage mechanisms, time window, seasonality, evolution

Considerations when representing shipping traffic as network, or reporting analysis results

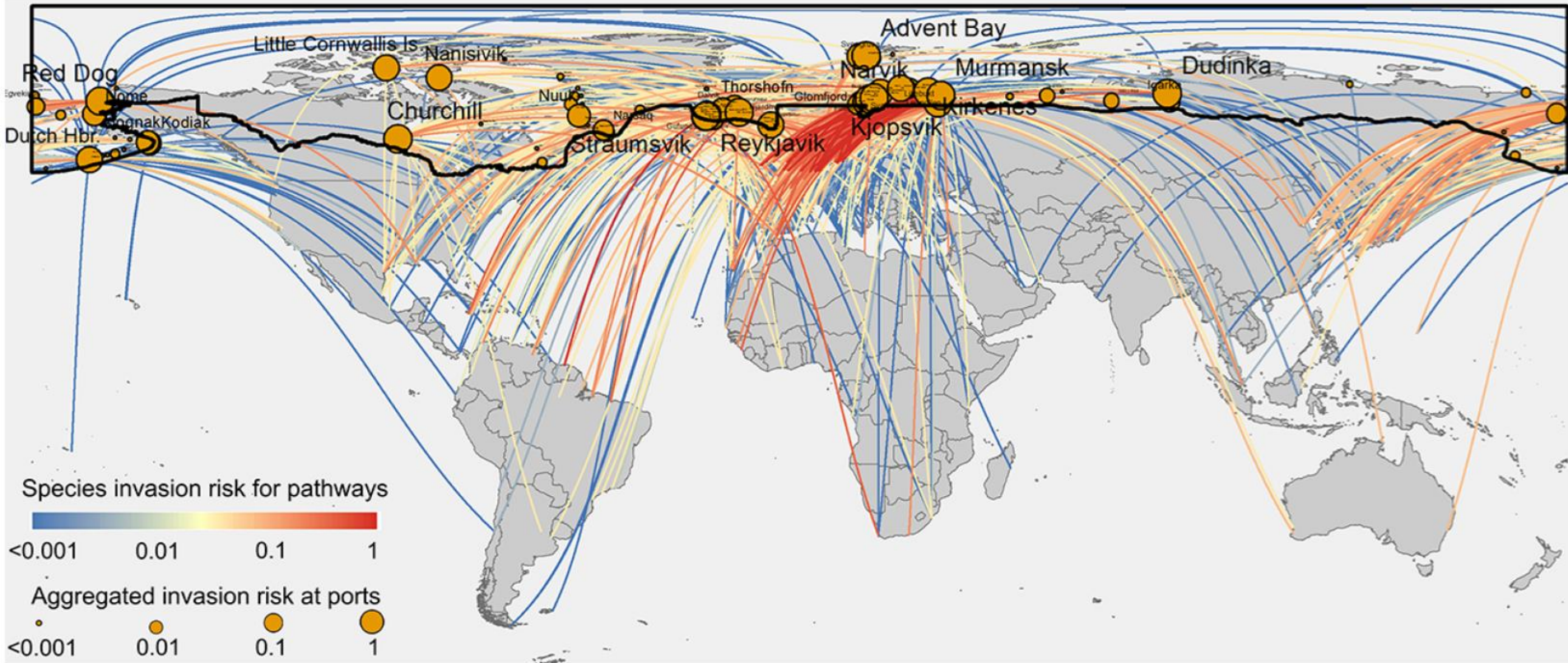
Species invasion in the Arctic

Introduction to Arctic ports & diffusion among Arctic ports

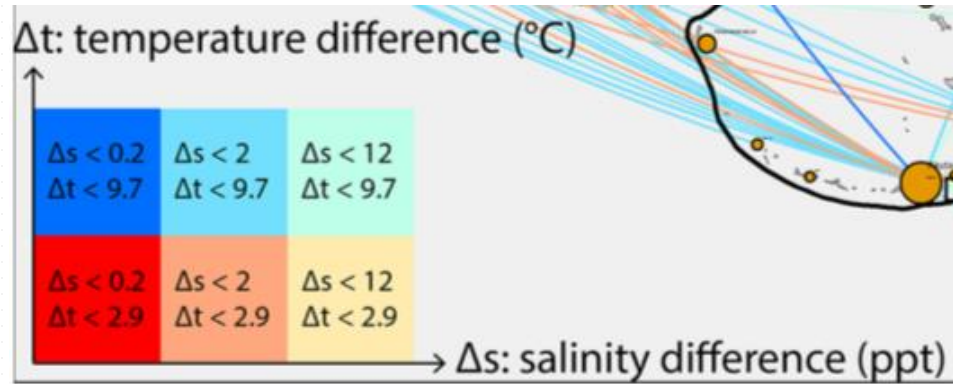
The melting Arctic sea ice



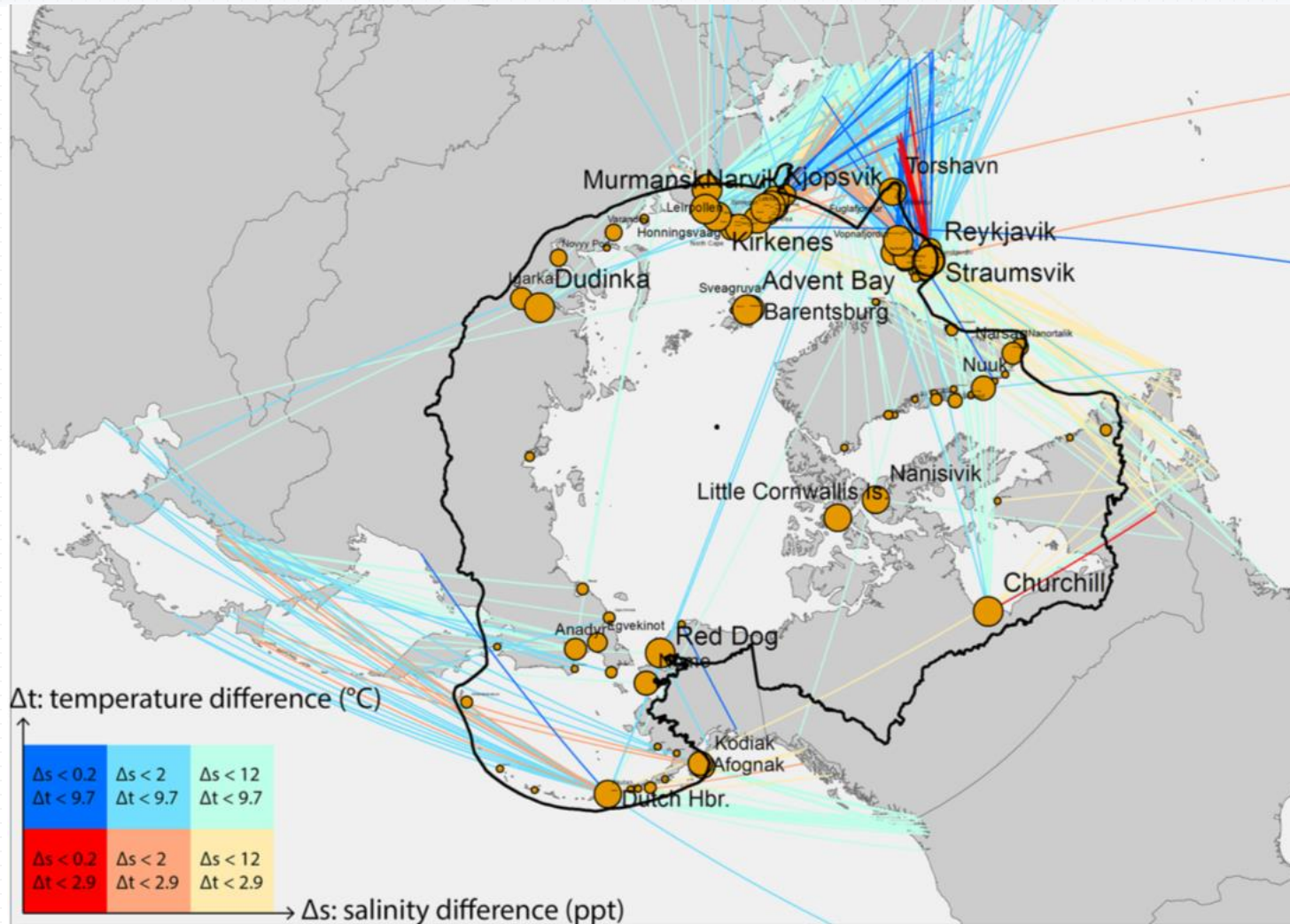
Species introduction pathways to the Arctic



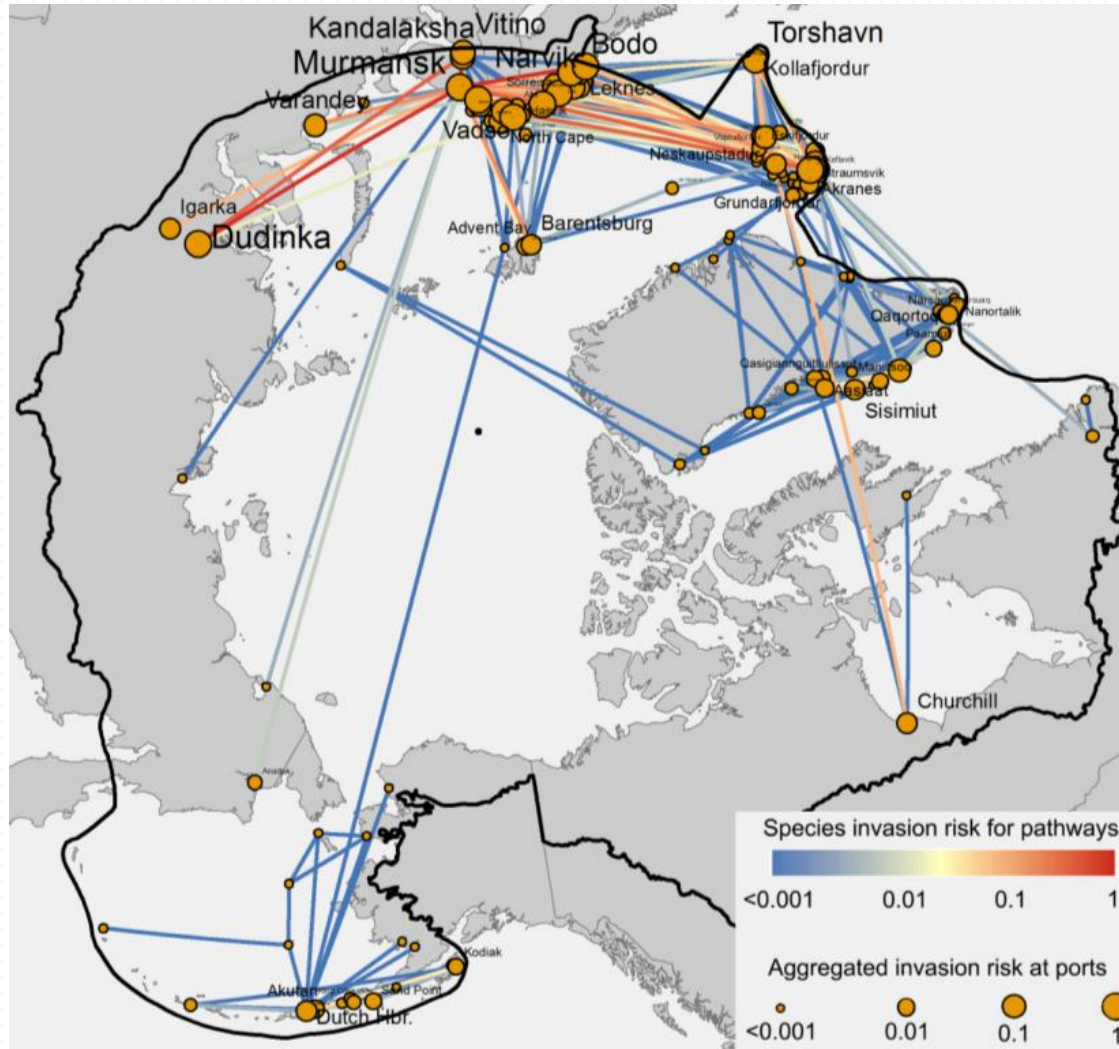
Environmental tolerance



Environmental tolerance

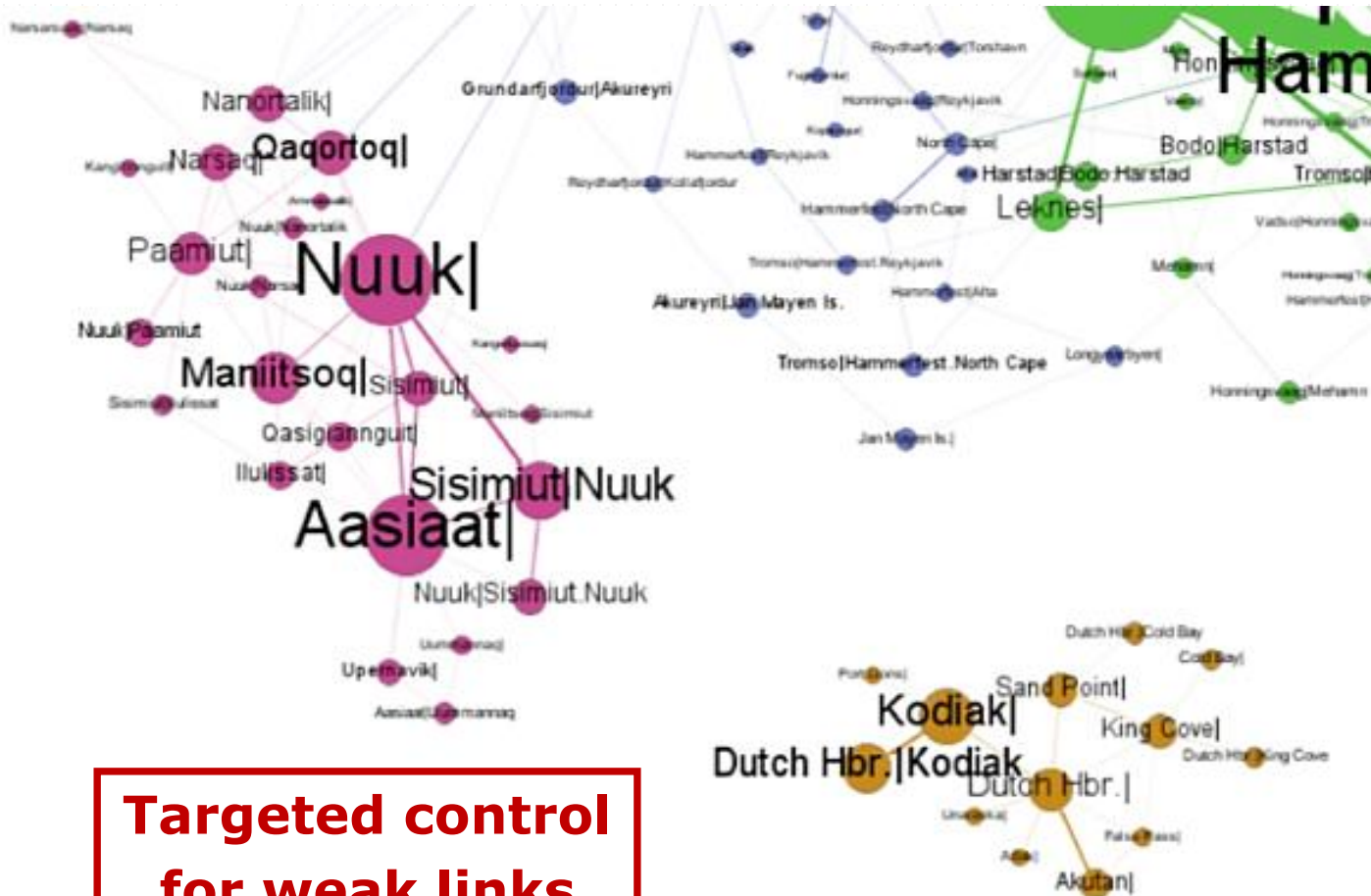


Species diffusion within the Arctic



	HON for ship movements	HON for species flow (SF-HON)
Input	<p>Ship 1: ● Port 1 $\xrightarrow{1 \text{ trip}}$ ● Port 3 $\xrightarrow{1 \text{ trip}}$ ● Port 4 \dashrightarrow</p> <p>Ship 2: ● Port 2 $\xrightarrow{1 \text{ trip}}$ ● Port 3 $\xrightarrow{1 \text{ trip}}$ ● Port 5 \dashrightarrow</p>	<p>Ship 1: ● Type k_1 Port 1 $\xrightarrow{D_{13} \Delta t_{13}}$ ● Port 3 $\xrightarrow{D_{34} \Delta t_{34}}$ ● Port 4 \dashrightarrow</p> <p>Ship 2: ● Type k_2 Port 2 $\xrightarrow{D_{23} \Delta t_{23}}$ ● Port 3 $\xrightarrow{D_{35} \Delta t_{35}}$ ● Port 5 \dashrightarrow</p>
Influence per trip	<p>Ship 1: ● Port 1 $\xrightarrow{1 \text{ trip}}$ ● Port 3</p>	<p>Ship 1: ● Type k_1 Port 1 $\xrightarrow{P_{1 \rightarrow 3}^{(1)} = (1 - e^{-\lambda D_{1 \rightarrow 3}^{(1)}}) e^{-u \Delta_{1 \rightarrow 3}^{(1)}}}$ ● Port 3</p>
Counting subsequences	<p>● Port 3 \rightarrow ● Port 4 30 trips = 1 + 1 + ...</p> <p>● Port 3 \rightarrow ● Port 5 10 trips = 1 + 1 + ...</p> <p>● Port 1 \rightarrow ● Port 3 \rightarrow ● Port 4 8 trips = 1 + 1 + ...</p>	<p>● Port 3 \rightarrow ● Port 4 $0.6 = P_{3 \rightarrow 4} = 1 - \prod_t (1 - P_{3 \rightarrow 4}^{(t)})$</p> <p>● Port 3 \rightarrow ● Port 5 $0.4 = P_{3 \rightarrow 5} = 1 - \prod_t (1 - P_{3 \rightarrow 5}^{(t)})$</p> <p>● Port 1 \rightarrow ● Port 3 \rightarrow ● Port 4 $0.1 = P_{1 \rightarrow 3 \rightarrow 4} = 1 - \prod_t (1 - P_{1 \rightarrow 3 \rightarrow 4}^{(t)})$</p>
Normalization	<p>● Port 3 $\xrightarrow{0.75}$ ● Port 4</p> <p>● Port 3 $\xrightarrow{0.25}$ ● Port 5</p>	<p>● Port 3 $\xrightarrow{0.6}$ ● Port 4</p> <p>● Port 3 $\xrightarrow{0.4}$ ● Port 5</p>
Rule extraction terminating condition	<p>Minimum support = 10</p> <p>● Port 3 \rightarrow ● Port 4 30 trips > 10</p> <p>● Port 1 \rightarrow ● Port 3 \rightarrow ● Port 4 8 trips < 10</p>	<p>Minimum support = 0.2</p> <p>● Port 3 \rightarrow ● Port 4 $0.6 > 0.2$</p> <p>● Port 1 \rightarrow ● Port 3 \rightarrow ● Port 4 $0.1 < 0.2$</p>

Species flow higher-order network



**Targeted control
for weak links**

Case studies

Soft shell clam



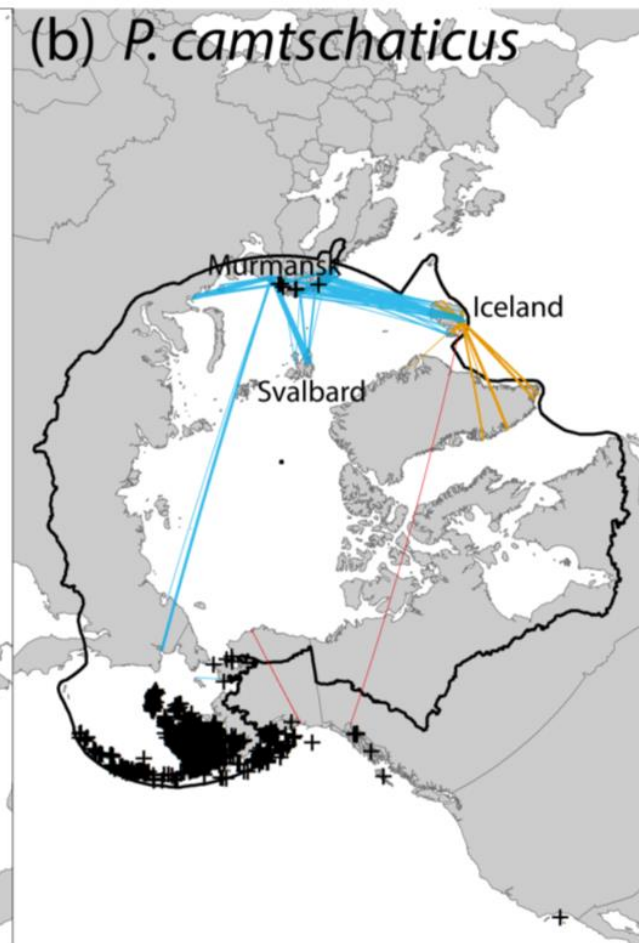
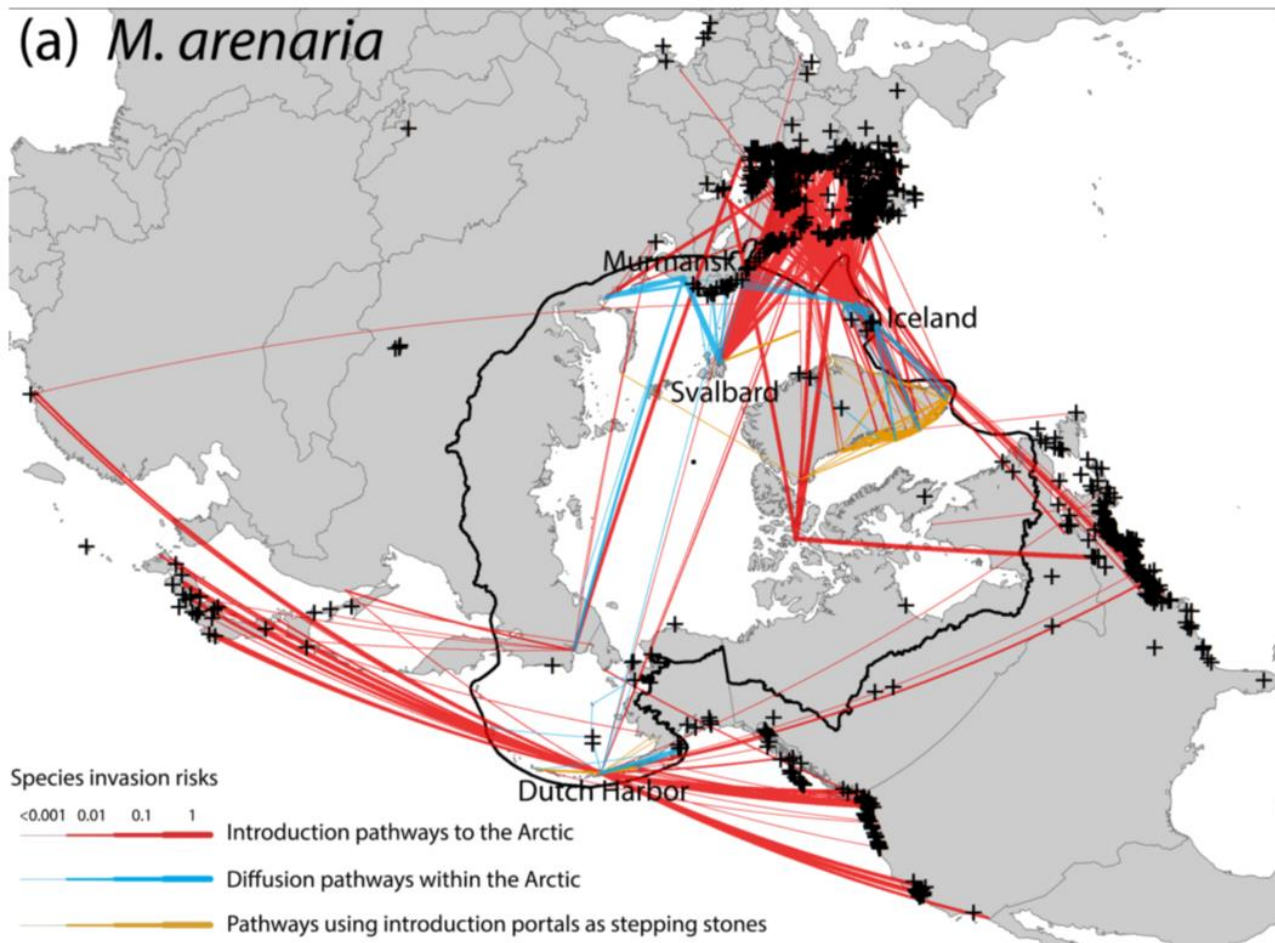
Scientific name: *M. arenaria*
Temperature tolerance: -2 – 18 °C
Salinity tolerance: 28 – 35 PSU

Red king crab



Scientific name: *P. camtschaticus*
Temperature tolerance: -2 – 18 °C
Salinity tolerance: 28 – 35 PSU

Case studies



Risk projection

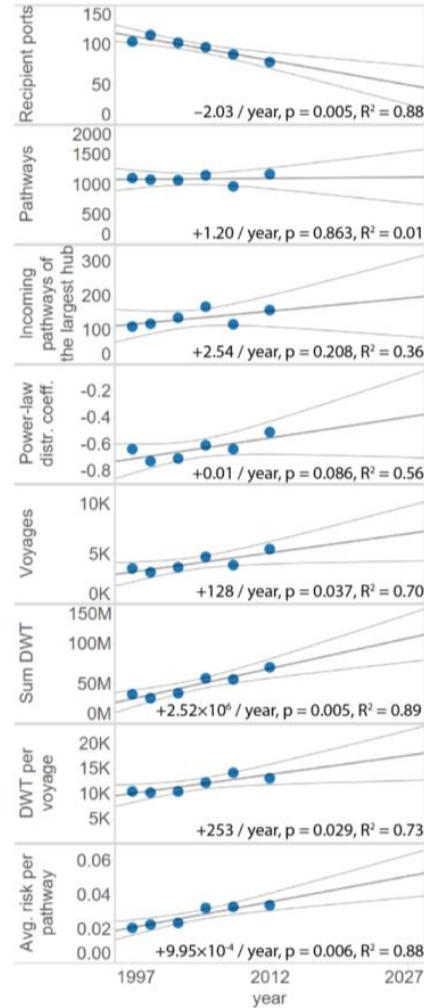
Decreasing recipient ports

Increased connections at hubs

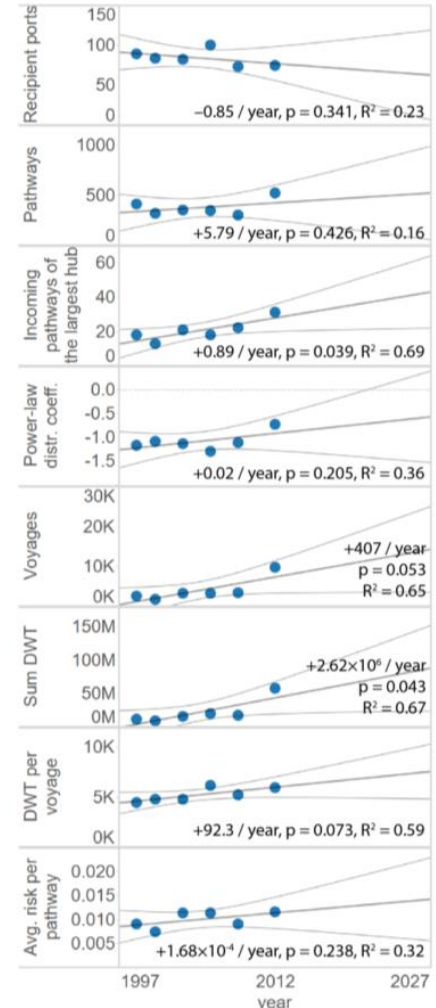
Emergence of hubs

“Rich gets richer”

Introduction to the Arctic



Diffusion within the Arctic



Risk projection

Decreasing recipient ports

Same # of pathways
Emergence of hubs
 Increased connections at hubs

“Rich gets richer”

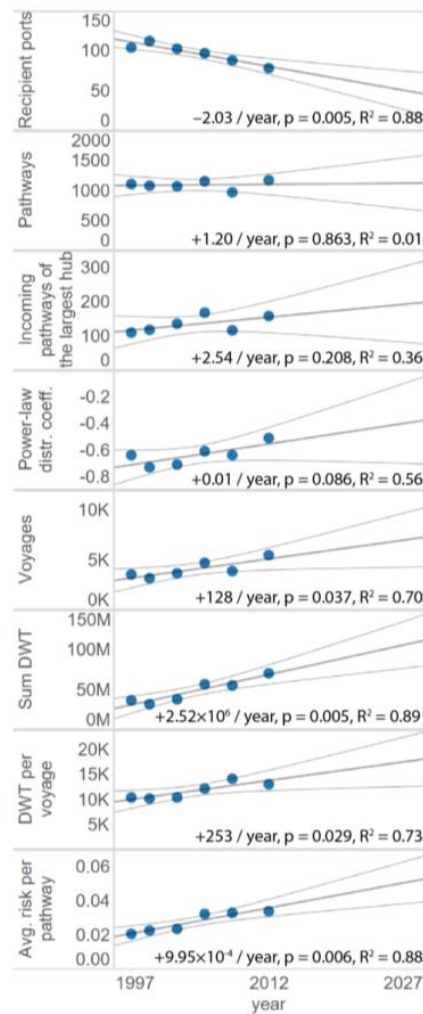
Increasing voyages

Increasing sum of shipping

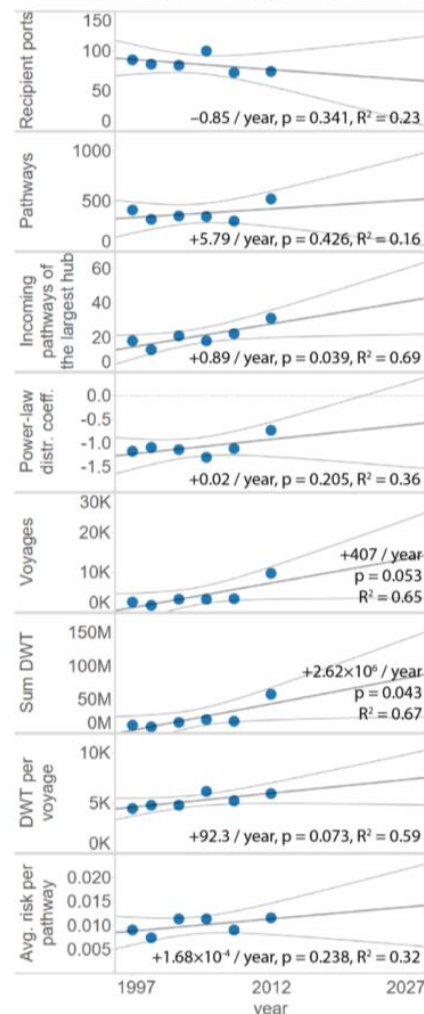
Increasing average shipping size
Increasing risk

Increasing risk per pathway

Introduction to the Arctic

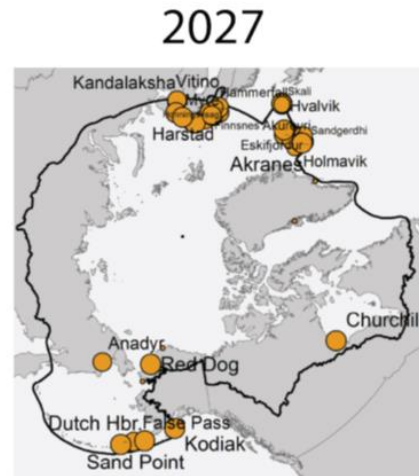
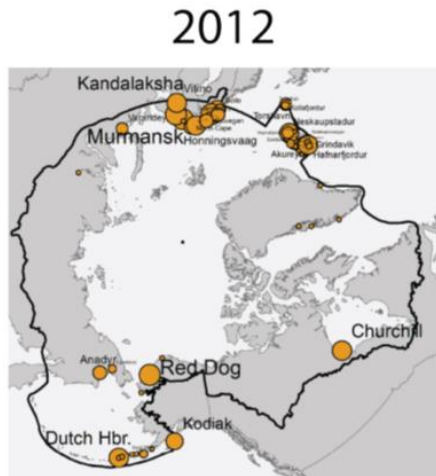
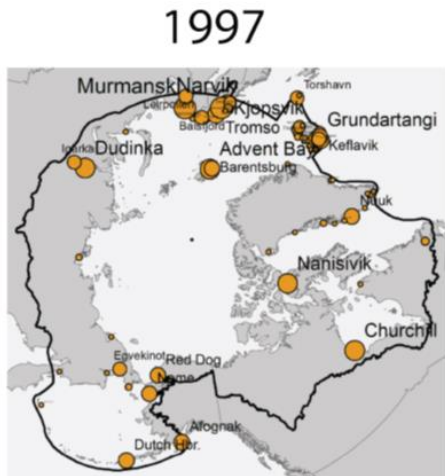


Diffusion within the Arctic

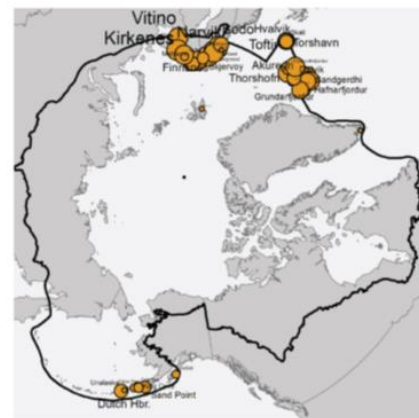
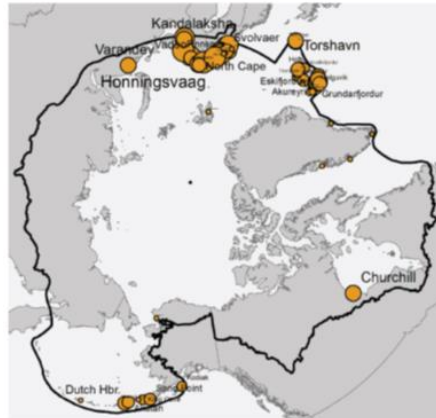
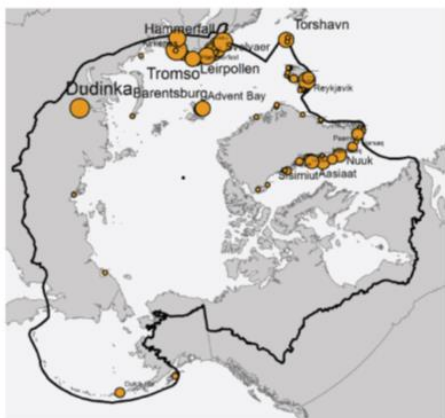


Risk projection

Introduction to the Arctic

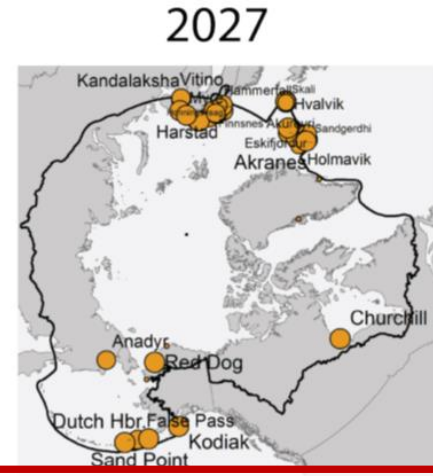
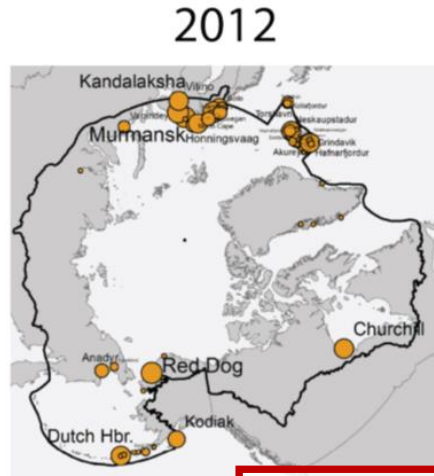
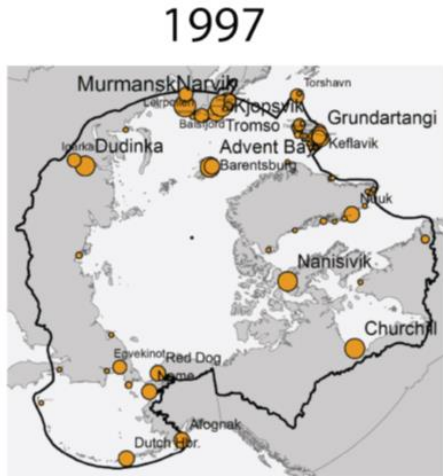


Diffusion within the Arctic

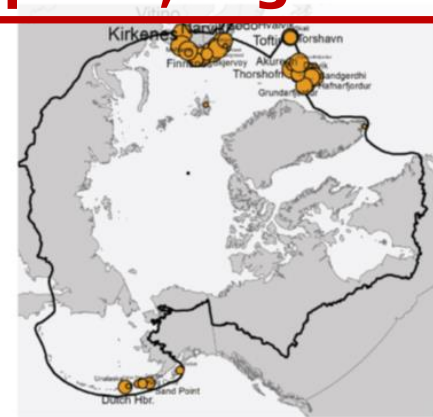
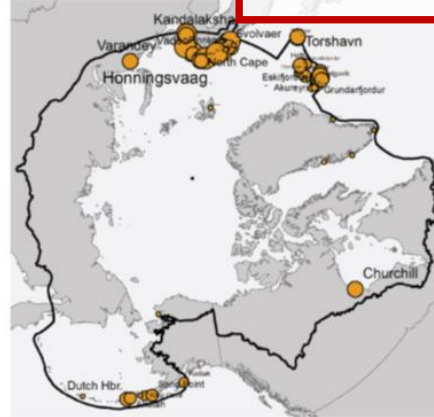
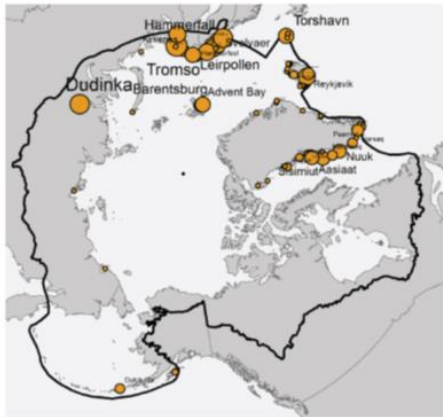


Risk projection

Introduction to the Arctic



Diffusion within the Arctic



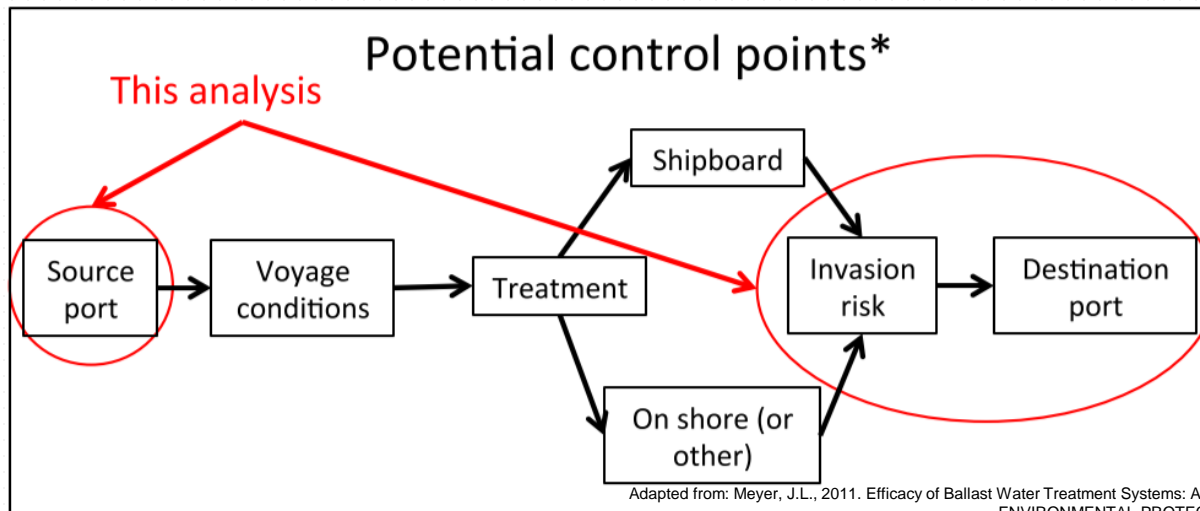
Fewer ports, higher risks



Takeaways

Arctic species invasion

- Increasing risk
- Emergence of hubs
- Targeted controls



Anomaly detection

Unveiling higher-order anomalies with HON

Anomaly detection with dynamic network

Time frames: _____ |

Trajectory 1: f a c d g f b c e g

Trajectory 2: f a c e g f b c d g

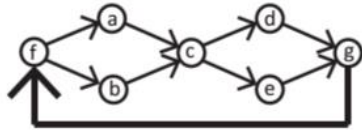
Trajectory 3: f b c d g f a c e g

Trajectory 4: f b c e g f a c d g

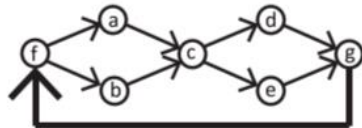
Anomaly detection with dynamic network

Time frames: _____ |
Trajectory 1: f a c d g f b c e g
Trajectory 2: f a c e g f b c d g
Trajectory 3: f b c d g f a c e g
Trajectory 4: f b c e g f a c d g

First-order network



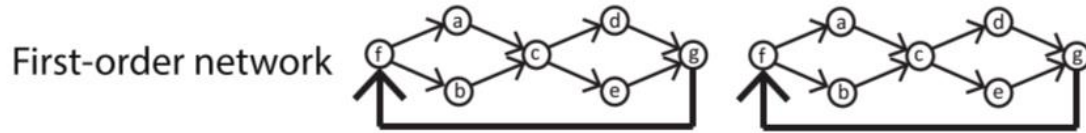
Higher-order network



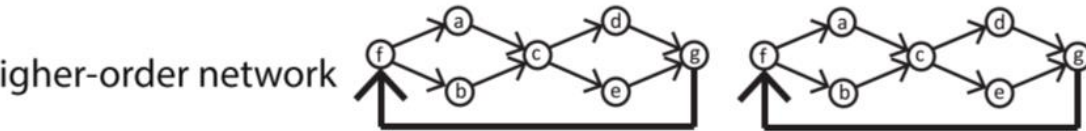
Anomaly detection with dynamic network

Time frames: I II

Trajectory 1: f a c d g f b c e g | f a c e g f b c d g
 Trajectory 2: f a c e g f b c d g | f a c d g f b c e g
 Trajectory 3: f b c d g f a c e g | f b c e g f a c d g
 Trajectory 4: f b c e g f a c d g | f b c d g f a c e g



Network distances $D(G_1, G_2) = 0$



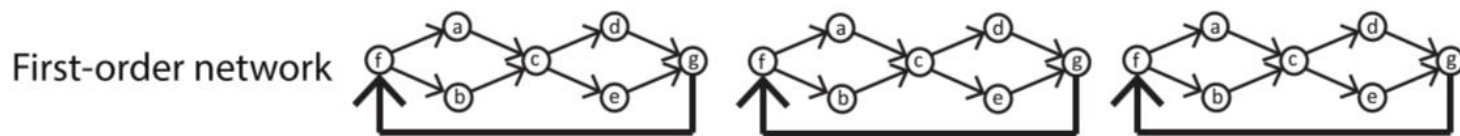
Network distances $D(G_1, G_2) = 0$

$$D(G, H) = \frac{\sum_{u,v \in V} \frac{|w_E^G(u,v) - w_E^H(u,v)|}{\max(w_E^G(u,v), w_E^H(u,v))}}{|E_G \cup E_H|}$$

Anomaly detection with dynamic network

Second-order patterns **emerge**

Time frames:	I	II	III
Trajectory 1:	f a c d g f b c e g	f a c e g f b c d g	f a c d g f b c e g
Trajectory 2:	f a c e g f b c d g	f a c d g f b c e g	f a c d g f b c e g
Trajectory 3:	f b c d g f a c e g	f b c e g f a c d g	f b c e g f a c d g
Trajectory 4:	f b c e g f a c d g	f b c d g f a c e g	f b c e g f a c d g

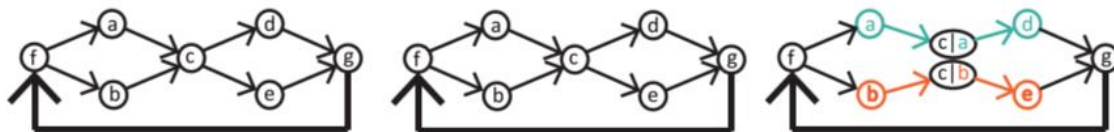


Network distances

$$D(G_1, G_2) = 0$$

$$D(G_2, G_3) = 0$$

Higher-order network

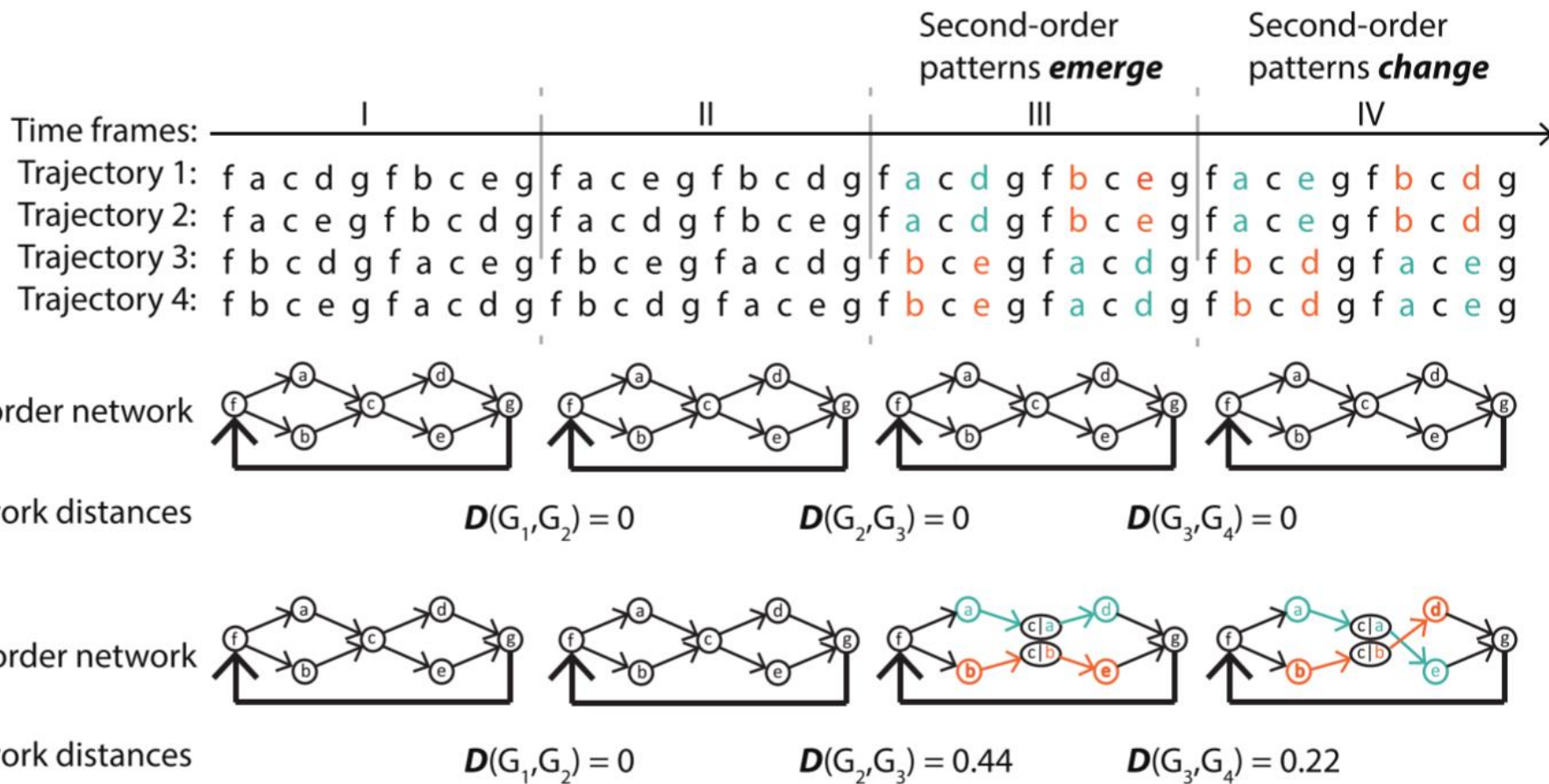


Network distances

$$D(G_1, G_2) = 0$$

$$D(G_2, G_3) = 0.44$$

Anomaly detection with dynamic network



Second-order patterns **emerge**

Second-order patterns **change**

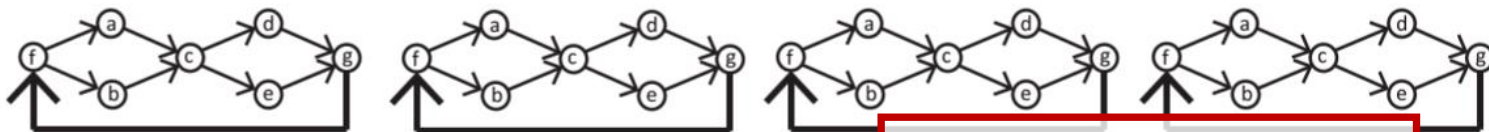
Anomaly detection with dynamic network

Time frames:	I	II	III	IV
Trajectory 1:	f a c d g f b c e g	f a c e g f b c d g	f a c d g f b c e g	f a c e g f b c d g
Trajectory 2:	f a c e g f b c d g	f a c d g f b c e g	f a c d g f b c e g	f a c e g f b c d g
Trajectory 3:	f b c d g f a c e g	f b c e g f a c d g	f b c e g f a c d g	f b c d g f a c e g
Trajectory 4:	f b c e g f a c d g	f b c d g f a c e g	f b c e g f a c d g	f b c d g f a c e g

Second-order patterns **emerge**

Second-order patterns **change**

First-order network



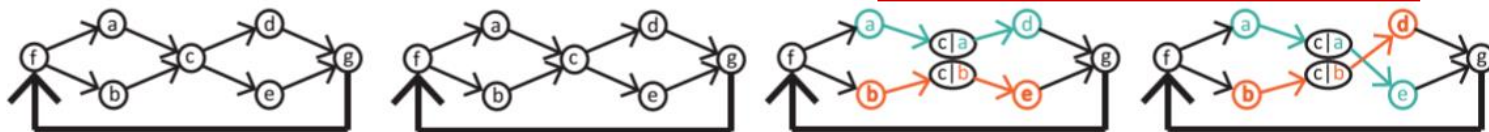
Network distances

$$D(G_1, G_2) = 0$$

$$D(G_2, G_3) = 0$$

No changes in Network topology

Higher-order network



Network distances

$$D(G_1, G_2) = 0$$

$$D(G_2, G_3) = 0.46$$

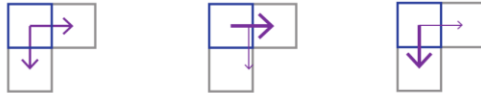
Capturing complex anomalous patterns

Synthetic data with 11 billion movements

100,000 ships, each moving 100 steps;
11 scenarios, each repeating 100 times;
Total: 11,000,000,000 movements

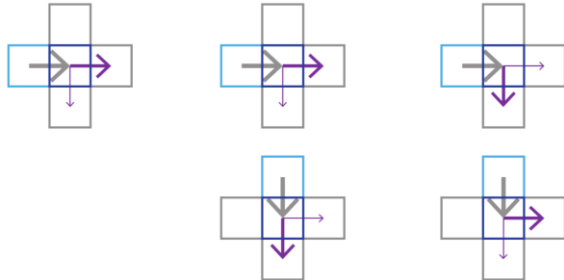
First order

$t = [1, 100]$ Random walking right and down
 $t = [101, 200]$ Add first order @ cell 00, 03, 06
 $t = [201, 300]$ Change first order @ cell 00, 03, 06



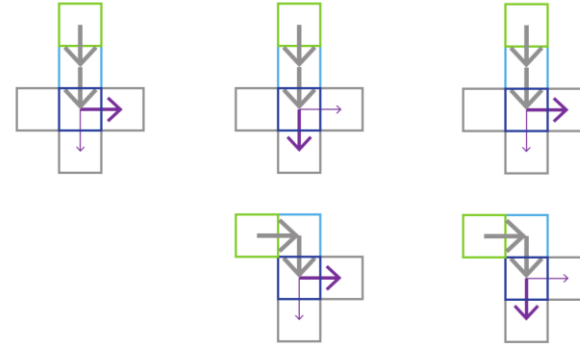
Second order

$t = [301, 400]$ Add second order @ cell 28
 $t = [401, 500]$ Add second orders @ cell 31, 35
 $t = [501, 600]$ Change second orders @ cell 31, 35



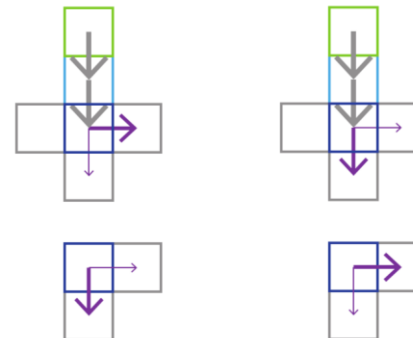
Third order

$t = [601, 700]$ Add third order @ cell 81
 $t = [701, 800]$ Add third orders @ cell 84, 87
 $t = [801, 900]$ Change third orders @ cell 84, 87



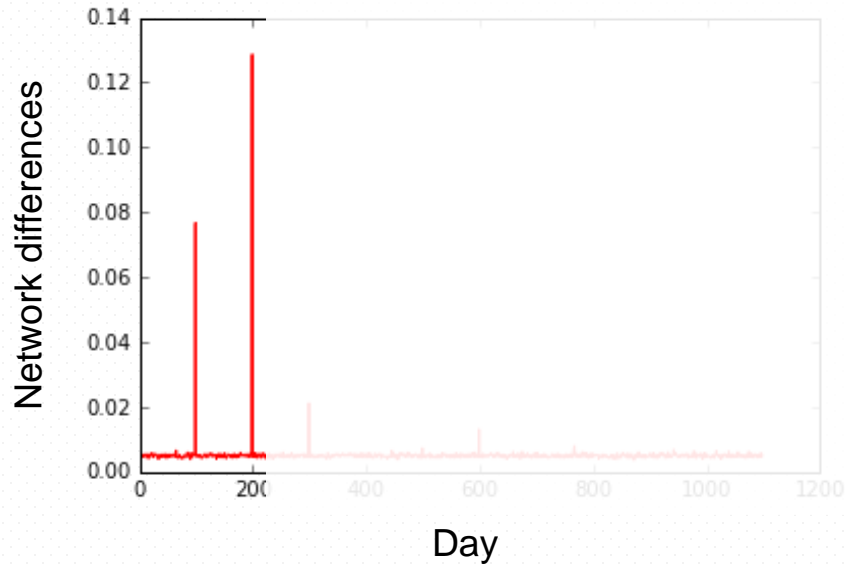
Mixed order

$t = [901, 1000]$ Add mixed orders @ cell 59
 $t = [1001, 1100]$ Change mixed orders @ cell 59

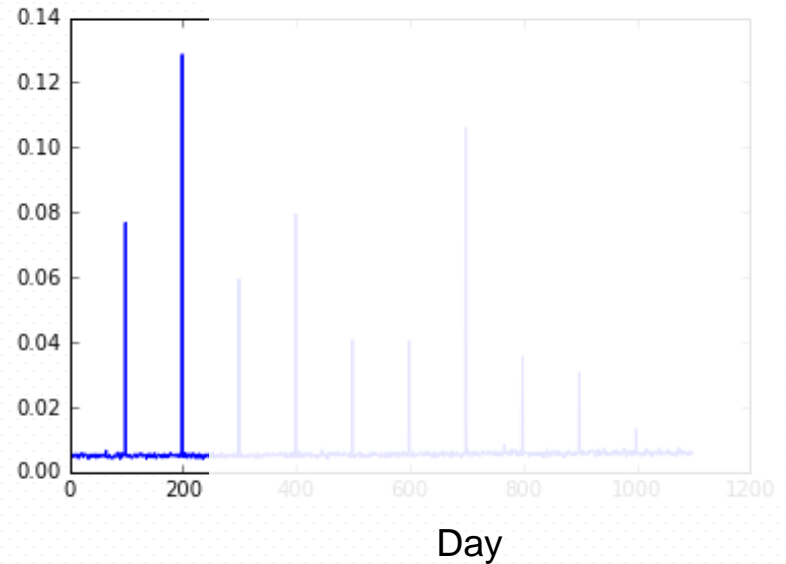


Higher-order anomalies captured by HON

First-order network

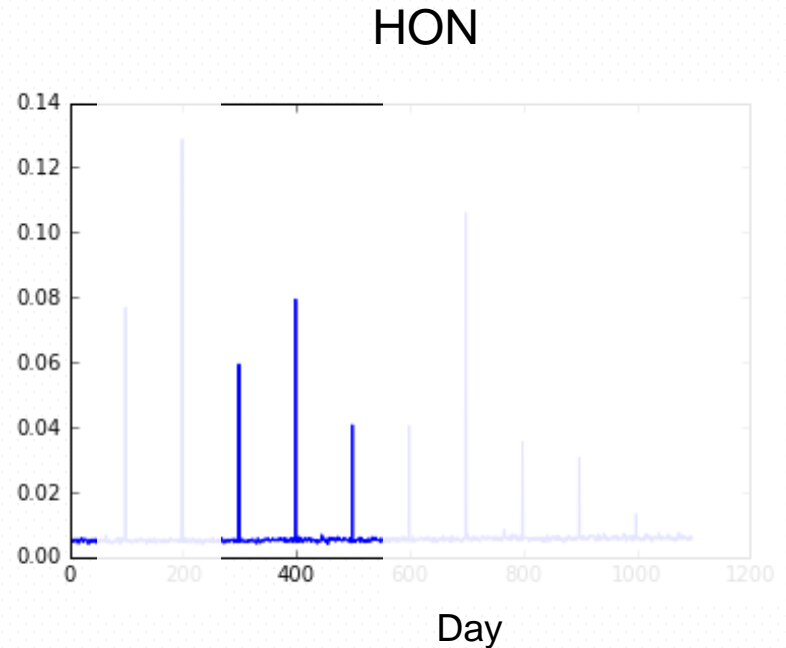
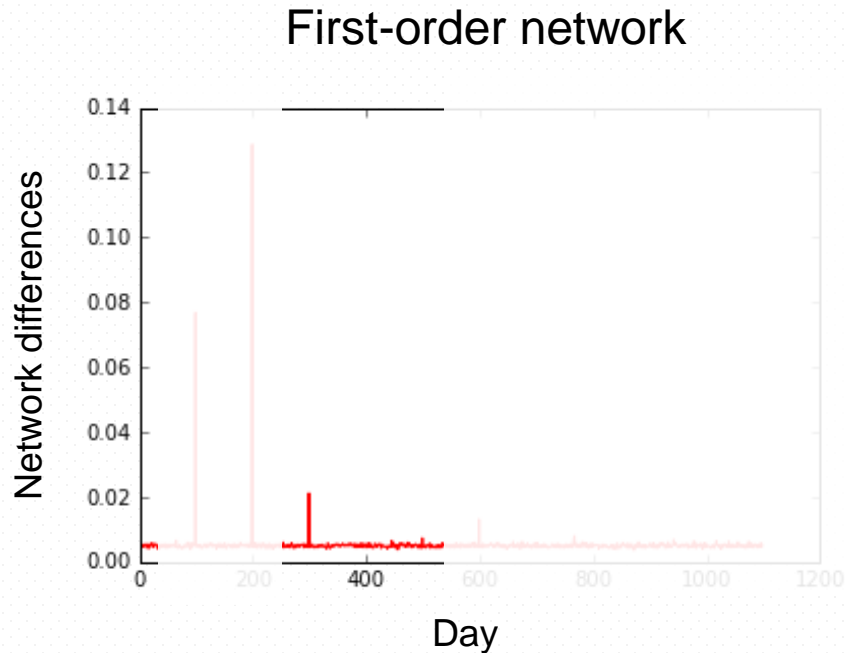


HON



Injection and alternation of 1st order dependencies

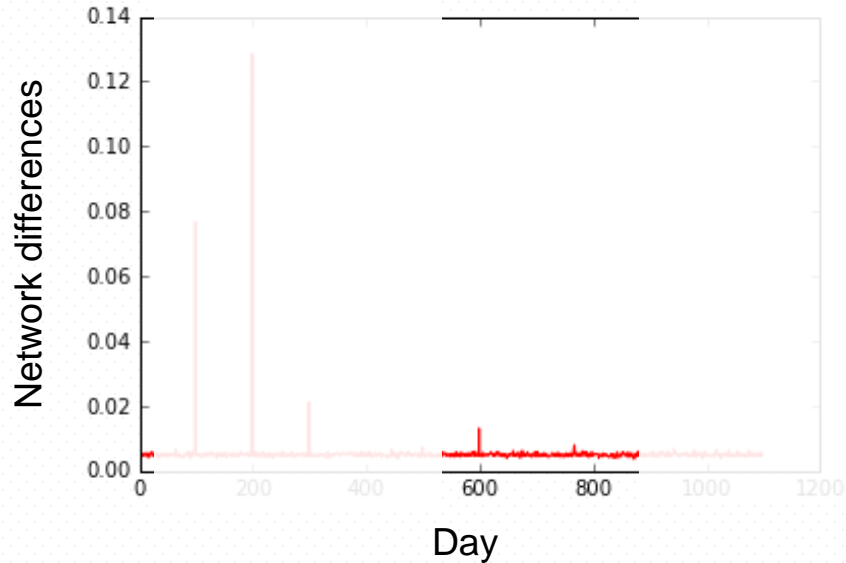
Higher-order anomalies captured by HON



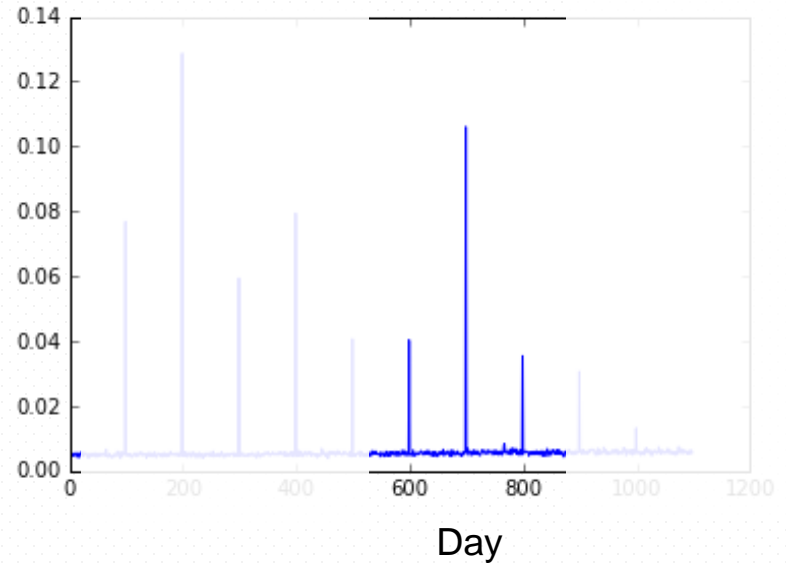
Injection and alternation of 2nd order dependencies

Higher-order anomalies captured by HON

First-order network



HON

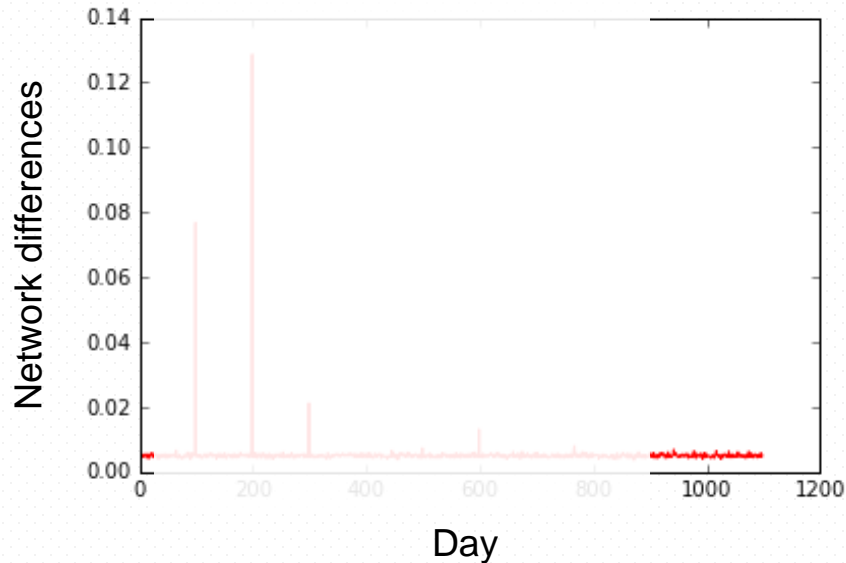


Injection and alternation of 3rd order dependencies

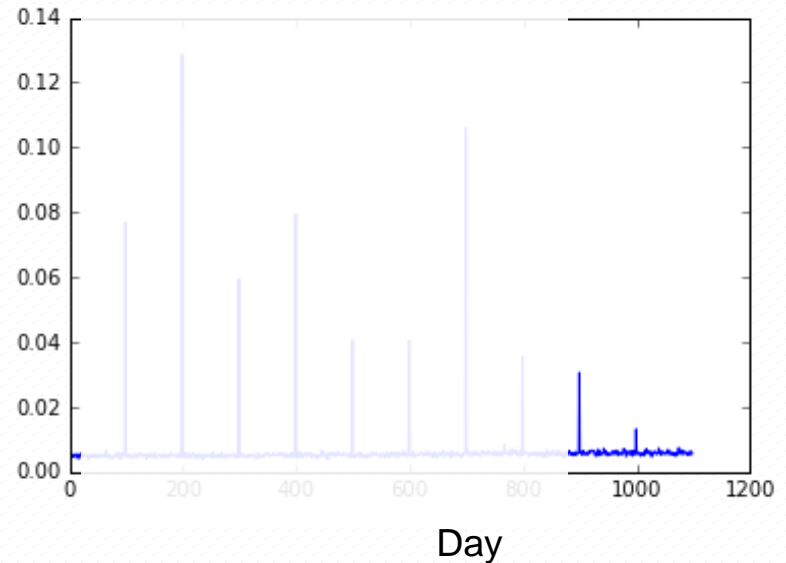
Higher-order anomalies captured by HON

Fails to capture certain anomalies

First-order network



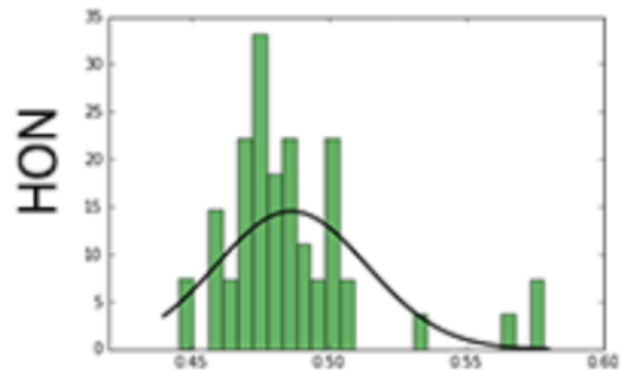
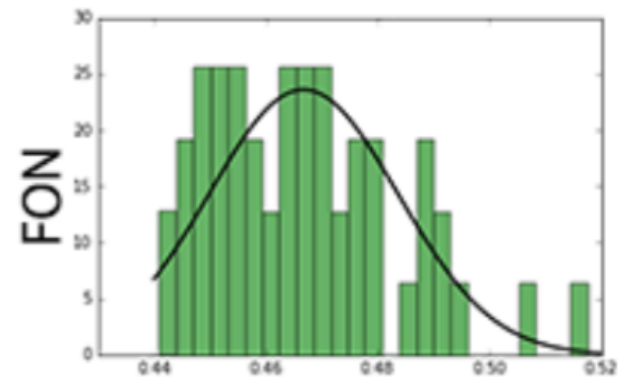
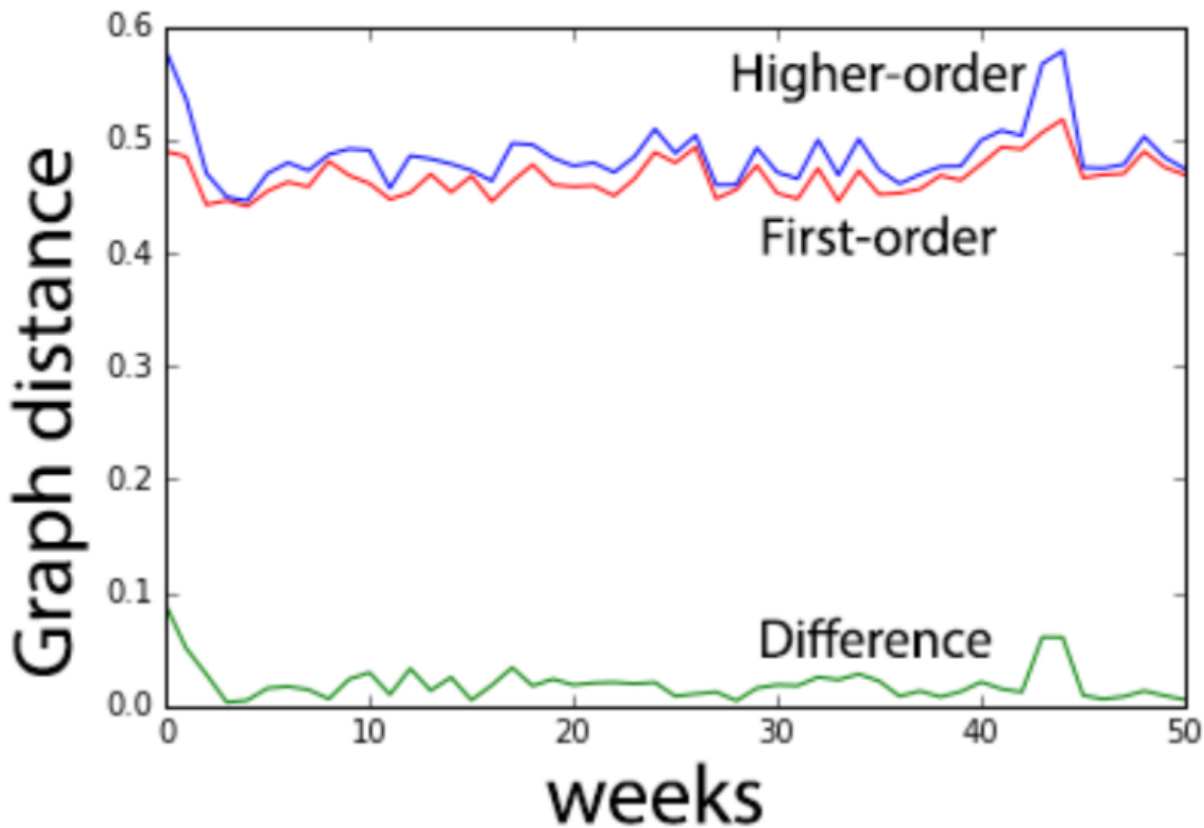
HON



Injection and alternation of higher-order dependencies

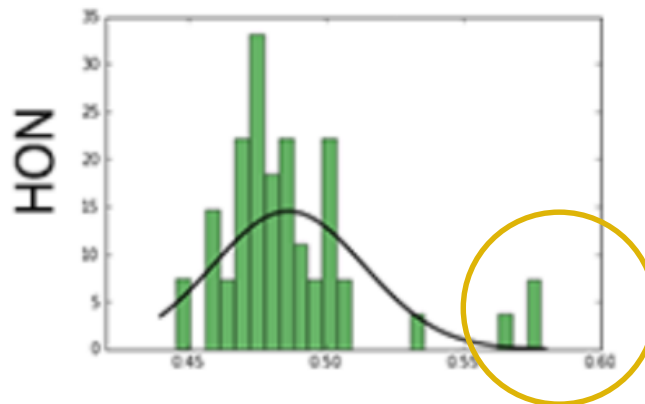
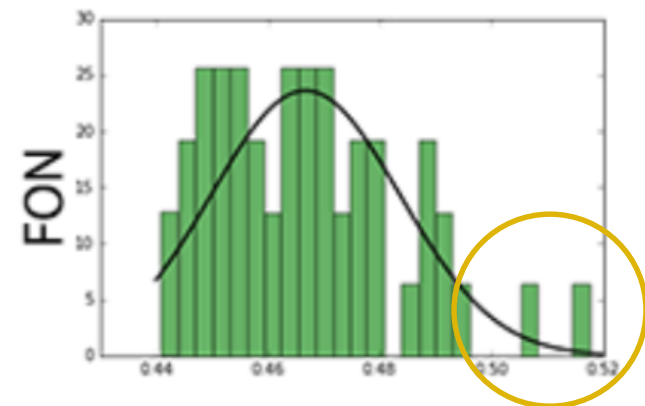
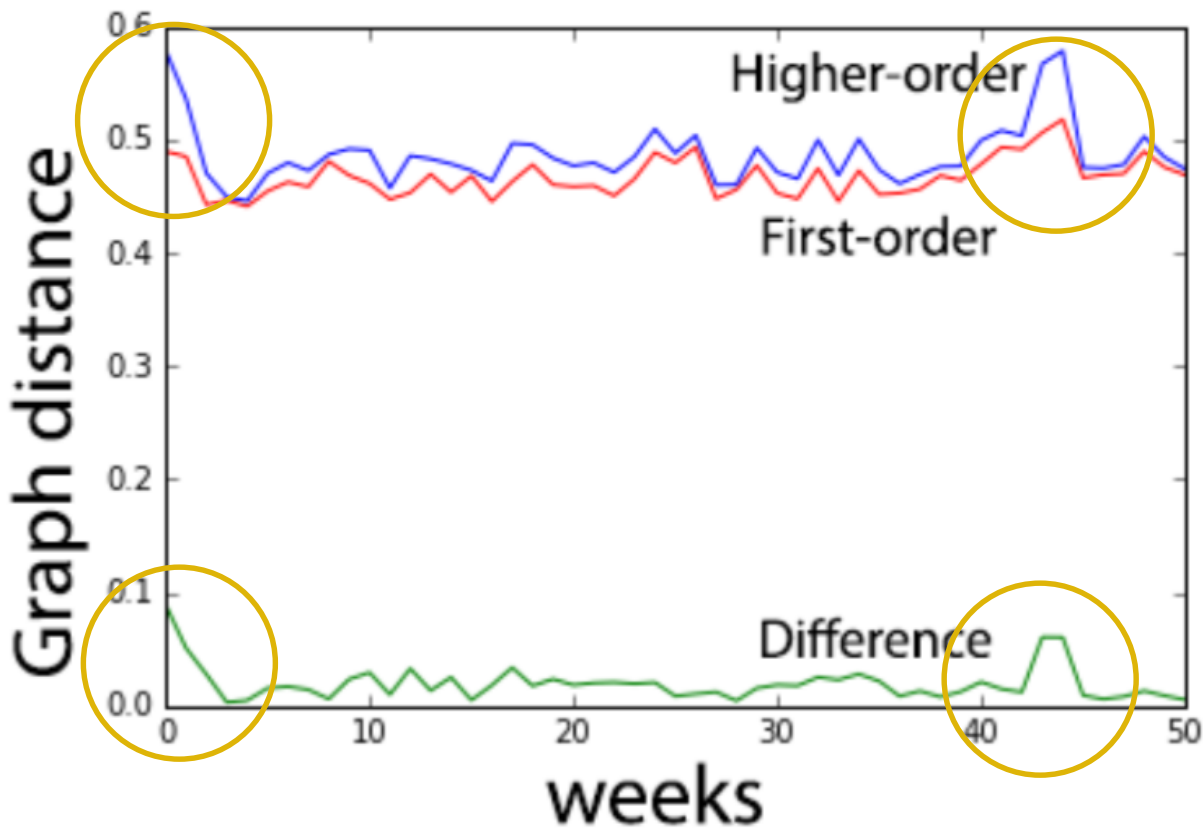
Higher-order anomalies captured by HON

Porto Taxi GPS trajectory data, 1 year



Higher-order anomalies captured by HON

Amplifying anomalous signals



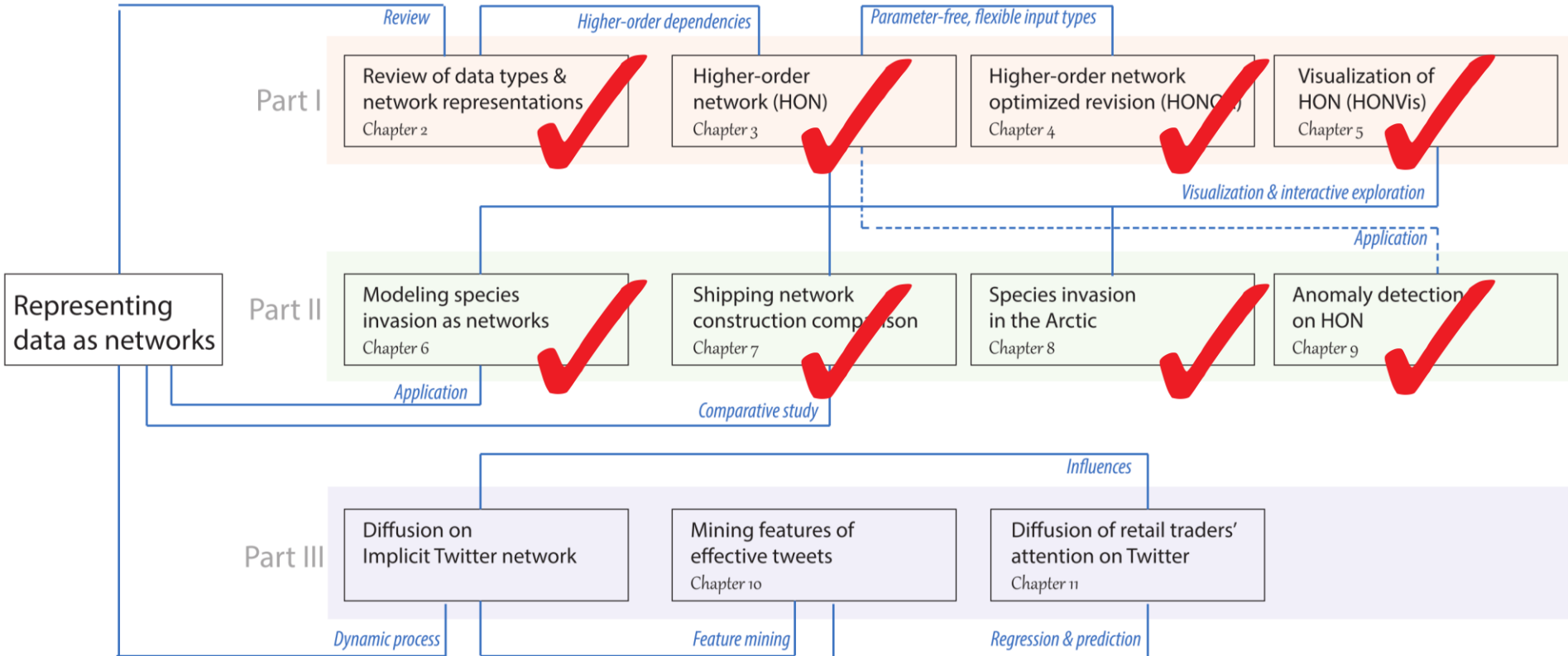
Takeaways

Anomaly detection on dynamic HON

Unveils higher-order anomalies that are otherwise ignored

Amplifies anomaly signals

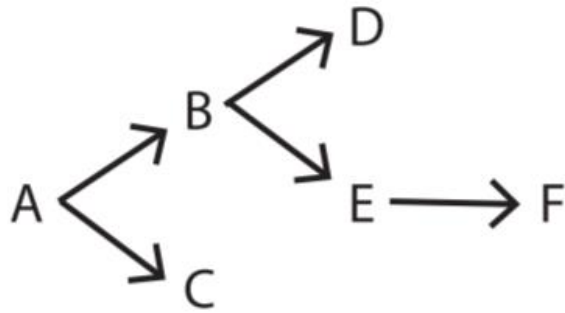
Overview



Discussions

Flexible inputs

Raw diffusion data

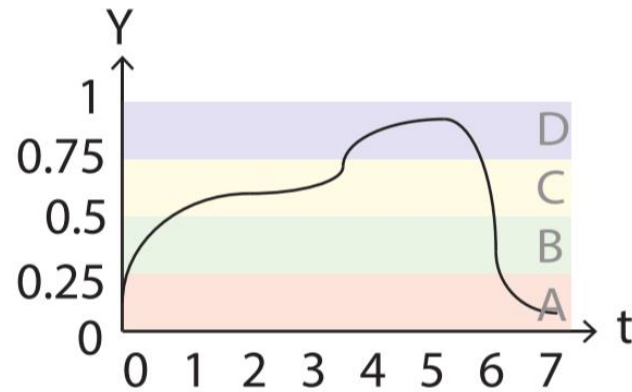


Observations

AB
AC
BD
BE
EF
ABD
ABE
BEF
ABEF

Flexible inputs

Raw time series data



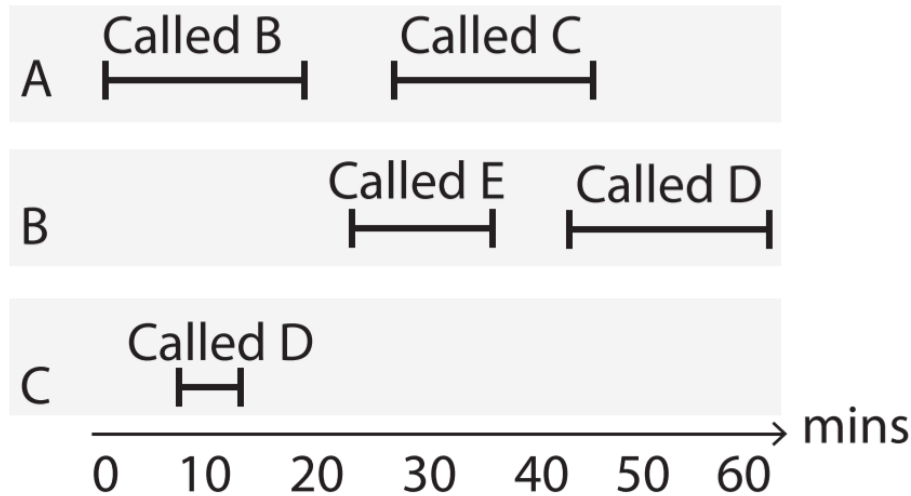
A C C C D D B A

Observations

AC
CD
DB
BA
ACD
CDB
DBA
ACDB
CDBA
ACDBA

Flexible inputs

Raw pairwise interaction
temporal data



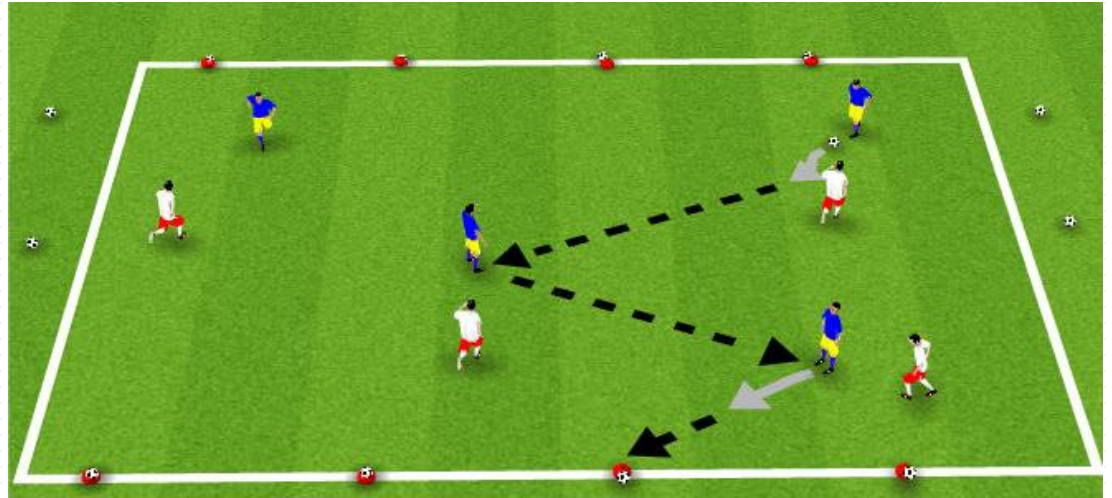
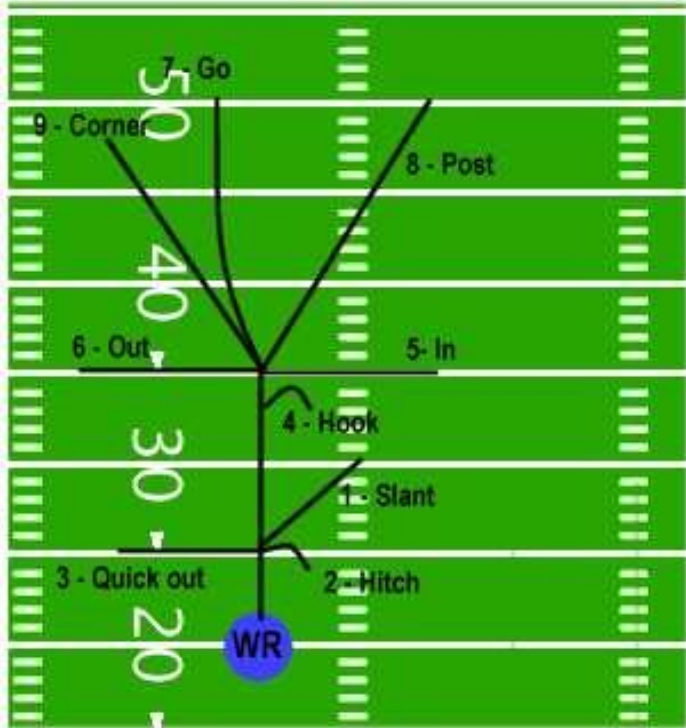
Observations

A B
A C
B E
B D
C D
C B
A B E

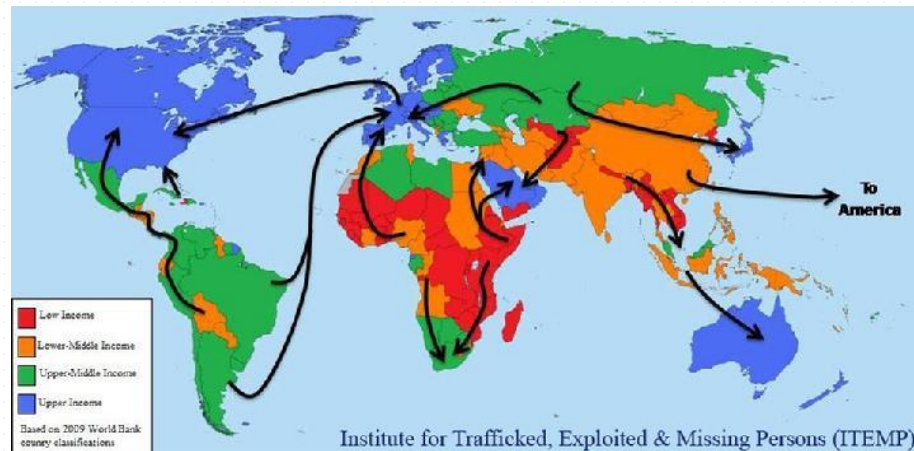
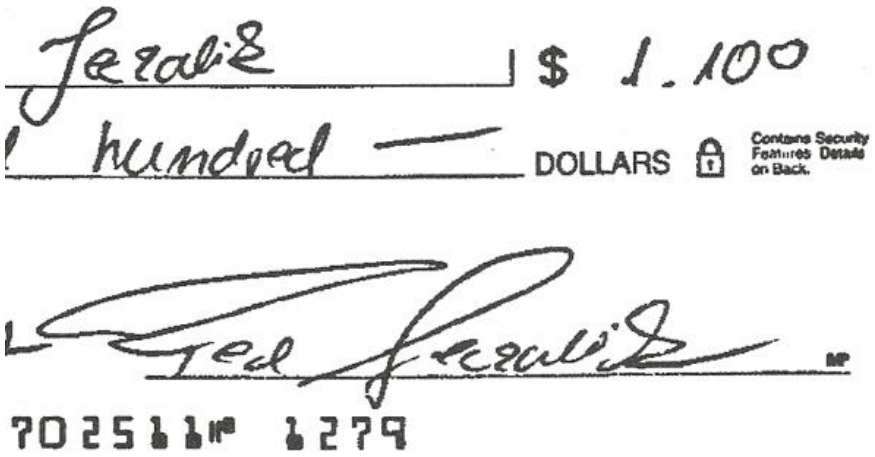
Varieties of data

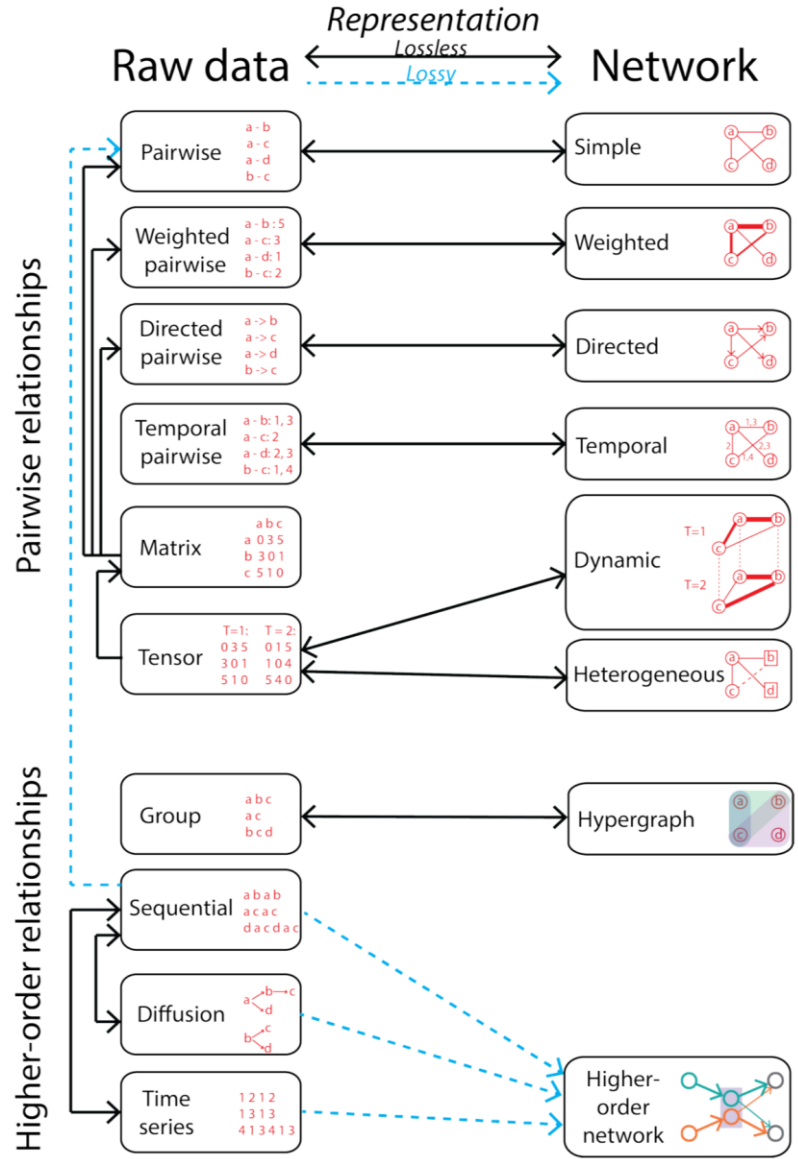
Application fields	Input Trajectories	Nodes	Edges
Transportation	Ship trajectories	Ports	Ship traffic
Computer network	Clickstreams	Web pages	Web traffic
Human interactions	Phone call or message cascades	People	Information flow
Human behavior	Human movements	POIs	Traffic
Healthcare	Patient records	Diseases	Disease evolutions
NLP	Sentences	Words	# word pairs

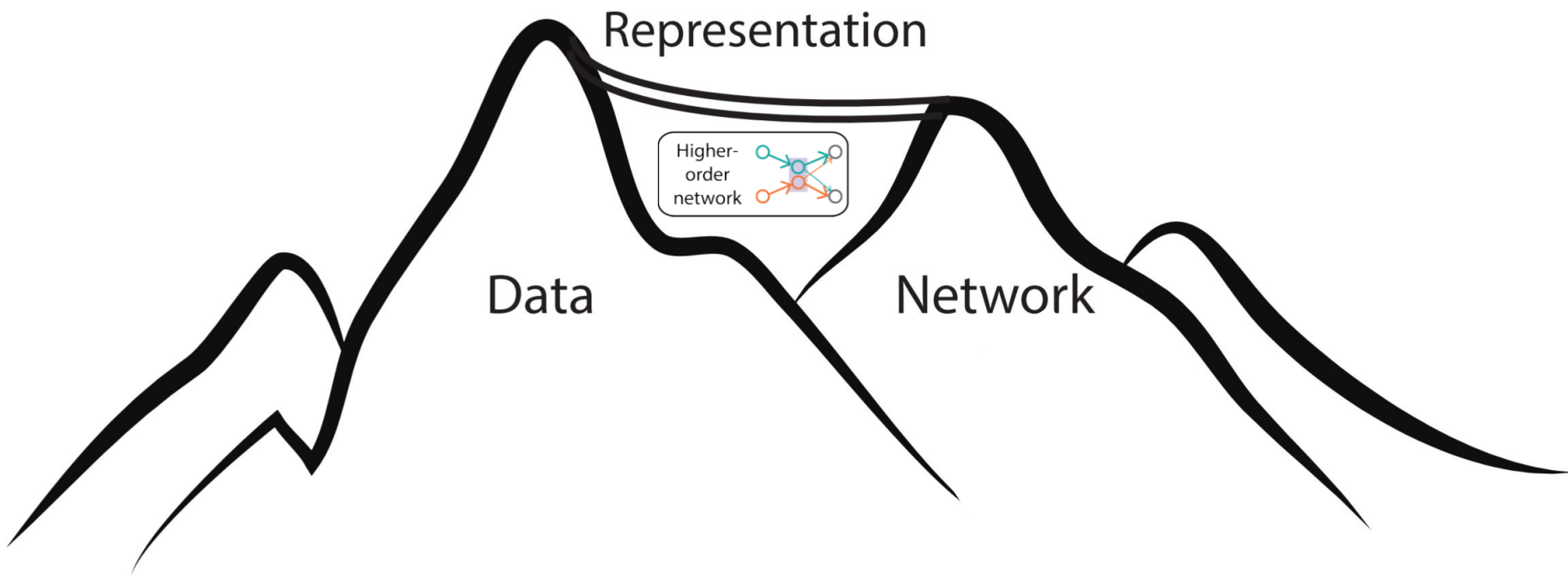
Other potential applications



Other potential applications







Research outputs

As leading student author:

- HON, published @ *Science advances*: **Jian Xu**, Thanuka L. Wickramaratne, and Nitesh V. Chawla. "Representing higher-order dependencies in networks." 2, no. 5 (2016): e1600028.
 - HoNVis, published @ *IEEE PacificVis*: Jun Tao, **Jian Xu**, Chaoli Wang, and Nitesh V. Chawla. "HoNVis: Visualizing and Exploring Higher-Order Networks."
 - HoNVis, demo published @ *IEEE IoTDI*: Jian Xu, Jun Tao, Nitesh V. Chawla and Chaoli Wang. "Visual Analytics of Higher-order Dependencies in Sensor Data"
 - Species invasions, published @ *ACM SIGKDD*: **Jian Xu**, Thanuka L. Wickramaratne, Nitesh V. Chawla, Erin K. Grey, Karsten Steinhaeuser, Reuben P. Keller, John M. Drake, and David M. Lodge. "Improving management of aquatic invasions by integrating shipping network, ecological, and environmental data: data mining for social good."
-
- Retail diffusion: under review @ *Journal of Management Science*: Nitesh Chawla, Zhi Da, **Jian Xu**, and Mao Ye. *Catching fire: the diffusion of retail attention on twitter*.
 - Effective tweeting: under review @ *ASONAM*: **Jian Xu**, Nitesh Chawla.
-
- Arctic species invasion: to submit to *Nature Communications*. Jian Xu, Salvatore Curasi, Erin Grey, Nitesh Chawla and David Lodge. "Species introduction and diffusion in the Arctic through global shipping: risk assessment and projection"
 - Anomaly detection with HON: to submit to *ICDM*. Jian Xu, Nitesh Chawla.

Research outputs

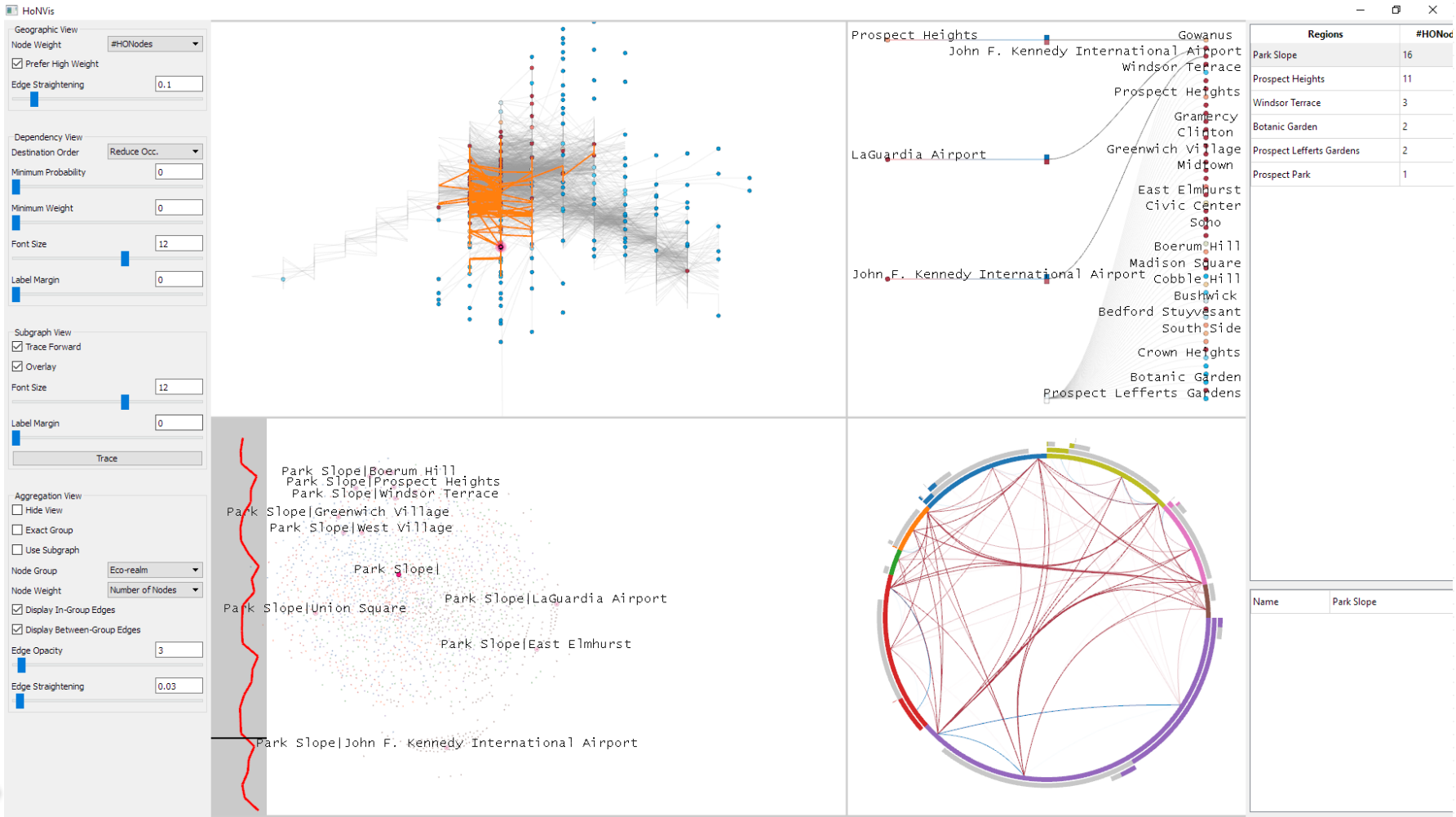
Other published collaborative work:

- Structural diversity, published @ *ACM SIGKDD*: Yuxiao Dong, Reid A. Johnson, **Jian Xu** and Nitesh V. Chawla. "Structural Diversity and Homophily: A Study Across More Than One Hundred Big Networks"
- Temporal motifs, published @ *IEEE Transaction on Systems, Man and Cybernetics*. Zhang, Yi-Qing, Xiang Li, **Jian Xu**, and Athanasios V. Vasilakos. "Human interactive patterns in temporal networks."

Other work in progress:

- HONVis extension: adding the time dimension, and the anomaly detection module.
- Comparative analysis of different network representations of global shipping.

HoNVis for dynamic HON & anomaly detection



For the community



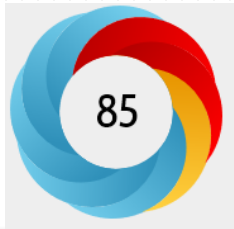
Overview Algorithm Applications Code Visualization
Paper Acknowledgement



Higher-order network

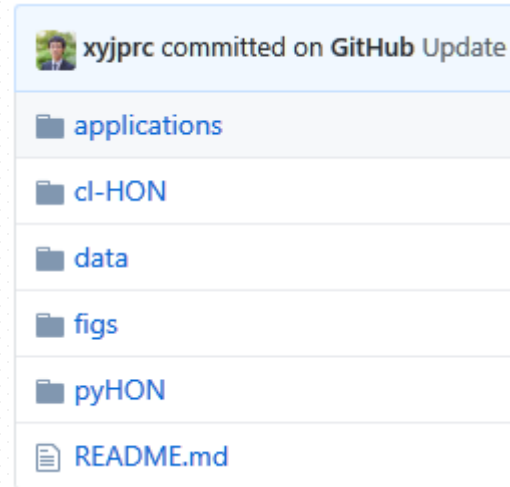
Capturing higher-order dependencies in big data

CLICK TO BEGIN



In the top 5% of all research outputs scored by Altmetric

High Attention Score compared to outputs of the same age (97th percentile)



Acknowledgements: committee

Prof. Nitesh Chawla, *chair*



Prof. David Lodge



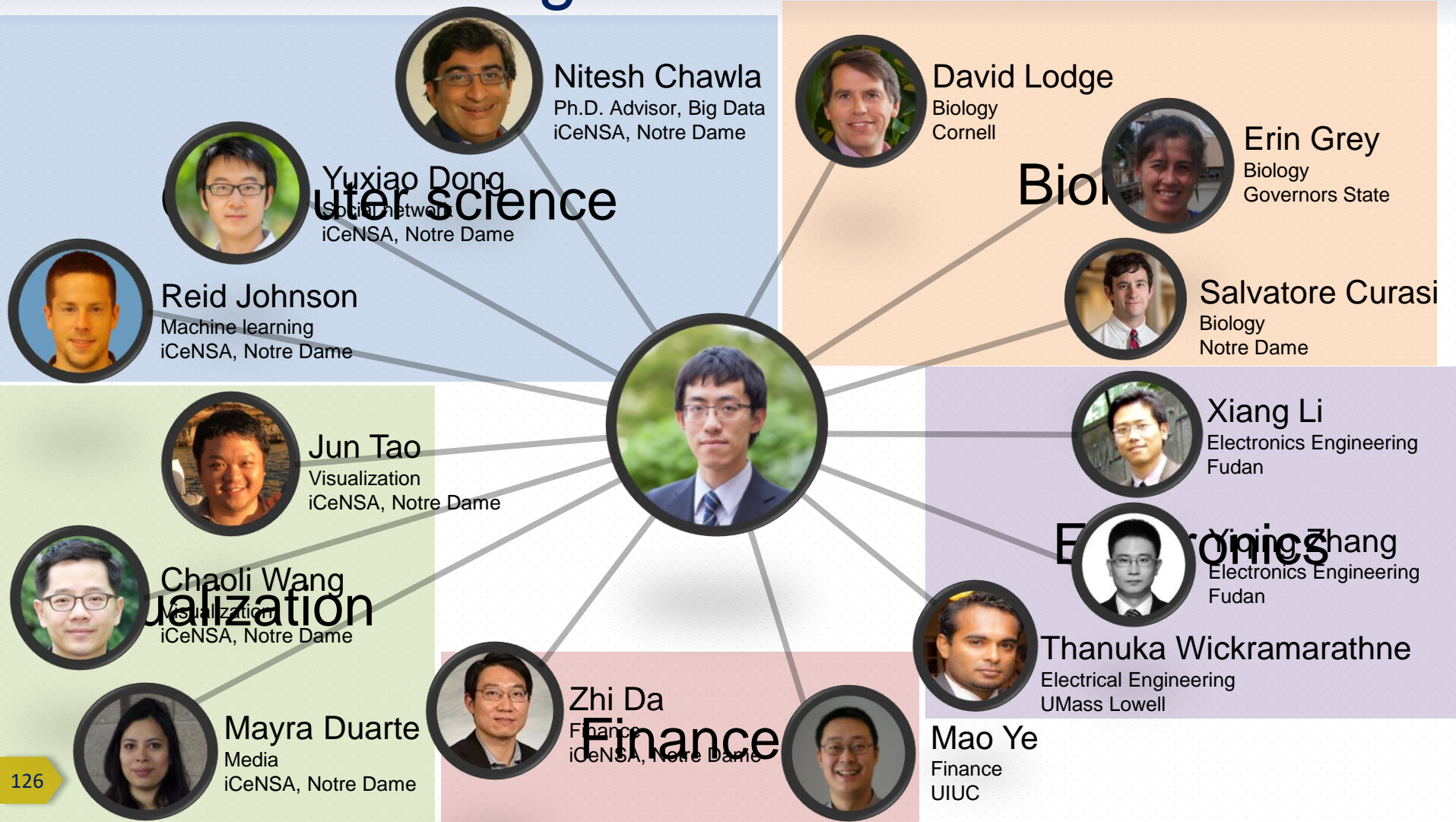
Prof. Tijana Milenkovic



Prof. Zoltan Torotzkai



Acknowledgements: collaborators



Acknowledgements: friends



Acknowledgements: Funding





Thank you!

Jian Xu



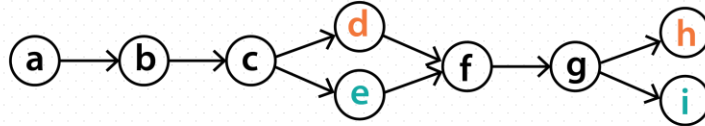
Appendix

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Comparison with VOM

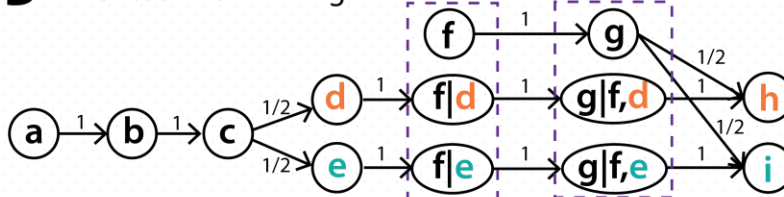
A True connections of ports



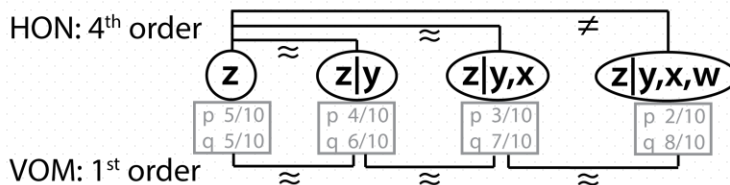
B Trajectories

Ship-1	a	b	c	d	f	g	h
Ship-2		b	c	d	f	g	h
Ship-3	a	b	c	e	f	g	i
Ship-4		b	c	e	f	g	i

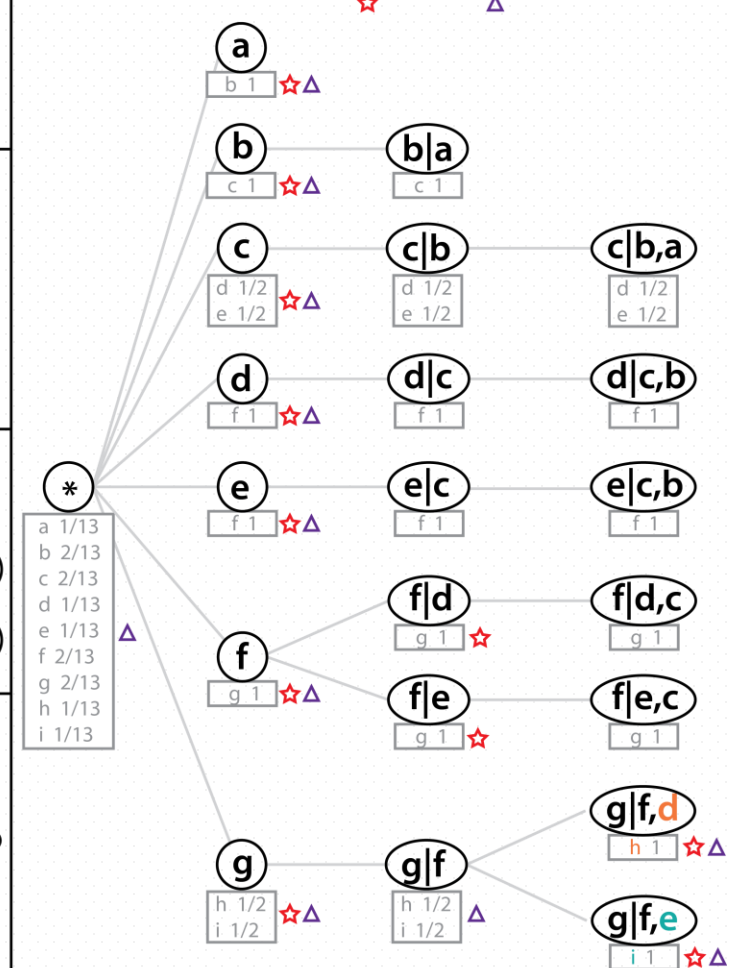
D Eventual HON wiring



E HON rule growing vs VOM pruning



C Rules extracted by HON and VOM





Higher-order network

Scalability

Scalability

Network representation (global shipping data)	Number of edges	Number of nodes	Network density	Clustering time (mins)	Ranking time (s)
Conventional first-order	31,028	2,675	4.3×10^{-3}	4	1.3
Fixed second-order	116,611	19,182	3.2×10^{-4}	73	7.7
HON, max order two	64,914	17,235	2.2×10^{-4}	45	4.8
HON, max order three	78,415	26,577	1.1×10^{-4}	63	6.2
HON, max order four	83,480	30,831	8.9×10^{-5}	67	7.0
HON, max order five	85,025	31,854	8.4×10^{-5}	68	7.6

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Scalability

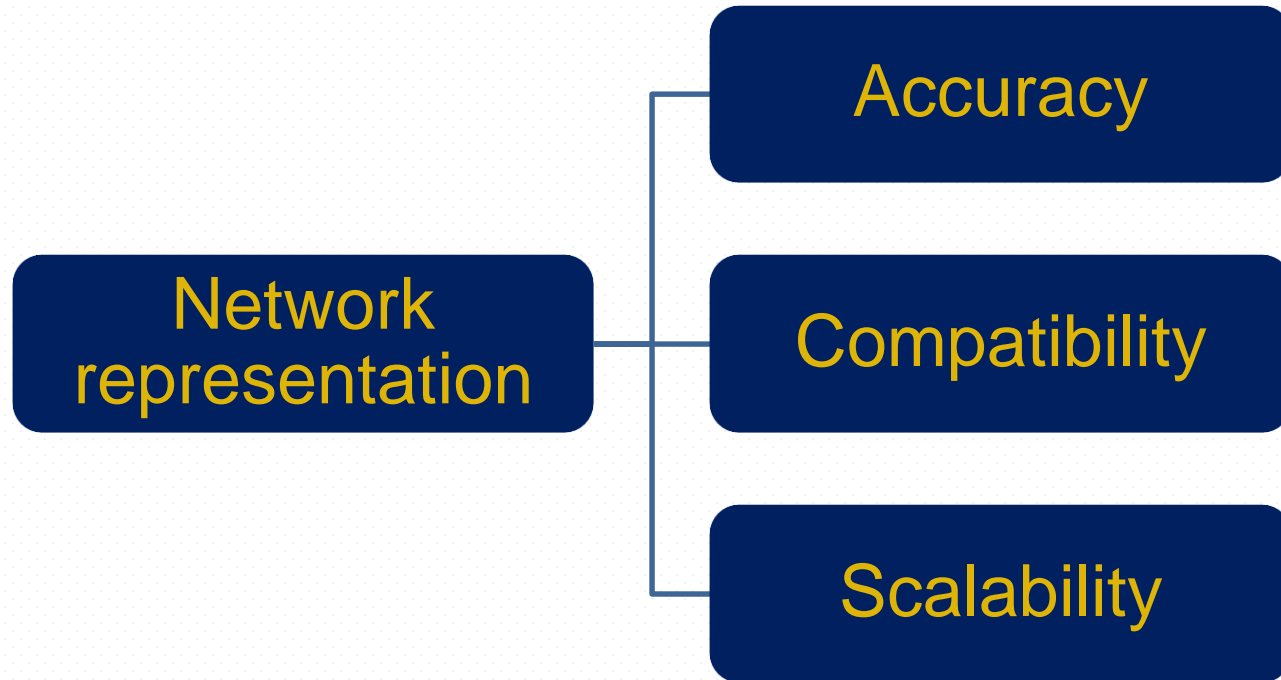
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HON, max order five	85,025	31,854	8.4×10^{-5}	68	7.6

* Using MapEquation with 1000 iterations

** Using PageRank

Goals

How shall we represent such big data derived from complex system as networks, and accurately capture higher-order dependencies?



Higher-order dependencies revealed by HON

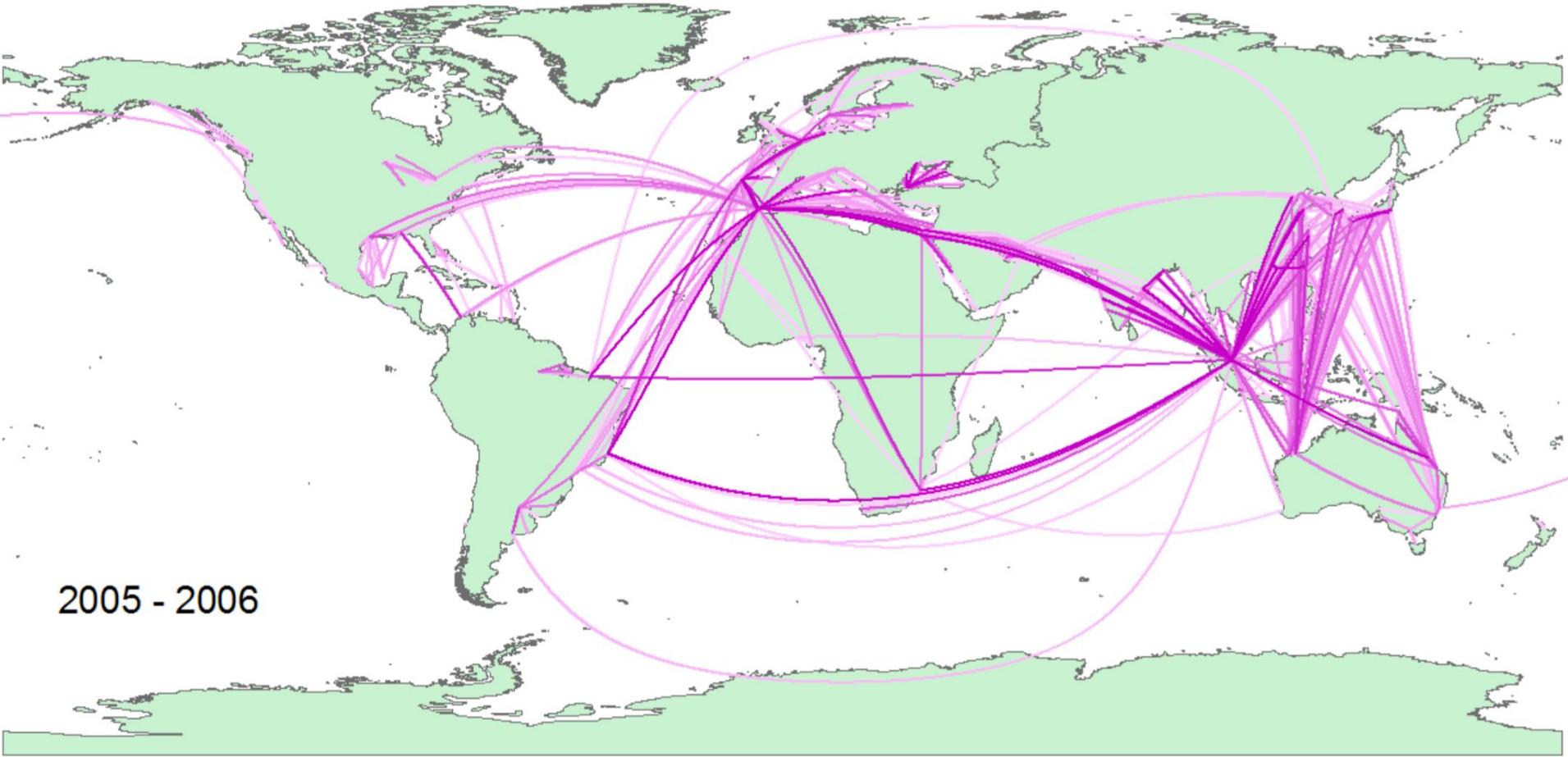
Data	# Records	Inject known variable-order dependencies
Synthetic	10,000,000	10 second-order 10 third-order 10 fourth-order

- **Effectiveness**: correctly captures all 30 of the higher-order dependencies
- **Accuracy**: does not extract false dependencies beyond the fourth order
- **Compactness**: determines that all other dependencies are first-order

Clustering: higher-order network

- 45% of ports belong to **more than one cluster**
- 44 ports (1.7% of all) belong to **five clusters**
 - New York, Shanghai, Hong Kong, Gibraltar, Hamburg, etc.
- Panama Canal belongs to **six clusters**
- Highlighting ports that may be invaded by species from multiple regions

Ship-borne species diffusion pathways



Ranking on clickstream network

Pages that gain PageRank scores	Δ PageRank	Pages that lose PageRank scores	Δ PageRank
South Bend Tribune - Home.	+0.0119	KTUU - Home.	-0.0057
Hagerstown News / obituaries - Front.	+0.0115	KWCH - Home.	-0.0031
South Bend Tribune - Obits - 3rd Party.	+0.0112	Imperial Valley Press - Home.	-0.0011
South Bend Tribune / sports / notredame - Front.	+0.0102	Hagerstown News / sports - Front.	-0.0005
Aberdeen News / news / obituaries - Front.	+0.0077	Imperial Valley Press / classifieds / topjobs - Front.	-0.0004
WDBJ7 - Home.	+0.0075	Gaylord - Home.	-0.0004
KY3 / weather - Front.	+0.0075	WDBJ7 / weather / web-cams - Front.	-0.0004
Hagerstown News - Home.	+0.0072	KTUU / about / meetnewsteam - Front.	-0.0003
Daily American / lifestyle / obituaries - Front.	+0.0054	Smithsburg man faces more charges following salvag	-0.0003
WDBJ7 / weather / closings - Front.	+0.0048	KWCH / about / station / newsteam - Front.	-0.0003
WSBT TV / weather - Front.	+0.0041	South Bend Tribune / sports / highschooolsports - Front.	-0.0003
Daily American - Home.	+0.0036	Hagerstown News / opinion - Front.	-0.0002
WDBJ7 / weather / radar - Front.	+0.0036	WDBJ7 / news / anchors-reporters - Front.	-0.0002
WDBJ7 / weather / 7-day-planner - Front.	+0.0031	Petoskey News / news / obituaries - Front.	-0.0002
WDBJ7 / weather - Front.	+0.0019	KWCH / news - Front.	-0.0002

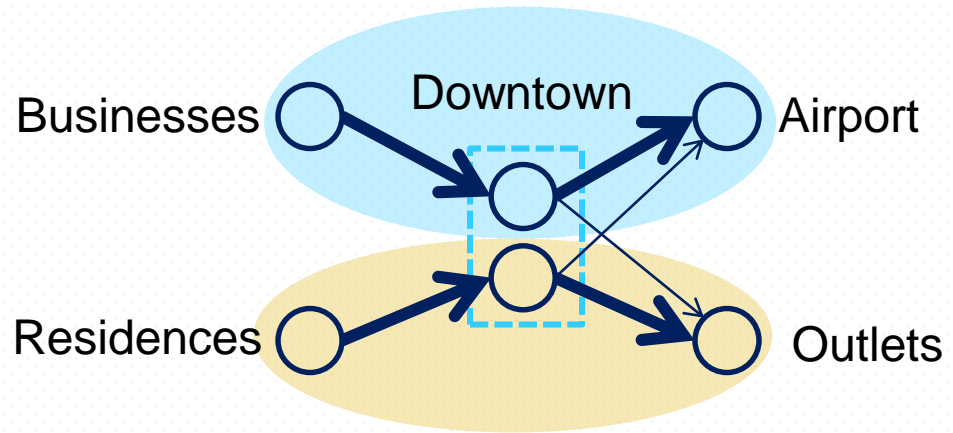
Ranking on clickstream network

Pages that gain PageRank scores	Δ PageRank	Pages that lose PageRank scores	Δ PageRank
South Bend Tribune - Home.	+0.0119	KTUU - Home.	-0.0057
Hagerstown News / obituaries - Front.	+0.0115	KWCH - Home.	-0.0031
South Bend Tribune - Obits - 3rd Party.	+0.0112	Imperial Valley Press - Home.	-0.0011
South Bend Tribune / sports / notredame - Front.	+0.0102	Hagerstown News / sports - Front.	-0.0005
Aberdeen News / news / obituaries - Front.	+0.0077	Imperial Valley Press / classifieds / topjobs - Front.	-0.0004
WDBJ7 - Home.	+0.0075	Gaylord - Home.	-0.0004
KY3 / weather - Front.	+0.0075	WDBJ7 / weather / web-cams - Front.	-0.0004
Hagerstown News - Home.	+0.0072	KTUU / about / meetnewsteam - Front.	-0.0003
Daily American / lifestyle / obituaries - Front.	+0.0054	Smithsburg man faces more charges following salvag	-0.0003
WDBJ7 / weather / closings - Front.	+0.0048	KWCH / about / station / newsteam - Front.	-0.0003
WSBT TV / weather - Front.	+0.0041	South Bend Tribune / sports / highschooolsports - Front.	-0.0003
Daily American - Home.	+0.0036	Hagerstown News / opinion - Front.	-0.0002
WDBJ7 / weather / radar - Front.	+0.0036	WDBJ7 / news / anchors-reporters - Front.	-0.0002
WDBJ7 / weather / 7-day-planner - Front.	+0.0031	Petoskey News / news / obituaries - Front.	-0.0002
WDBJ7 / weather - Front.	+0.0019	KWCH / news - Front.	-0.0002

**No changes
to the ranking algorithm**

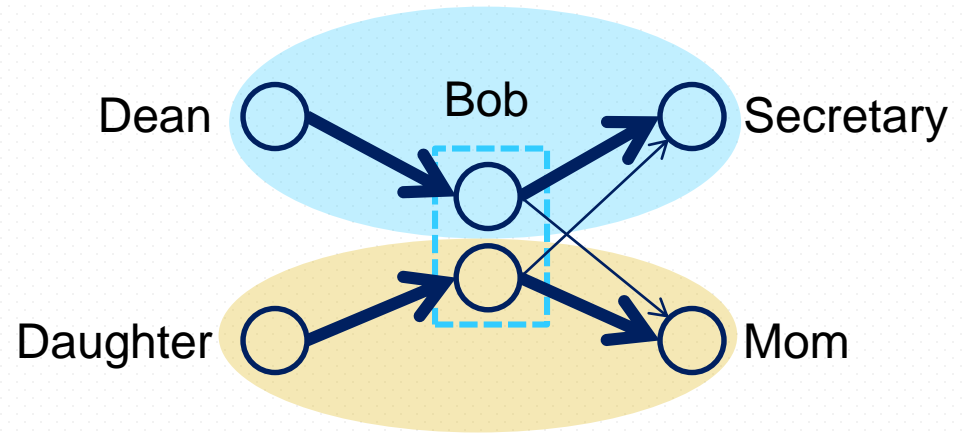
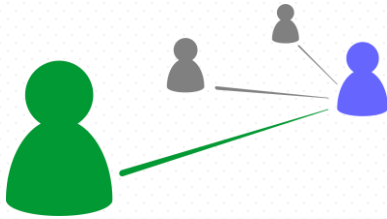
Interdisciplinary applications

Urban planning
&
Event detection



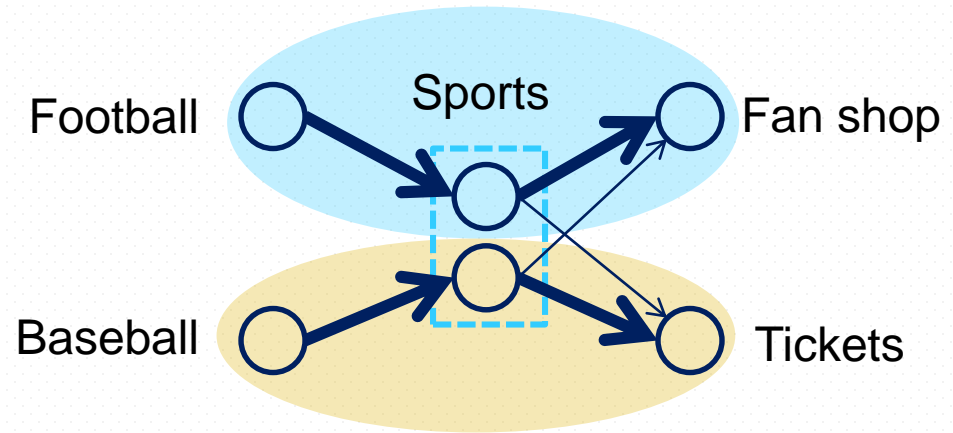
Interdisciplinary applications

Social network & Information diffusion



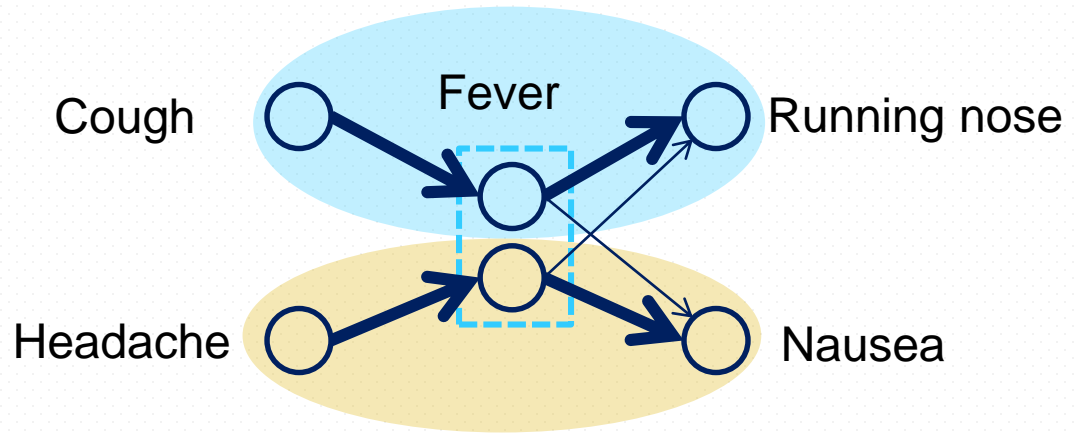
Interdisciplinary applications

Web optimization,
advertising,
network security

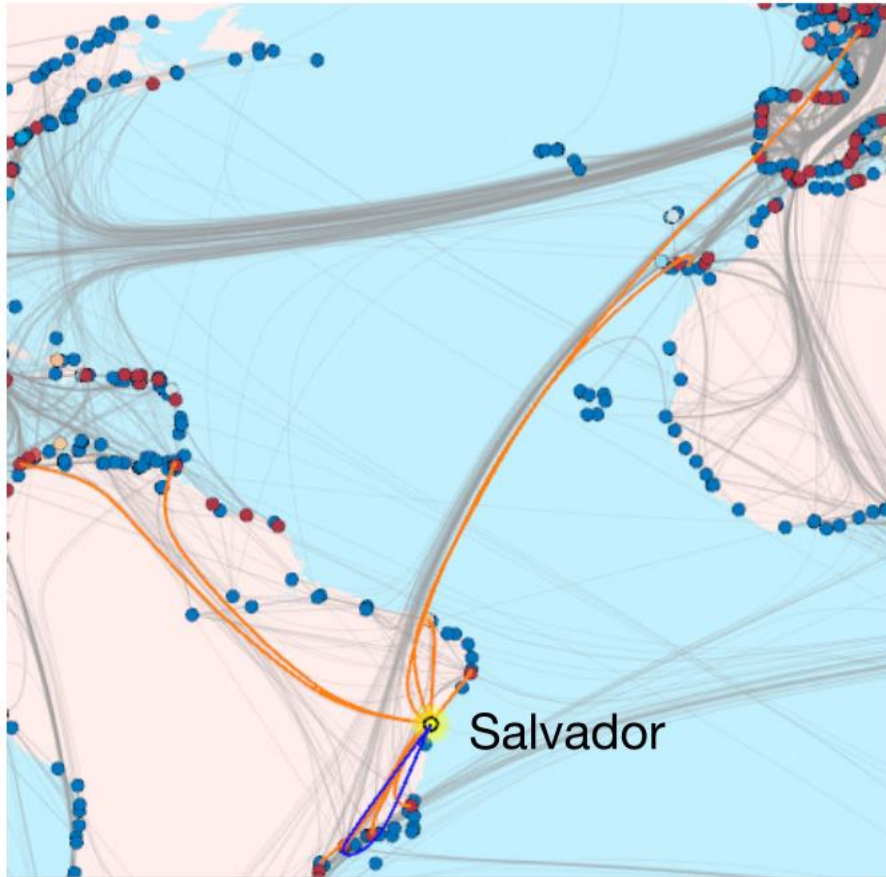


Interdisciplinary applications

Healthcare,
Epidemics monitoring,
Gene tech

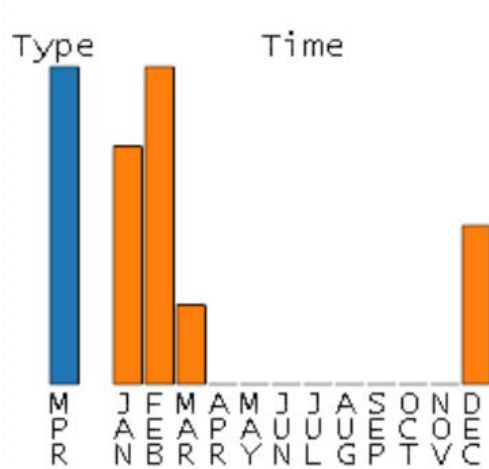


Explore geographically & rank by features

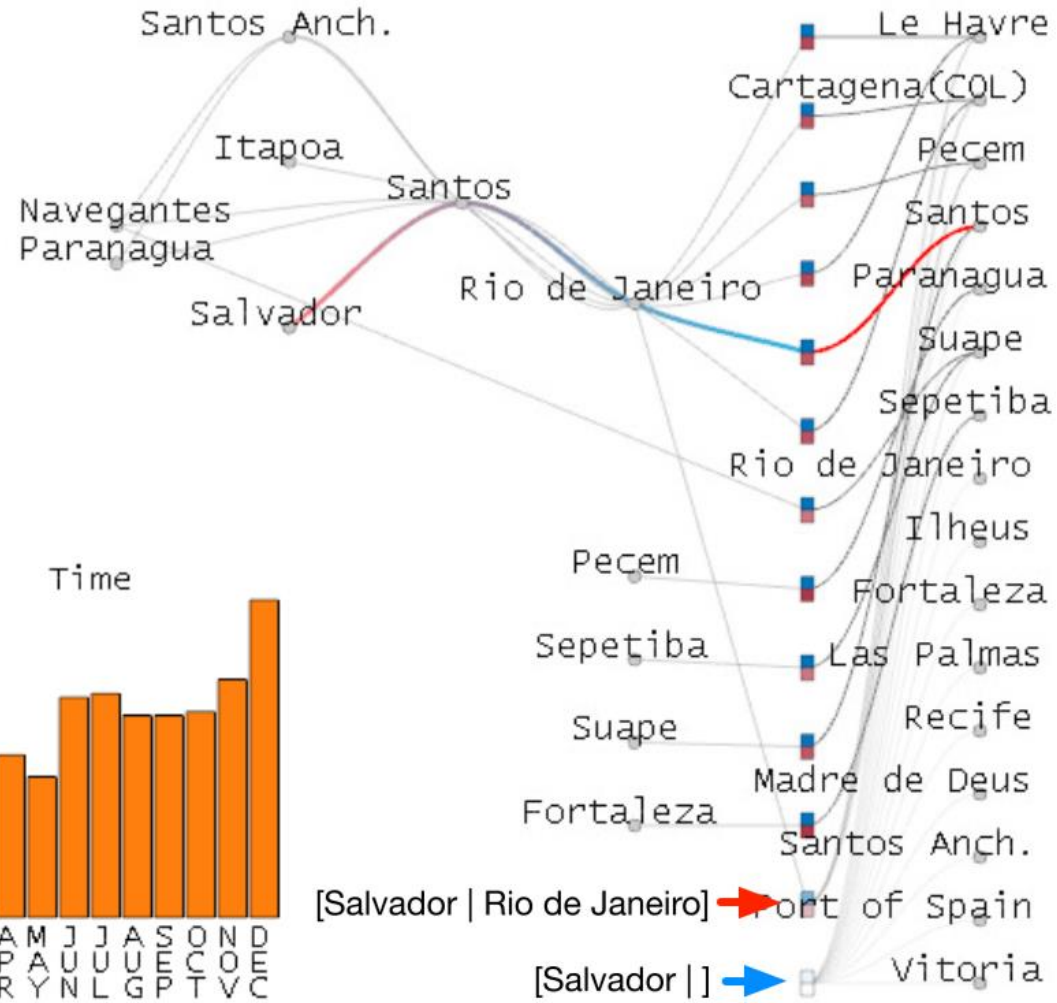
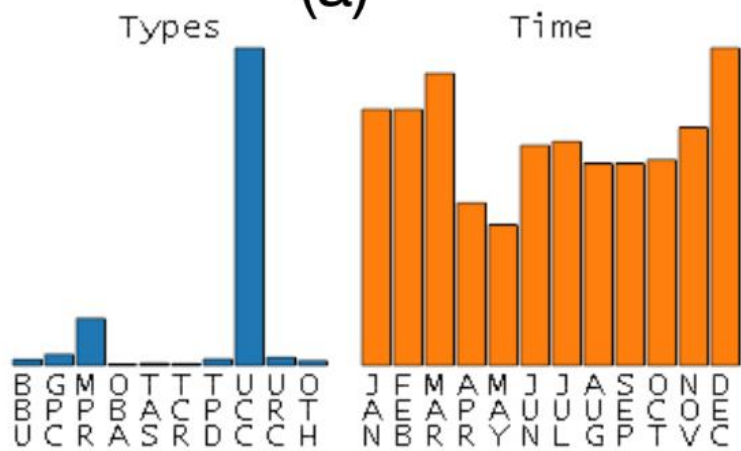


Ports	#HO Nodes
Suape	19
Vitoria	19
Salvador	13
Tubarao	6
Praia Mole	5
Portocel	2
Ponta do Ubu	2
Aratu	2
Recife	2
Madre de Deus	1
Cabedelo	1
Ilheus	1
Maceio	1
Jubarte Field	1

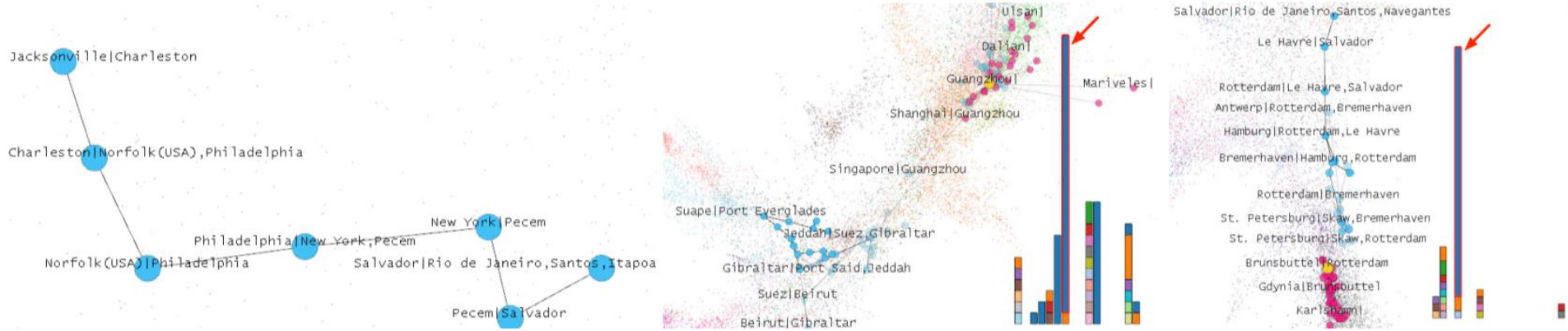
View dependencies & underlying metadata



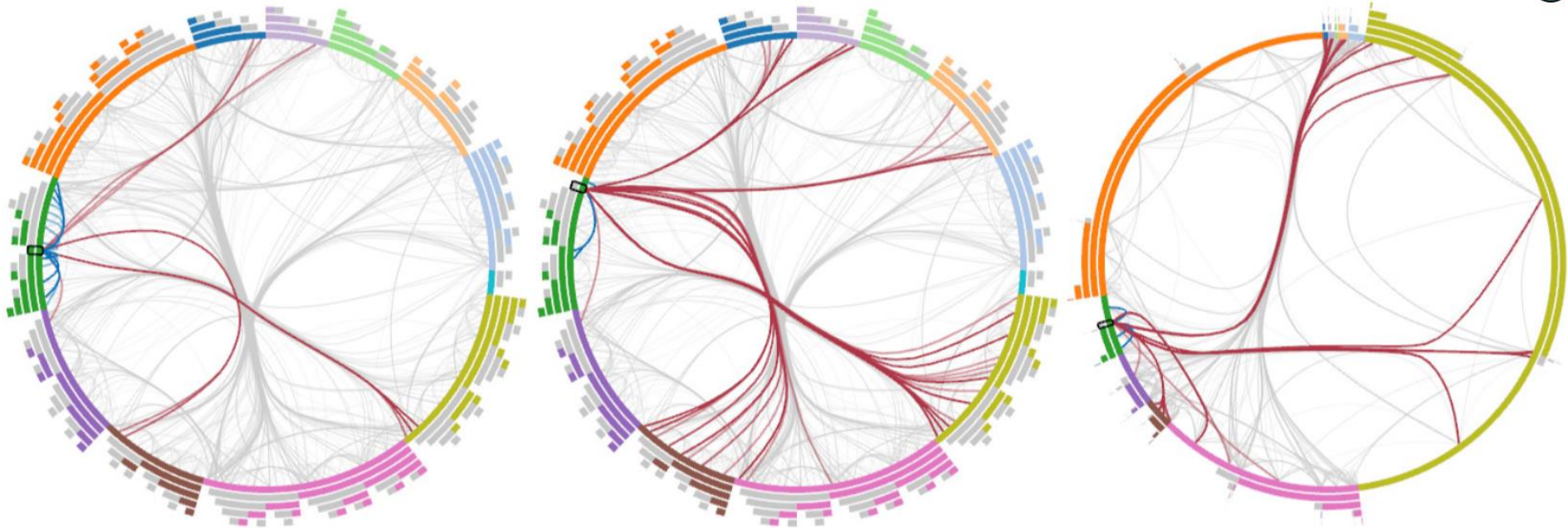
(a)



Track diffusion on the network



Aggregate at different granularities



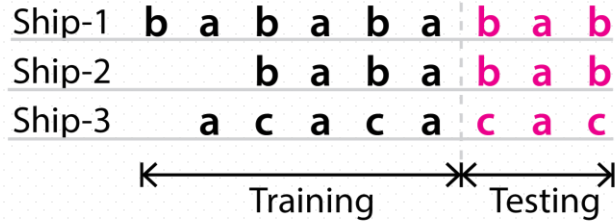
Clustering

- *Walktrap*: “Random walks on a graph tend to get ‘trapped’ into densely connected parts corresponding to communities.” (Pons & Latapy 2006)

Ranking

- *PageRank*: “The simplified version corresponds to the standing probability distribution of a random walk on the graph of the Web.” (Page et al. 1999)

Influence on dynamics



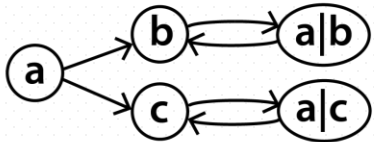
First-order network



b	a	b	✓
b	a	c	✗
c	a	b	✗

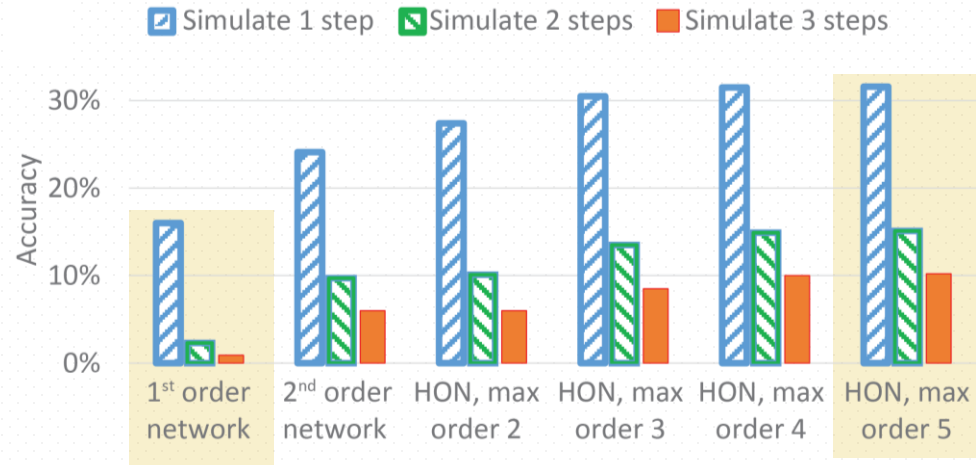
Prediction 1/3 correct

HON



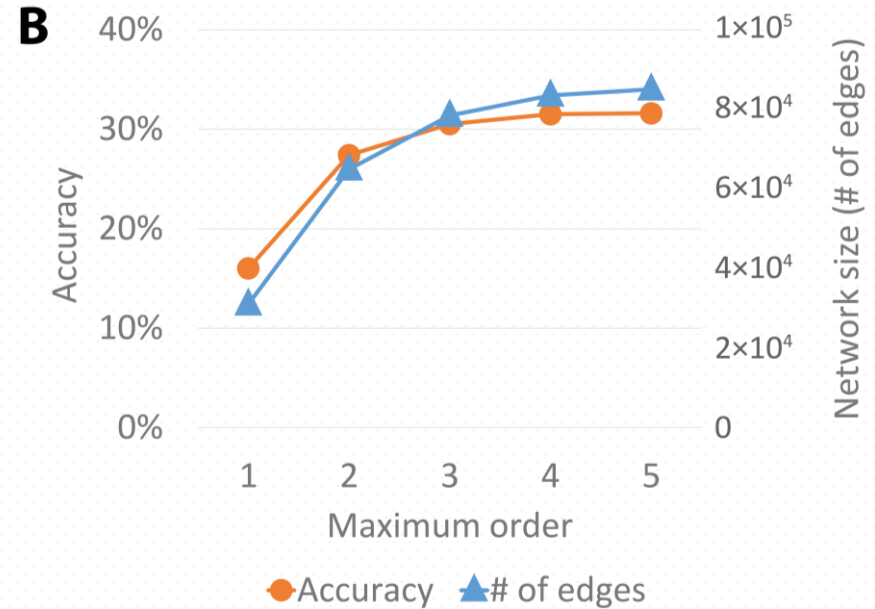
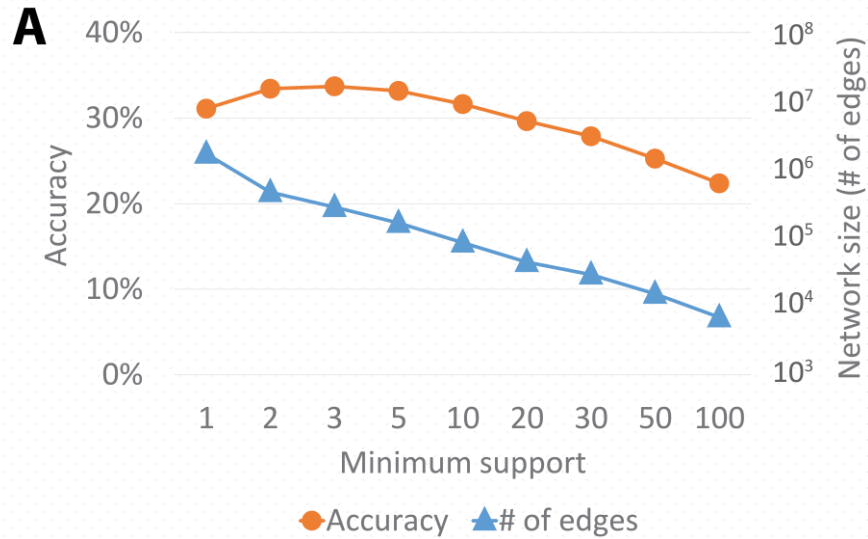
b	a	b	✓
b	a	b	✓
c	a	c	✓

Prediction 3/3 correct



Network representation	Number of edges	Number of nodes	Network density	Prob. of returning after two steps	Prob. of returning after three steps	Entropy rate (bits)	Clustering time (mins)	Ranking time (s)
Conventional first-order	31,028	2,675	4.3×10^{-3}	10.7%	1.5%	3.44	4	1.3
Fixed second-order	116,611	19,182	3.2×10^{-4}	42.8%	8.0%	1.45	73	7.7
HON, max order two	64,914	17,235	2.2×10^{-4}	41.7%	7.3%	1.46	45	4.8
HON, max order three	78,415	26,577	1.1×10^{-4}	45.9%	16.4%	0.90	63	6.2
HON, max order four	83,480	30,631	8.9×10^{-5}	48.9%	18.5%	0.68	67	7.0
HON, max order five	85,025	31,854	8.4×10^{-5}	49.3%	19.2%	0.63	68	7.6

Parameter sensitivity



Comparison with VOM

	HON	VOM	In HON but not in VOM	In VOM but not in HON
0 th order	0	3,029	0	3029
1 st order	31,028	31,028	0	0
2 nd order	32,960	35,288	427	2,755
3 rd order	15,642	21,536	550	6,444
4 th order	4,632	8,973	302	4,643
5 th order	763	2,084	23	1,344
Total	85,025	101,938	1,302	18,215

- **Global shipping data.** This data made available by Lloyd's Maritime Intelligence Unit (LMIU) contains ship movement information such as vessel_id, port_id, sail_date and arrival_date. Our experiments are based on a recent LMIU data set that spans one year from May 1st, 2012 to April 30th, 2013, totaling 3,415,577 individual voyages corresponding to 65,591 ships that move among 4,108 ports and regions globally. A minimum support of 10 is used to filter out noise in the data.
- **Clickstream data.** This data made available by a media company contains logs of users clicking through web pages that belong to 50 news web sites owned by the company. Fields of interest include user_ip, pagename and time. Our experiments are based on the clickstream records that span two months from December 4th, 2012 to February 3rd, 2013, totaling 3,047,697 page views made by 179,178 distinct IP addresses on 45,257 web pages. A minimum support of 5 is used to filter out noise in the data. Clickstreams that are likely to be created by crawlers (abnormally long clickstreams / clickstreams that frequently hit the error page) are omitted.
- **Retweet data.** This data (50) records retweet history on Weibo (a Chinese microblogging website), with information about who retweets whose messages at what time. The data was crawled in 2012 and there are 23,755,810 retweets recorded, involving 1,776,950 users.

Synthetic data. We created a trajectory data set (data and code are available at <https://github.com/xyjprc/hon>) with known higher-order dependencies to verify the effectiveness of the rule extraction algorithm. In the context of shipping, we connect 100 ports as a 10×10 grid, then generate trajectories of 100,000 ships moving among these ports. Each ship moves 100 steps, yielding 10,000,000 movements in total. Normally each ship has equal probabilities of going up/down/left/right on the grid in each step (with wrapping, e.g., going down at the bottom row will end up in the top row); we use additional higher-order rules to control the generation of ship movements. For example, a second-order rule can be defined as whenever a ship comes from Shanghai to Singapore, instead of randomly picking a neighboring port of Singapore for the next step, the ship has 70% chance of going to Los Angeles and 30% chance of going to Seattle. We predefine 10 second-order rules like this, and similarly 10 third-order rules, 10 fourth-order rules, and no other higher-order rules, so that movements that have variable orders of dependencies are generated. To test the rule extraction algorithm, we set the maximum order as five to see if the algorithm will incorrectly extract false rules beyond the fourth order which we did not define; we set minimum support as five for patterns to be considered as rules.



Higher-order network

Algorithm

How can we tell if this network representation more accurately captures the pattern in raw data?

Raw data

Rule
extraction

Network
wiring

HON

A

- Convert all first-order rules into edges



Raw data

Rule
extraction

Network
wiring

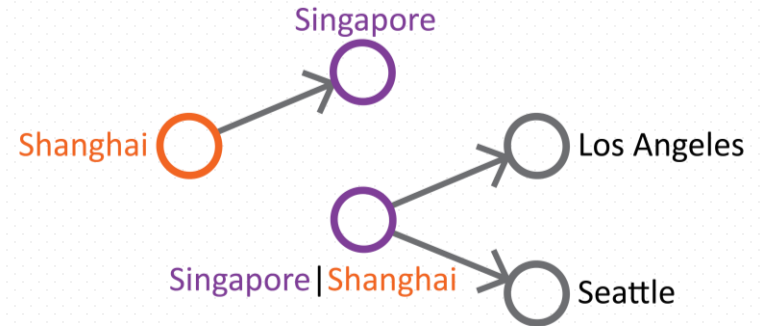
HON

A

- Convert all first-order rules into edges

B

- Convert higher-order rules
- Add higher-order nodes when necessary



Raw data

Rule
extraction

Network
wiring

HON

A

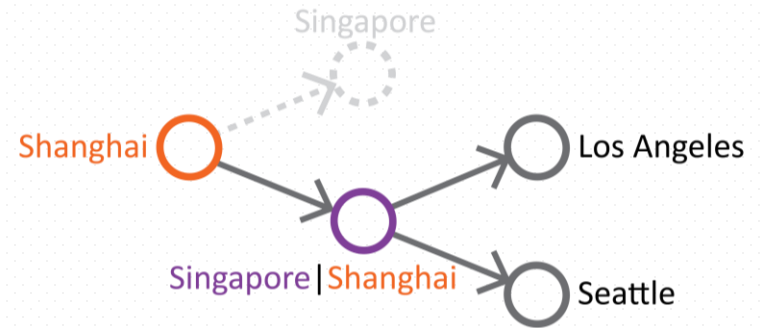
- Convert all first-order rules into edges

B

- Convert higher-order rules
- Add higher-order nodes when necessary

C

- Rewire edges
- The edge weights are preserved



Raw data

Rule
extraction

Network
wiring

HON

A

- Convert all first-order rules into edges

B

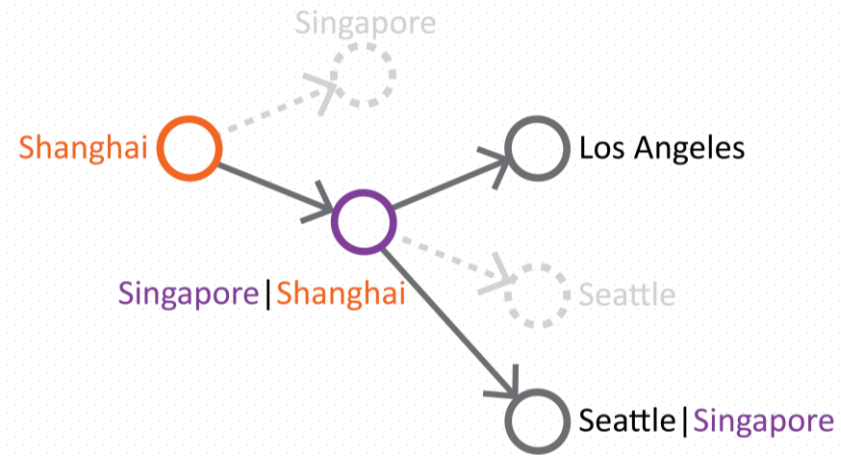
- Convert higher-order rules
- Add higher-order nodes when necessary

C

- Rewire edges
- The edge weights are preserved

D

- Rewire remaining edges





Higher-order network

Effectiveness

Higher-order dependencies revealed by HON

Data	# Records	Dependencies revealed	Similar observations
Ship movement	3,415,577	Up to 5 th order	N/A
Clickstream	3,047,697	Up to 3 rd order	<i>"... appear to saturate at $k = 3$ for Yahoo... browsing behavior across websites is definitely not Markovian but can be captured reasonably well by a not-too-high order Markov chain."</i> --- Chierichetti et al. (2012)
Retweet	23,755,810	N/A	Assuming the second order has <i>"marginal consequences for disease spreading"</i> --- Rosvall et al. (2014)

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Existing approaches



Ignore
higher-orders

Inaccurate



Modify
existing
algorithms

Cannot generalize

Existing approaches



Ignore
higher-orders

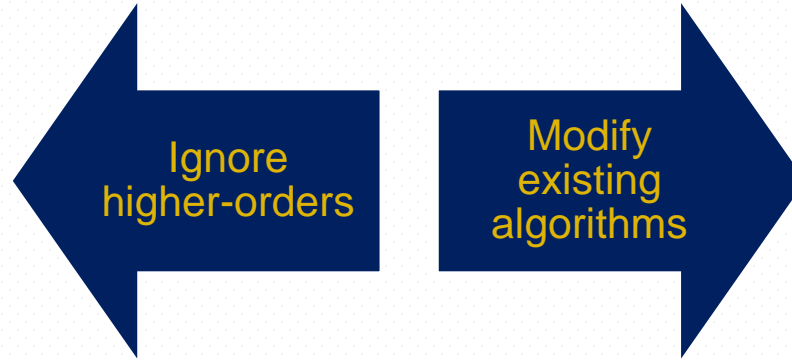
Inaccurate



Modify
existing
algorithms

Cannot generalize

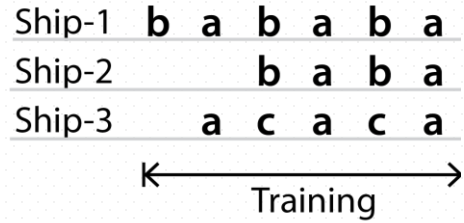
Existing approaches



Higher-order network

- ✓ Accurate representation
- ✓ Generalizes to existing algorithms

Influence on dynamics



Influence on dynamics

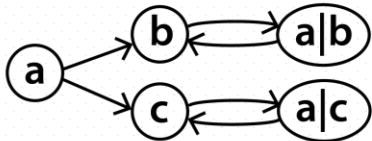
Ship-1 b a b a b a
Ship-2 b a b a
Ship-3 a c a c a

← Training →

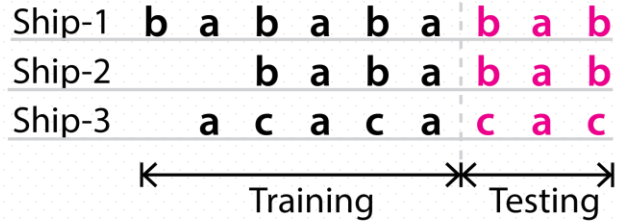
First-order network



HON



Influence on dynamics



Influence on dynamics

Ship-1 **b a b a b a** | **b a b**
Ship-2 **b a b a** | **b a b**
Ship-3 **a c a c a** | **c a c**

← Training | Testing →

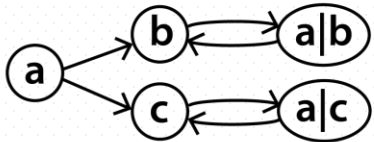
First-order network



b a b ✓
b a c ✗
c a b ✗

← Prediction →
Prediction 1/3 correct

HON



b a b ✓
b a b ✓
c a c ✓

← Prediction →
Prediction 3/3 correct

Influence on dynamics

Ship-1 **b a b a b a** | **b a b**
 Ship-2 **b a b a** | **b a b**
 Ship-3 **a c a c a** | **c a c**

← Training | Testing →

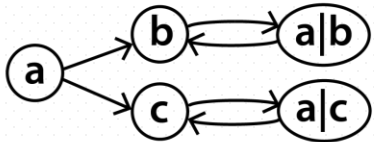
First-order network



b a b ✓
b a c ✗
c a b ✗

← Prediction →
 1/3 correct

HON



b a b ✓
b a b ✓
c a c ✓

← Prediction →
 3/3 correct



Influence on dynamics

Ship-1	b	a	b	a	b	a	b	a	b
Ship-2			b	a	b	a	b	a	b
Ship-3		a	c	a	c	a	c	a	c

← Training | Testing →

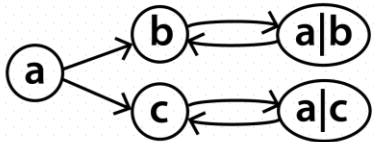
First-order network



b	a	b	✓
b	a	c	✗
c	a	b	✗

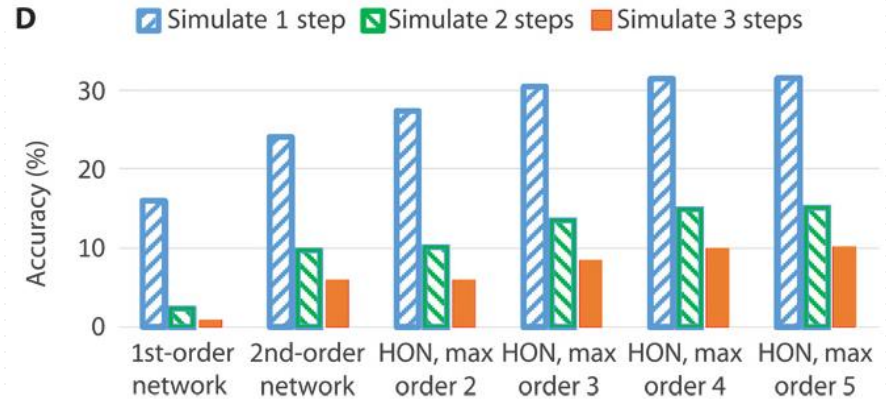
Prediction 1/3 correct

HON



b	a	b	✓
b	a	b	✓
c	a	c	✓

Prediction 3/3 correct



**Higher accuracy
in simulating real movements**



Higher-order network

Application: ranking

Web page access behaviors for server optimization and advertising

Ranking on clickstream network

User 1 WDBJ7 home → View photo → WDBJ7 home → ...

User 2 WDBJ7 home → View photo → Upload photo → ...

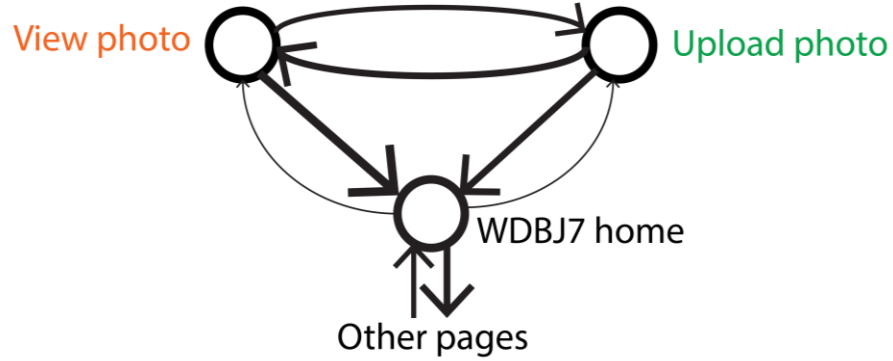
User 3 View photo → Upload photo → View photo → ...

User 4 WDBJ7 home → Upload photo → WDBJ7 home → ...

... ..

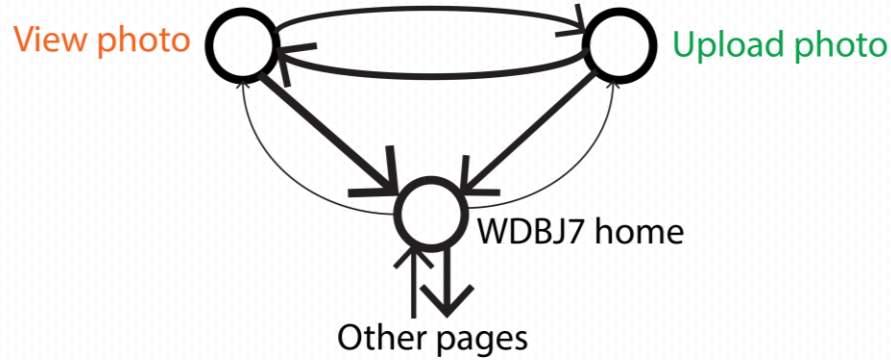
Ranking on clickstream network

First-order network

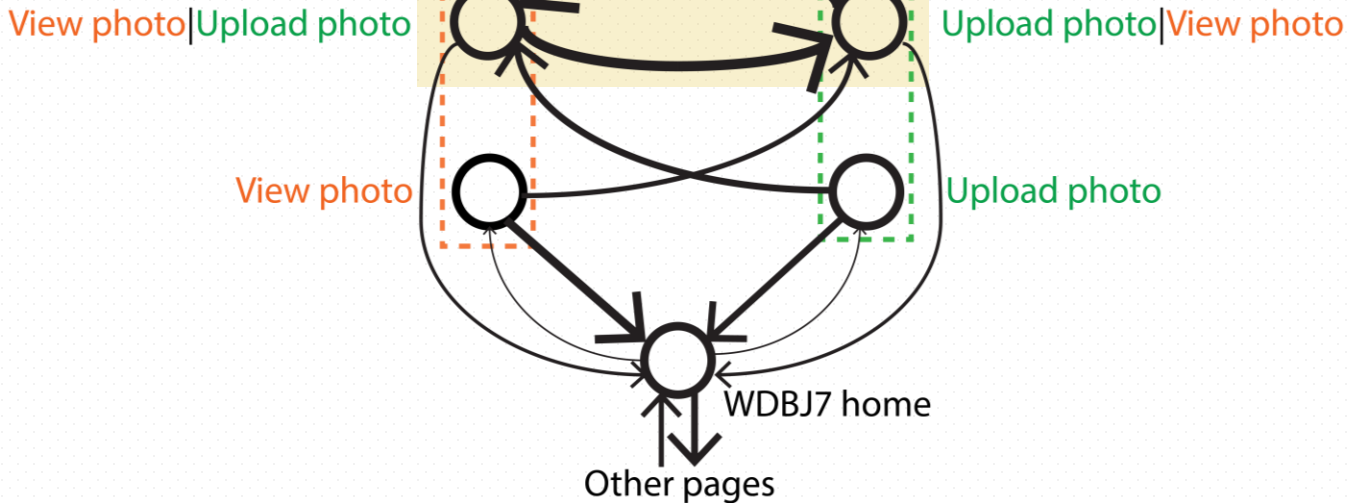


Ranking on clickstream network

First-order network

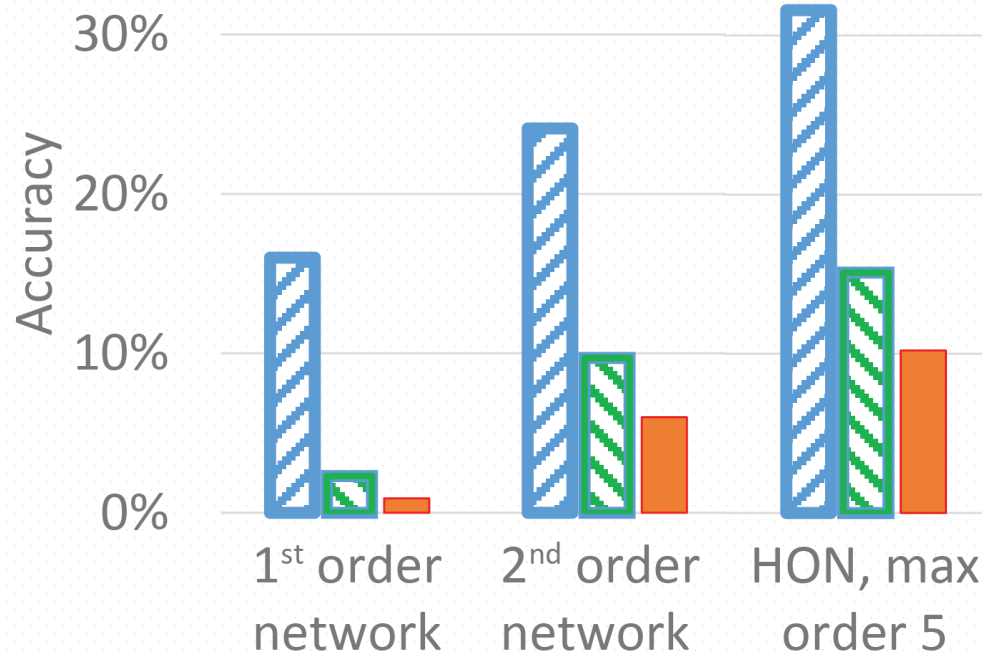


HON

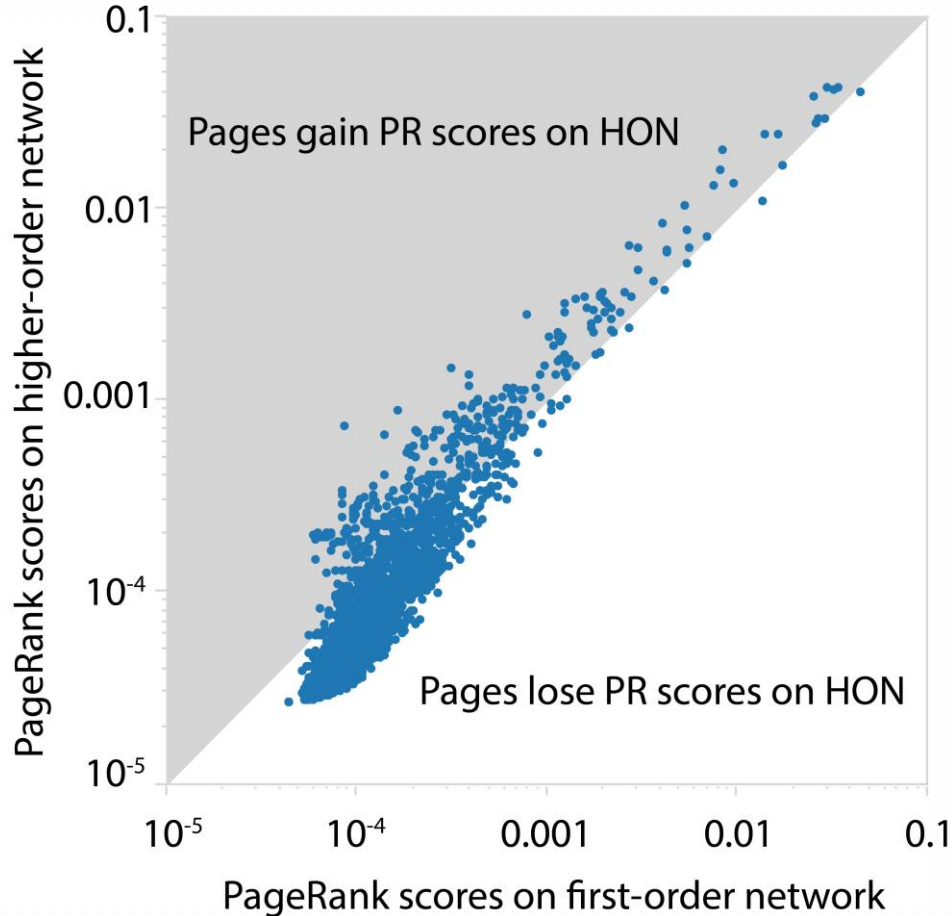


Ranking on clickstream network

Simulate 1 step Simulate 2 steps Simulate 3 steps



Ranking on clickstream network



- 26% pages show more than 10% changes in ranking
- More than 90% pages lose PageRank scores, while a few pages gain significant scores

**No changes
to the ranking algorithm**

Algorithm 3 HONOR rule extraction algorithm. Given the raw sequential data T , extracts arbitrarily high orders of dependencies, and output the dependency rules R . Optional parameters include $MaxOrder$, $MinSupport$, and $ThresholdMultiplier$

```

1: define global  $C$  as nested counter
2: define global  $D, R$  as nested dictionary
3: define global  $SourceToExtSource$ ,  $StartingPoints$  as dictionary
4:
5: function EXTRACTRULES( $T$ , [ $MaxOrder$ ,  $MinSupport$ ,  $ThresholdMultiplier = 1$ ])
6:   global  $MaxOrder$ ,  $MinSupport$ ,  $Aggressiveness$ 
7:   BUILDFIRSTORDEROBSERVATIONS( $T$ )
8:   BUILDFIRSTORDERDISTRIBUTIONS( $T$ )
9:   GENERATEALLRULES( $MaxOrder$ ,  $T$ )
10:
11: function BUILDFIRSTORDEROBSERVATIONS( $T$ )
12:   for  $t$  in  $T$  do
13:     for ( $Source, Target$ ) in  $t$  do
14:        $C[Source][Target] += 1$ 
15:        $IC.add(Source)$ 
16:
17: function BUILDFIRSTORDERDISTRIBUTIONS( $T$ )
18:   for  $Source$  in  $C$  do
19:     for  $Target$  in  $C[Source]$  do
20:       if  $C[Source][Target] < MinSupport$  then
21:          $C[Source][Target] = 0$ 
22:       for  $Target$  in  $C[Source]$  do
23:         if then  $C[Source][Target] > 0$ 
24:            $D[Source][Target] = C[Source][Target] / (\sum C[Source][*])$ 
25:
26: function GENERATEALLRULES( $MaxOrder$ ,  $T$ )
27:   for  $Source$  in  $D$  do
28:     ADDTORULES( $Source$ )
29:     EXTENDRULE( $Source$ ,  $Source$ , 1,  $T$ )
30:
31: function KLDTHRESHOLD( $NewOrder, ExtSource$ )
32:   return  $ThresholdMultiplier \times NewOrder / \log_2(1 + \sum C[ExtSource][*])$ 

```

Algorithm 3 (*continued*)

```
33: function EXTENDRULE(Valid, Curr, order, T)
34:   if Order ≤ MaxOrder then
35:     ADDTORULES(Source)
36:   else
37:     Distr = D[Valid]
38:     if  $-\log_2(\min(\text{Distr}[*].\text{vals})) < \text{KLDTHRESHOLD}(\text{order} + 1)$ , Curr then
39:       ADDTORULES(Valid)
40:     else
41:       NewOrder = order + 1
42:       Extended = EXTENDSOURCE(Curr)
43:       if Extended = ∅ then
44:         ADDTORULES(Valid)
45:       else
46:         for ExtSource in Extended do
47:           ExtDistr = D[ExtSource]
48:           divergence = KLD(ExtDistr, Distr)
49:           if divergence > KLDTHRESHOLD(NewOrder, ExtSource) then
50:             EXTENDRULE(ExtSource, ExtSource, NewOrder, T)
51:           else
52:             EXTENDRULE(Valid, ExtSource, NewOrder, T)
53:
54: function ADDTORULES(Source):
55:   for order in [1..len(Source) + 1] do
56:     s = Source[0 : order]
57:     if not s in D or len(D[s]) == 0 then
58:       EXTENDSOURCE(s[1:])
59:     for t in C[s] do
60:       if C[s][t] > 0 then
61:         R[s][t] = C[s][t]
62:
63: function EXTENDSOURCE(Curr)
64:   if Curr in SourceToExtSource then
65:     return SourceToExtSource[Curr]
66:   else
67:     EXTENDOBSERVATION(Curr)
68:     if Curr in SourceToExtSource then
69:       return SourceToExtsource[Curr]
70:     else
71:       return ∅
```

Algorithm 3 (continued)

```

72: function EXTENDOBSERVATION(Source)
73:   if length(Source) > 1 then
74:     if not Source[1 :] in ExtC or ExtC[Source] =  $\emptyset$  then
75:       EXTENDOBSERVATION(Source[1 :])
76:   order = length(Source)
77:   define ExtC as nested counter
78:   for Tindex, index in StartingPoints[Source] do
79:     if index - 1  $\leq$  0 and index + order < length(T[Tindex]) then
80:       ExtSource = T[Tindex][index - 1 : index + order]
81:       ExtC[ExtSource][Target]+ = 1
82:       StartingPoints[ExtSource].add((Tindex, index - 1))
83:   if ExtC =  $\emptyset$  then
84:     return
85:   for S in ExtC do
86:     for t in ExtC[s] do
87:       if ExtC[s][t] < MinSupport then
88:         ExtC[s][t] = 0
89:         C[s][t]+ = ExtC[s][t]
90:         CsSupport =  $\sum$  ExtC[s][*]
91:         for t in ExtC[s] do
92:           if ExtC[s][t] > 0 then
93:             D[s][t] = ExtC[s][t]/CsSupport
94:             SourceToExtSource[s[1 :]].add(s)
95:
96: function BUILDSOURCETOEXTSOURCE(order)
97:   for source in D do
98:     if len(source) = order then
99:       if len(source) > 1 then
100:         NewOrder = len(source)
101:         for startingin[1..len(source)] do
102:           curr = source[starting :]
103:           if not curr in SourceToExtSource then
104:             SourceToExtSource[curr] =  $\emptyset$ 
105:           if not NewOrder in SourceToExtSource[curr] then
106:             SourceToExtSource[curr][NewOrder] = {}
107:             SourceToExtSource[curr][NewOrder].add(source)

```

Rank	Risk of single-step direct invasion	Risk of multi-step indirect invasion
1	Murmansk, RUS	Tromso, NOR
2	Tromso, NOR	Reykjavik, ISL
3	Dudinka, RUS	Murmansk, RUS
4	Glomfjord, NOR	Hammerfest, NOR
5	Hammerfest, NOR	Nuuk, GRL
6	Kirkenes, NOR	Kirkenes, NOR
7	Grundartangi, ISL	Harstad, NOR
8	Harstad, NOR	Dutch Harbor, USA
9	Hammerfall, NOR	Grundartangi, ISL
10	Bodo, NOR	Aasiaat, GRL

The method also adapts to

Transportation



Flow of information



Evolution of diseases



Raw data

Rule
extraction

Network
wiring

HON

Sequential data

①

Ship-001: ..., Tokyo, Singapore, Los Angeles, ...
Ship-002: ..., Shanghai, Singapore, Seattle, ...
⋮

Raw data

Rule
extraction

Network
wiring

HON

Sequential data

①

Ship-001: ..., Tokyo, Singapore, Los Angeles, ...
Ship-002: ..., Shanghai, Singapore, Seattle, ...
⋮

Count subsequences of various orders

Singapore → Los Angeles: 60
Singapore → Seattle: 65
Shanghai → Singapore → Los Angeles: 30
Shanghai → Singapore → Seattle: 5
⋮

Sequential data

①

Ship-001: ..., Tokyo, Singapore, Los Angeles, ...
 Ship-002: ..., Shanghai, Singapore, Seattle, ...
 ⋮

Count subsequences of various orders

②

Singapore → Los Angeles: 60
 Singapore → Seattle: 65
 Shanghai → Singapore → Los Angeles: 30
 Shanghai → Singapore → Seattle: 5
 ⋮

Probability distributions: 1st order

$$P(X_{t+1}|X_t = \text{Singapore}) = \begin{cases} \text{Los Angeles: 4.8\%} \\ \text{Seattle: 5.2\%} \\ \vdots \end{cases}$$

Source node
Target nodes

Sequential data

①

Ship-001: ..., Tokyo, Singapore, Los Angeles, ...
 Ship-002: ..., Shanghai, Singapore, Seattle, ...
 ⋮

Count subsequences of various orders

②

②

Singapore → Los Angeles: 60
 Singapore → Seattle: 65
 Shanghai → Singapore → Los Angeles: 30
 Shanghai → Singapore → Seattle: 5
 ⋮

Probability distributions: 1st order

$$P(X_{t+1}|X_t = \text{Singapore}) = \begin{cases} \text{Los Angeles: 4.8\%} \\ \text{Seattle: 5.2\%} \\ \vdots \end{cases}$$

Source node
Target nodes

Probability distributions: 2nd order

$$P(X_{t+1} | X_t = \text{Singapore}, X_{t-1} = \text{Shanghai}) = \begin{cases} \text{Los Angeles: 86\%} \\ \text{Seattle: 14\%} \\ \vdots \end{cases}$$

Extended source node
Target nodes

